TITLE
INSTITUTION
PUB DATE
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PUB TYPE

EDRS PRICE DESCRI PTORS

Superstars II, Primary. A Standards of Excellence Curriculun Project for Primary-Level Students. Florida State Dept. of Education, Tallahassee. [86]
337p.; For a relised document, see SE 048578. Public School Resource Center, Florida Department of sducation, Knott Building, Tallahassee, FL 32301 (\$5.00) .
Guides - Classroom Use - Materials (For Learner) (051) -- Guides - Classroom Use - Guides (For Teachers) (052)

MF01/PCl4 Plus Postage.
*Basic Skills; Elementary Education; *Elementary School Mathematics; *Mathematical Enrichment; Mathematics Curriculum Mathematics Education; Mathematics Instruction; *Mathematics Skills; *Minimum Competencies; Primary Education; Problem Solving; State Boards of Education; *Teacher Aides; Teaching Methods; Volunteers *Florida


#### Abstract

The accountability movement has forced educators to expend energys during the past few years ensuring that students master a developmental sequence of skills in the major content areas. In mathematics this has resulted in an emphasis upon computational proficiency, and, in the view of many mathematics educators, not enough time has been spent on problem-solving skills. This material was designed to be systematic approach to curriculum enrichment so that much of the work can be handled by someone other than a classroom teacher, freeing the teacher to work with students on problem solving, creative thinking, and critical thinking. Superstars II is offered as an opportunity for self-motivated students who choose to become involved in the program. The program is managed by an adult (volunteer, aide, etc.) and focuses on the acquisition of the "skills for excellence" identified for Florida schools. This document includes: (1) a description of the Superstars program; (2) student worksheets for grades one, two, and three; and (3) teacher comentary for the atudent worksheets, including the skills of excellence for third grade. (TW)


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## ACKNOWLEDGEMENTS

This project was concaived of, coordinated by, and supported financially through the Florida Departinent of Education (DOE). Student materials were developed, field tested, and reviewed by a large number of florida's district teachers, principals, supervisors and DOE consultants.

Many of the problems in SUPERSTARS II are adaptations of problems from the National Council of Teachers of Mathematics (NCTM) publications, Long Island Mathematical Olympiads for Elementary Schools (LIMOS), and Brevard County's Project Magic. We gratefully acknowledge these contributions.

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Providing appropriate educational experiences for the entire spectrum of students found in most elementary classrooms is a very real problem. Accountability has forced educators to expend most of their energies during the past few years ensuring that students master a developmental sequence of skills in the major content areas. Society has generally interpreted such sequences in elementary mathematics as leading primarily to computational proficiency. One consequence of this emphasis is that not as much time is available for activities that develop basic problem-solving skills that go beyond the minimal, nor for enrichment experiences that expand a student's creative tendencies.

In 1984, Florida's State Board of Education adopted "Standards of Excellence" as benchmark indicators of what able students in quality programs should strive for in mathematics. These skills are written for students who have completed the 3 rd, 5 th, $8 t h$, and 12 th grades. Those skills that pertain to the elementary grades are listed in the first few pages of the Teacher Commentary section of this package. This material is intended to provide a supplementary program to help students learn and practice these "skills of excellence" over a five- year period.

This material uses a systematic approach to curriculum enrichment that is designed so that much of the work can be handled by someone other than a classroom teacher, freeing the teacher for the part that he or she does best-helping students learn how to think critically and creatively. The system is not meant to replace any aspect of the normal school curriculum--it is offered as a peripheral opportunity to self-motivated students who identify with challenges, who want to do more in school than we ask of them, and who enjoy being rewarded for their extra efforts. Since progress toward "excellence" requires a commitment on the student's part, participation in SUPERSTARS should be optional--only those students who choose to become involved will be successful in the program, over a full academic year. Any student, regardless of prior achievement in mathematics, should be allowed to participate as long as they remain interested in the program.

We believe that our schools will respond to this program by recruiting several dedicated adults who can spend the few hours each week making the system operate effectively in a school. We believe that Florida's teachers will well come this supplementary program intended to enhance their daily efforts to get children to use higher-level thought processes. And finally, we believe that Florida's elementary students will far surpass our initial expectations in demonstrating "excellence" in elementary mathematics.


## ORGAMIZATION OF THESE MATERIALS

Section 1 ... Description of the SUPERSTARS II program

1) General information
2) Information/checklist for principals
3) Information/checklist for assisting adults
4) Information for teachers
5) Letter to participating students and their parents

Section 2 ... Student worksheets

1) For grade 1, numbers I through $\mathbf{X X Y}$
2) For grade 2, numbers I through XXV
3) For grade 3, numbers I through XXY

Section 3 ... Teacher Commentary for student worksheets

1) Skills of Excellence for 3rd grade, end-of-year
2) Teacher Commentary for grade 1, worksheets I through XXY
3) Teacher Commentary for grade 2, worksheets I through XXV
4) Teacher Commentary for grade 3, worksheets I through XXV

## SUPERSTARS II: GENERAL INFORMATION

SUPERSTARS II is a program designed to be managed by an assisting adult (volunteer, aide, etc.) and supported by school administrators and classroom teachers. Each has a key role to play in the success of the program. Instiuctions for each role are described in the succeeding pages.

Students choose on their own to participate in SUPERSTARS II. A weekly cycle is established early in the school year, and follows this format:

On Monday of each week, student worksheets are distributed by the assisting adult to those in the program. Students have until Friday to complete the problems, working entirely on their own. On Friday, the classroom teacher hosts a brief problem-solving session for the students in the program, discussing the more difficult problems on the worksheet for that week.

Students get double-credit for those problems they completed correctly prior to the problem-solving session, and regular credit for those they complete over the week-end. On Monday all papers are handed in, checked by the assisting adult, and stars posted as a reward for working individual problems. This completes the cycle for the preceding week, allows for the new worksheets to be passed out, and the cycle begins again.

The use of calculators is permissable.
The visual reinforcement of seeing their names displayed in a prominent place in the school, with a string of stars indicating their success, is the basic reward a student receives for the extra work. Some competition will naturally emerge among the students who accumulate a good many stars, but the system does not rely on this competition for its success. Some students will continue in the program week after week, even though they are earning only a few stars. This is particularly evident when schools enhance the basic reward system by awarding varying prizes for attaining different levels of success.

SUPERSTARS II is not a program for every child--it's only for those who are self-motivated and who are not frustrated by challenging situations. This does not diminish the value of the program, but rather makes us realize that "excellence in elementary mathematics" requires something special on the part of the child. Those children who complete the SUPERSTARS program are in the process of becoming excellent mathematics students.

## SUPERSTARS II: INFORMATION FOR PRINCIPALS

SUPERSTARS II is a curriculum enrichment package designed to be managed by volunteer assisting adults, with coordinated teaching by the classroom instructor. The purpose of the program is to help students learn the "skills of excellence" identified for florida schools, in the subject area of mathematics. The compiete set of material comes in two packages, one for grades 1, 2, and 3, and the other for grades 4 and 5. Worksheets from the origial SUPERSTARS package can be used for students in grade 6.

As an administrator, you need to:
become thoroughly familiar with the program;

* duplicate for each teacher a copy of the worksheets and teacher commentary for that grade level, and then introduce the program at a faculty meeting early in the year;
* speak to parents at your school's first "open house" of the year, explaining the purpose of the program and the long-term value of their child working independently on the worksheets; and
* recruit or assign several assisting adults (volunteers, aides, etc.) who are enthusiastic, dependable people to manage the program. Early in the year, meet with the assisting adults to plan the following details:

1. A prominent place and format for the STAR CHART.
2. A place and time each Monday for the assisting adult to be in the school.
3. A system for the activity sheets to be duplicated each week. They must be clear and legible.
4. A plan for extra incentives for accumulating stars. ("World records" to be kept from year-to-year, or a "brain bowl" planned for the end of school. Can students earn SUPERSTAR prizes for attaining certain levels of success? See the reverse side of this page for examples.)
5. A schedule for when the program will start. Will there be opportunities later in the year for others to start? Will a new chart be started at the beginning of each quarter or each succeeding grading period? (Review a school calendar, and work backwards from the end of the yea:, using only weeks that have at least 4 school days. You'll need 25 weeks for the primary program, and 28 for the intermediate program).

* monitor the program every two weeks to clear up any unforeseen problems. Administrators need to be highly visible.

SUPERSTARS is an optional program for students. It should be available to any student who wants to try it, regardless of prior success in mathematics. You should expct to see a large group of students begin the program, but a
majority of them will lose interest. The small group that stays involved with SUPERSTARS over the fill academic year are self-motivated students with good study habits, the sort most likely to become "excellent" students.


SUPERSTARS II is designed to be managed by assisting adults and supported by teachers, administrators, and parents. The success of the program will depend on this team effort. Reliability and punctiality are important-students will rapidly learn to depend on the assisting adult being there each week, checking their oapers, and posting their stars. If possible, wear an outfit that fits in with the SUPERSTARS logo; students will quickly begin to identify you as an imporiant person in their school.


SUPERSTARS II works on a weekly cycle. Each Monday, you collect the worksheet from the previous week and distribute new worksheets to the participating students from your SUPERSTARS area in the school. You then check the worksheet from the previous week and post the stars earned on the STAR CHART.

Students have from Monday until Friday to work the problems entirely on their own--the only help they can receive is to have someone read the problems to them. On Friday, the teacher will host a problem-solving session in the classroom, discussing how to approach the more difficult problems. Students who have al ready worked the problems (prior to the problem-solving session) can earn double the number of stars--you can tell these by looking for the teacher's initials beside certain problems. The students will have from Friday until Monday to re-do those problems they did not understand--for these problems, they earn the indicated number of stars if they are correct.

There are a number of creative ways to format the STAR CHART. The basic method of posting stars one at a time will probably eventually yield to a color-coded system, or one that involves posting only 1 star per week, with a number inside it. Try to personalize the chart and the entire SUPERSTAR $\dot{J}$ areas with pictures of the students, "smiling faces," etc. Be creative--your efforts will be rewarded by seeing enthusiastic students making progress toward mastering high-level thinking skills.

As an assisting adult, you will need to:
Plan with the principal the following:

1. A prominent place and format for the STAR CHART,
2. the time and place each Monday for you to take up and check papers and distribute new worksheets,
3. the system for duplicating each week's worksheets, ensuring legible copies, and
4. which, if any, extra incentives ("world records," stickers, coupons, pencils, tee shirts, etc.) will be part of the system for rewarding various levels of achievement in SUPERSTARS II.

Make the SUPERSTARS spot a happy place with bright col ors, smiles, and cheerful words. Show confidence, friendliness, and encouragement to students.

Collect the letters, signed by the student and parent, which is sent home prior to the first activity sheet. If at any time you have good evidence that a student is getting nelp on the problems, mention it to the classroom teacher.

Check the worksheet from the previous week consistently. If you decide to give partial credit for a problem with several parts, award the stars consistently and be firm, but fair, in explaining this to students who question it. Do not give partial credit for problems with only one answer.

Allow students to see the answers to problems when they hand in a worksheet and to defend an answer that is different from the given answer. If they used clear logic in arriving at a unique answer, give them full credit.

Leave extra worksheets with the classroom teacher for students who were absent on Monday. Allow a worksheet to be turned in late only if the student was absent on Monday. If a worksheet does nct have a student's name in the proper place, check the paper but award the stars to "No name" on the STAR CHART. Adhering strictly to these rules will teach responsibility to the students, and keep your work load manageable.

Keep all returned worksheets. Do not give them back to the student, since the same worksheets are used year-after-year.

On the Mondays when SUPERSTARS II will not be available (perhaps a vacation shortens the week too much), post a sign such as "No star problems this week, but come back next week, please!"

## SUPERSTARS 1I: INFORMATION FOR TEAC IERS

SUPERSTARS II is designed to help you teach the mathematics Skills of Excellence adopted by Florida's State Board of Education in 1984. It is intended to complement, not replace, your normal curriculum by offering peripheral opportunities to self-motivated students who frequently exceed normal expectations.

The program is designed so that your involvement is strictly as a teacher. SUPERSTARS II will remain "special" to students if it's managed by someone outside the classroom setting, and if the teacher is viewed as a "helper" in the system, rather than as a dominant figure. Your primary role is to monitor the system in your own classroom and host a problem.solving session for SUPERSTARS students on Friday of each week.

A IEACHER COMMENTARY page accompanies each worksheet, and will tell you which Skill of Excellence is addressed by each problem. The Commentary will also give you hints on how to cover the problems in your problem-solving session, without actually giving away the answers. Even though there is a comment for each problem, you will have to decide which 3 or 4 problems you will cover during this brief session. Concentrate on those that require higher-level thinking!

Do not be disappointed if a large number of students in your class begin SUPERSTARS, but some of them drop out after a few weeks. This is a natural phenomenon; problem-solving requires a great deal from students, and only certain ones are ready to accept this sort of challenge. You will notice that certain students do choose to stay in SUPERSTARS week-after-week, even though they aren't as successful in earning stars as other students.

Please read the General Information in the SUPERSTiRS package, to get an overview of the program. The back of this page contains some "helpful hints" that you might find useful in your work with SUPERSTARS II. The use of calculators is permissable. And finally, look over the first few student worksheets for your grade level so that in the weeks before the program starts in your school, you can review in class any terminology or symbolism that might be confusing to students.

SPECIAL NOTE FOR KINDERGARTEN TEACHERS: Because of a reluctance to design a paper-and-pencil-dependent system for such young students, SUPERSTARS II does not include student materials for your students. Many of them will be ready for the type of activities we have at the beginning of the first grade material, however, by the end of your year with them. We encourage you to look at the first grade worksheets, and begin incorporating such problem experiences, at a concrete level, into your kindergarten curriculum toward the end of the year.

Allow your students to leave the classroom at the designated time on Monday morning to turn in their worksheets and pick up new ones. The "assisting adult" will take a few extra minutes, and read the new worksheet to students in the primary grades.

Read e.'h week's worksheet yourself, and feel free to structure classroom activities that parslle; those on the SUPERSTARS worksheets. However, please do not "teach to the worksheets."

During the school week, students can work on SUPERSTARS during their spare time, but the only help they can receive is for some adult to read the problems to them. Give them one warning if ou see them discussing the worksheets, and take away their papers for the next violation.

Host a brief problem-sclving session for SUPERSTAR participants on Friday. Remember these points:

Students come to this session with their worksheets, but without pencils.

The session nust be brief- -15 minutes at most. Discuss only the 3 or 4 more difficult problems on the sheet.

Do not give answers to the problems. Rather, concentrate on approaches to the problems.

Help students surmarize their own approaches to the problems, in a non-judgemental fashion. Offer your own approach last, and only when it's different from the student strategies.

End the session by encouraging students to complete the problems they haven't done, over the week-end. Put your initials beside any problem discussed in class which a student has already done, if the answer is correct. The assisting adult will award "double stars" for these.

Remember that part of the SUPERSTARS program is to teach responsibility. Students will rapidly learn to follow whatever rules structure a program, if the program is important to them. SUPERSTARS becomes very important to certain students, so they will adhere to rules about where their name goes on each paper, no credit if they forget their worksheet on Monday, no talking about the problems, etc., if you enforce the rules.

Enjoy SUPERSTARS. Students will impress you with their ability to think, and their creative ways to solve problems that seem to be above their level.

SUPERSTARS II is for kids who enjoy extra work, with very little pay! All you might get for this extra work are some stars on a chart. But at least your friends and parents will know that you're a SUPERSTAR, because your stars will be placed in the school where everybody can see them.

You can get a worksheet full of problems each Monday, and you'll have until Friday to do them in your spare time. Your classroom teacher will show you how to begin the harder problems on Friday, if you haven't already finished them. You can do those problems over the week-end, but on Monday you have to turn in the worksheet to get your stars. If you forget to turn in the paper, or to put your name on the paper in the right place, you won't get your stars!
You don't have to take a worksheet every week--if you get tired or want a vacation, you can skip a week. You also don't have to do every problem on each sheet. All worksheets should be turned in on Monday, even if only one problem is completed. Those completed by Friday earn double credit.
There is one big rule -- you can't talk about the problems with anyone uritil you have turned in the worksheet. (Your teacher and parents will know about this rule, too, and remind you.) An adult can read any problem out loud to you if you can't read it yourself. When you sign your name on the worksheet and turn it in, you are saying that you didn't receive any help or give any help to other students.

If you have read this letter and want to become a part of SUPERSTARS, sign below. Have your parents read the other side of this sheet and sign it al so. Then turn this page in before you receive your first worksheet.


Your signature

Your child has indicated an interest in starting the SUPERSTARS II mathematics enrichment program. The purpose of the program is to help students become "excellent" students of mathematics, over a several-year time period.

Most of SUPERSTARS II is problem solving. Your child will be given a worksheet full of problems on Monday, and have until Friday to solve them completely on his/her own. You can read the problems to your child if he/she is having difficulty with the words, but that is the only help youl can give. On Friday, the teacher will discuss how to approach the more difficult problems. Your child will then have the week-end to re-do the harder problems before turning the worksheet in on Monday. The advantage to doing the problems by Friday is that the child receives double credit for doing them prior to getting help.

How can you help your child be successful with SUPERSTARS? Perhaps the best way is to establish a work schedule that allows enough time each week to think about the problems prior to Thursday night. A schedule like the one below often helps:

Monday night: The child reads all the problems, to understand the problem situations.

Tuesday night: The child reads all the problems again, and does the easy ones.

Wednesday night: The child reads the remaining problems again, and tries one or two harder ones.

Thursday night: The child finishes the worksheet, doing as much as he/ she can.

Help your child understand that he/she will rarely be able to do all the problems on a worksheet prior to the Friday "help session." But learning how to approach the harder problems will pay off in the end, since he/she will see problems like them in the future.

SUPERSTARS II is entirely optional for students. When the "lure" of participating in a new program begins to wear off and students realize how difficult some of the problems are, some will lose interest and drop out. This is a natural phenomenon and reflects that SUPERSTARS is for selfmotivated students with good work habits. If your child decides to discontinue SUPERSTARS, allow him/her to do so in a non-judgemental fashion-perhaps they'll pick it up again later on their own, when they're ready for this type of experience. As long as he/she is participating in SUPERSTARS, remain interested in their progress but not "pushy" about the program.

If you agree for your child to begin SUPERSTARS II, sign below:

# WORKSHEETS 

FOR
GRADE 1

## STAR PROBLEMS

GRADE 1, I

* 1. FIVE LITTLE A's FLYING HIGH,

SIX MORE COME TO SIT NEARBY,
HOW MANY 'S IN ALL?

ANSWER: $\qquad$ 'S IN ALL.
 HOW MANY OS DO NOT HAVE A ROCK?

ANSWER: $\qquad$

* 3. ANN CAN EARN 10¢ A DAY FOR DOING GOOD WORK. HOW MUCH MONEY DID SHE GET THIS WEEK?

ANN


ANSWER: AND, EARNED $\qquad$ THIS WEEK,
$\star \star 4$. ABOUT HOW TALL IS EACH PICTURE?


WRITE A NUMBER SENTENCE TO SHOW HOW FAR THE BOY JUMPED.

ANSWER: $\qquad$
$\star \star$ 6. ADD OR SUBTRACT FOR EACH STEP IN THIS FLOWCHART, WRITE YOUR ANSWER IN THE FINAL BOX.

$\qquad$ grade l, II
$\star \star \star \star 1$. HOW MANY WAYS CAN YOU PUT 5 fish in 2 BOWLs?

make a table to show all the ways.

$\star \star \star 2$. USE $A$
to do each problem below, write your answer in the RIGHT

*** 3 。

(A) HOW MANY LEGS ON 4 cows?
(b) how many legs on 7 chicks?
(c) HOW MANY LEGS ON 2 cows and 3 chicks together?
$\star \star \star \star 4$, bOB SPENT 26 CENTS ON 3 toys, CIRCLE THE TOYS.

$\qquad$
$\star \star \star$ 1, 0. K., SUPERSTAR, WHAT NUMBER IS MISSING ON THE STAR SO THAT THE SUM is 17 ?

Answer:

$\star \star$ 2. YOU ARE THE NEW ZOO KEEPER. YOUR FIRST JOB IS TO COUNT THE dots on spot. How many dots ARE THERE?

Answer: $\qquad$

* 3. WHICH ANIMAL IS HEAVIER? COLOR THAT ANIMAL.
$\qquad$


## STATE YOUR CLAIM!



TEXAS

KANSAS

FLORIDA
$\star \star \star \star$ 5. Jan watches sesame street for 1 hour and cartoons for 2 hours each school day. how many hours does she spend Watching these programs each week?

Answer: $\qquad$ HOURS
$\star \star$ 6. FIND THE PATTERN AND FILL IN THE EMPTY BOXES.


* 7. congratulations! you are a star! you are not the last star. you are not the second star but you are to the left of the SECOND STAR. COLOR THE STAR THAT yuiu ARE.


22
** 1. HOW MANY TRIANGLES CAN YOU FIND IN The picture to the right?

ANSWER: _ TRIANGLES

tht 2. THERE ARE TOO MANY FISH IN THE FISH BOWL, TAKE ENOUGH OF THEM OUT AND PUT THEM IN THE OTHER BOWL SE YOU WILL HAVE THE EXACT SAME NUMBER IN BOTH BOWLS. HOW MANY DO YOU HAVE TO MOVE?

ANSWER: $\qquad$

$\star \star \star$ 3. how many ears are there in THIS GROUP OF DOGS?


ANSWER: $\qquad$
how many legs are there in THIS GROUP OF DOGS?

ANSWER: $\qquad$
$\star \star \star \star$ 4. PLace the numbers $1,2,3,4,5$, and 6 in the cikcles so that the sum along each side is 10.

$\star \star \star$ 5. HOW MANY WAYS CAN YOU PUT 7 fish in 2 bOWLs?

make a table to show all the ways.


ANSWER: there are __ ways to put 7 fish in 2 bowls.

* 6. HOW MANY dOLLAR BILLS WOULD YOU USE TO PAY FOR THE CAR, IF YOU did not have any coins in your POCKET?


ANSWER:


STAR PROBLEMS

* 1. draw the shape that comes next:
- 18 $\bigoplus \bigotimes$
$\star \star 2$. fill in the box with a number that will make the sentence correct!

$$
10=\square+6
$$

$\star \star$ 3. What is the temperature? print your answer on the line beneath EACH THERMOMETER.

$\star \star 4$. On EACH THERMOMETER, DARKEN-IN THE MIDdLE SECTION TO SHOW THE TEMPERATURE GIVEN.

$75^{\circ}$

** 5. mary had a ten dollar bill, and bought a doll that cost \$7. how much change should she get from the store clerk?
answer: Mary should get $\qquad$ BACK.

* 6, hold this paper up, and fold it so that you divide the line EXACTLY IN HALF, YOU CAN DO IT IF YOU PUT ONE END POINT ON TOP OF THE OTHER ONE AND THEN FOLD CAREFULLY,

$\star \star \star \star 7$. PRACTICE ADDING IN YOUR HEAD ON TYE PROBLEMS BELOW, YOU SHOULD FIND NUMBERS THAT ADD TO TEN, rO MAKE YOUR WORK EASIER.




WHEN YOU TURN IN YOUR PAPER, YOU WILL BE GIVEN A PROBLEM LIKE those ABOVE, AND YOU'll HAVE TO DO IT IN YOUR HEAD TO GET YOUR STARS. YOU CAN PUT YOUR ANSWER IN THE BOX BELOW, AS YOU TURN IN YOUR PAPER.

ANSWER:

$\qquad$
thtth 1 , ABOUT HOW TALL IS THE GIRAFFE? ABOUT HOW LONG IS THE NECK? $\qquad$ ABOUT HOW LONG ARE THE LEGS? ABOUT HOW LONG IS THE TAIL? ___

$\star \star 2$. WHAT NUMERAL IS SHOWN BELOW?

$\star$. 3. WRITE THE NUMERAL FOR:

$$
8 \text { TENS + } 4 \text { ONES + } 1 \text { hUNDRED }
$$

ANSWER: $\qquad$
$\star \star 4$. do each step of the flowchart. Write your answer in the empty box.


* $*$ 5. find the number that goes in the first step of the flowchart, to give the correct final answer. Write it in the empty box.

$$
\square+4+2+3=12
$$

6. help the girl get from

START TO EACH OF THE
ANIMALS. TELL HER HOW FAR EAST TO GO, AND THEN how many blocks NORTH.

* TO GET TO GO: 1 EAST AND 3 NORTH.
* TO GET TO GO:

$\qquad$ EAST AND $\qquad$ NORTH.
* to get to 跘 GO:
$\qquad$ EAST AND $\qquad$ NORTH.
* TO GET TO
 GO:


7. DRAW THE SHAPE (CIRCLE, TRIANGLE, OR SQUARE) THE GIRL WOULD FIND, IF SHE TOOK THESE TRIPS:

* 2 blocks East, 1 block North:
$\star 4$ blocks East, 2 blocks North:
$\star 1$ block East, 2 blocks North: $\qquad$

$\star$ 8. how many stars are there in the TRIANGLE? $\qquad$ STARS
* 9. how many stars are in the circle? _ Stars
$\qquad$ grade 1, VII
$\star \star \star$ 1. HOW MUCH DOES THE DUCK COST? WRITE YOUR ANSWER ON THE TAG.
$\star \star \star 2$. yOU buy the duck WITH ONE OF THESE: HOW MUCH CHANGE WOULD YOU GET?

ANSWER: $\qquad$

$\star$ 3. PUT A NUMBER IN EACH EMPTY 4 bOX in the table, to make A TRUE SENTENCE, THE FIRST ONE IS DONE FOR YOU,
$\star \star$ 4. make a graph of the NUMBER OF PIECES OF PIE that each child ate.

\author{

GRAPH <br> | Jill |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Bob |  |  |  |  |  |  |  |
| Joe |  |  |  |  |  |  |  |
| Mary |  |  |  |  |  |  |  |
| 1 |  |  |  |  |  |  |  |
| pieces eaten |  |  |  |  |  |  |  |

}

$\star \star$ 5. jay came to school at
 Jay ate lunch at

how much time passed before jay ate lunch? $\qquad$ HOURS
$\star \star \star$ 6. ABOUT HOW LONG iS SANDY, THE SNAKE? CIRCLE YOUR ANSWER BELOW,
(hint: you may use a ruler, string, or CENTIMETER BLOCKS TO HELP MEASURE.)

about 7 CENTIMETERS
about 10 centimeters
about 13 centimeters
$\star \star$ 7. WHICH WEIGHS MORE, A OR A ?
ANSWER: $\qquad$

$\qquad$ GRADE 1, VIII

* $*$ 1. HOW MANY DIfferent triangles can you find in the FIGURE BELOW?


ANSWER: $\qquad$
$\star \star \star$ 2. put $2,3,4,6,7$, and 8 in the circles so that the sum along each line is 15. use each number just once,


* 3. how many unit squares does it take to make each SHAPE BELOW?
(HINT: A UNIt SQuare is this Size: $\square$ )

※¥₹ 4. Put the numbers inside the barrel where they belong!
Hint: 3 numbers will not belong in any of these barrels.

$\star \star \star$ 5. PUT THE PICTURES BELOW IN ORDER, FROM THE FIRST TO THE LAST ACTIVITY OF A DAY.


STAR PROBLEMS
I DID THIS WORK MYSELF $\qquad$
grade 1, IX
*t 1. ellie the elephant loves peanuts. she ate 20 bags of peanuts in 3 days, she ate 3 bags on the first day. she ate 7 bags on the second day. how many bags did she eat on the third day?

88888


38883
85 588
OB RE
ANSWER $\qquad$
** 2, farmer brown wants to put some more boards on the fence POSTS, TO MAKE A PLACE TO KEEP HIS HORSES. HOW MANY MORE boards does he need to buy?

$\star \star \star$ 3. IF YOU START WITH A NUMBER AND FOLLOW THE ARROWS YOU WILL end with the starting number, write the number in the box.


* 4. barry keeps a chart on visits he makes to the zoo each month, use the chart below to tell what month he made the most visits,

ANSWER $\qquad$

| VISITS TO THE ZOO |  |
| :--- | :---: |
| JANUARY | 2 VISITS |
| FEBRUARY | 0 VISITS |
| MARCH | 5 VISITS |
| APRIL | 3 VISITS |
| MAY | 1 VISII |

5. use the chart above to tell what month barry visited the ZOO 3 TIMES.

ANSWER $\qquad$
6. an angle is where two straight lines meet, put an $X$ on the angles you see on the picture of a lamp.

** 7. Lenny wanted to fill a container with lemonade, he needed 4 glasses to fill the container, each glass held 2 ounces of LEMONADE, HOW MANY OUNCES DID THE CONTAINER HOLD?

$\star \star \star$ 1. put 2, 3, 4, 6, 7, and 8 in the circles so that the sum along each line is 19. Use each number just once.


* 2. Which weighs more? circle the animal.

$\star \star$ 3. amy got up at 7:00 am. What time will it be in three hours?

$\star \star$ 4. COLOR THE SHAPES That CAN be folded to match.

$\star \star \star$ 5. jan has a toy train. she placed george's house 2 meters FROM SUSAN'S HOUSE, GUESS HOW FAR IT IS FROM GEORGE'S house to barry's house, circle the answer.

$\star \star$ 6. JODY DID THIS PROBLEM ON HER CALCULATOR.

SHE PUSHED

 What answer did she see?

Answer:
$\star \star$ 7. LOOK at this flowchart. Circle the missing
take A Bath

EAT BREAKFAST

EAT DINNER

GO SWIMMING

$\star \star 1$ 。


ANSWER: $\qquad$
*** 2 .


Pablo wants a top, a kite and a hat. How much will they cost
in all?
ANSWER:

* 3. Circle the word that makes this statement true,

You would measure the length of your classroom in $\qquad$ . CELSIUS LITERS METERS GRAMS

* 4. If your mother made 24 cgokies and you ate 1 cookie, how MANY COOKIES DID YOU EAT?

ANSWER:

* 5. Is this number sentence true or false?

$$
7+5=6+6
$$

ANSWER:
$\star$ 6. You leave home at 3:30 pim. Your mother tells you to be home in one hour. What time must you be home?

ANSWER:
$\star \star \star$ 7. Jenny asked the students in her class which color they liked best. She made this table.

| COLOR | NUMBER |
| :--- | :---: |
| RED | 10 |
| BLUE | 8 |
| YELLOW | 6 |
| GREEN | 3 |
| PURPLE | 7 |

A) How many students liked blue best?
B) Which color was chosen 7 times?
C) Most of the students liked which color best?
** 8. Find the answer to this problem by using a calculator.

$$
9833-4296
$$

ANSWER: $\qquad$

TURN THE CALCULATOR UPSIDE DOWN.
The answer spells a word that is the opposite of "more." What is the word?


STAR PROBLEMS grade 1, XII

1 DID THIS WORK MYSELF: $\qquad$
it t* 1. how many 2-digit numerals can you MAKE, USING THE DIGITS IN THE BOX?

ANSWER: I CAN MAKE $\qquad$ NUMERALS.


* 2. For your birthday, your Grandma gives you $\$ 1$, your mom gives you \$2, and your dad gives you \$4. how much money DID YOU GET FOR YOUR BIRTHDAY?

IF YOU WANT to buy a sticker book for \$5, how much will you have left?

* 3. how many centimeters long is this pencil? CIRCLE THE CORRECT ANSWER.
(A) 1 cm
(B) 5 cm
(c) 10 cm

(D) 20 cm
t*** 4. FILL IN EACH SQUARE WITH A NUMBER SO THAT EACH LINE ACROSS AND DOWN, HAS A SUM OF 11.

* 5. put the number shown by each picture, in the square.

* 6. an angle is a corner where Two straight lines meet. how many angles are there in the shape to the right?


ANSWER: $\qquad$ ANGLES

* 7. draw a handle on this fork. make the handle 10 centimeters long.

$\star \star \star$ 8. A Penny has two sides. the side with a person's face is called "heads", and the other side is called "tails."
toss a penny in the air 10 times, and let it land on the floor. mark on the chart below each head and each tail you get.


Which side landed up most often, or did heads land up the same NUMBER OF TIMES AS TAIIS?
$\qquad$

* 1. how many pennies are there below?

ANSWER: $\qquad$

*t 2. If you and a friend shared the pennies above equally, HOW MANY PENNIES WOULD YOU GET? ANSWER: I'd GET __ PENNIES.
$\star \star \star \star$ 3. HOW MANY PENCILS COULD YOU BUY WITH 20 PENNIES?

ANSWER: $\qquad$ PENCILS

$\star \star \star$ 4. you have 20 pennies, how mujch money WOULD YOU HAVE LEFT IF YOU BOUGHT ALL THE PENCILS YOU COULD BUY?
$\qquad$ $\xi$ LEFT.
$\star \star$ 5. put an $X$ on any of the toys you could buy with a one-dollar bill.

$\star \star$ 6. draw a line to the number that is the correct sum or difference.

$\qquad$
Grade 1, XIV
$\star \star \star$ 1. COLOR THE BEAR RED AT:
EAST 3, NORTH 3
COLOR THE BEAR BLUE AT:
EAST 1, NORTH 2
COLOR THE BEAR GREEN AT:
EAST 2, NORTH 3


* 2. LOOK AT THE THERMOMETERS BELOW. WHAT IS THE TEMPERATURE SHOWN ON EACH THERMOMETER? WRITE THE TEMPERATURE IN THE BLANK BELOW THE THERMOMETER.

$\star \star \star$ 3. there are too many fish in the fish bowl. take enough of them out and put them in the other bowls so you will have the exact same number in all three BOWLS. HOW MANY WILL YOII HAVE IN EACH BOWL?

ANSWER:
FISH


* 4. JOSE'S CLASS MADE A GRAPH SHONNG DIFFERENT KINDS OF PETS THEY OHNED. THEIR GRAPH LOOKED LIKE THIS:


HOW MANY CHILDREN OWNED DOGS? $\qquad$
HOW MANY CHILDREN OWNED CATS? $\qquad$
HOW MANY CHILDREN OWNED FISH? $\qquad$
$\qquad$

* $\star$ 1. you have 5 pennies and lose 2 pennies. Are the pennies you have LEFT CLOSER IN NUMBER TO THE NUMBER OF SHOES IN A PAIR, OR TO THE NUMBER OF DAYS IN A WEEK?

CIRCLE THE CORRECT ANSWER: SHOES DAYS
$\star \star \star$ 2. Look at the numbers in the square below. draw a line around numbers that add to the numblr of pennies in a dime. find ten more to go with the one that has been done for you.
$\left[\begin{array}{ccccccc|}2 & 6 & 5 & 9 & 8 & 7 & 3 \\ 8 & 4 & 5 & 1 & 3 & 2 & 3 \\ 6 & 1 & 5 & 7 & 4 & 9 & 1 \\ 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \hdashline 8 & 9 & 7 & 6 & 5 & 4 & 3 \\ 1 & 6 & 8 & 4 & 7 & 9 & 5 \\ 7 & 6 & 2 & 6 & 7 & 2 & 9 \\ 5 & 4 & 6 & 3 & 8 & 1 & 8\end{array}\right.$

* 3. the square below is covering up a number. write the correct number in the square,

$$
8+\square=12
$$

$\star \star$ 4. dRAW The correct number of dots in the middle domino below, to fit the pattern.

$\star \star$ 5. the number of corners (vertices) has been written inside EACH FIGURE BELOW:


Write the number of corners (vertices) inside each of these figures:

$\star \star$ 6. If you push these two piles of cubes together, how many will YOU HAVE? CIRCLE THE CORRECT ANSWER:

23

$\star \star \star$ 7. using the map below, how many different paths can you find FROM HOME TO SCHOOL?

ANSWER: THERE ARE _ DIFFERENT PATHS.


STAR PROBLEMS GRADE 1, XVI
*** 1. 3 ducks.
2 bunnies.
1 duck ran amay.
How many were left?

I DID THIS WORK MYSELF $\qquad$


Answer $\qquad$ ANIMALS
*** 2. Help Freida the frog hop back across the pond. Fill in the missing number on the lily pad.


* 3. HOW MuCH MONEY ALL TOGETHER?


Answer $\qquad$

* 4. Which circle has more shaded in?


Answer $\qquad$
47
** 5. How many days in 2 weeks?
Answer ___ DAYS
*** 6. Fill in the missing numbers.

$\therefore$ 7. Frisbee for 15
Hat for 11 द
Yoyo for 13
How much for all 3 together?


ANSWER: $\qquad$

$\star \star \star$ 8. using the map below, how many different paths can you find FROM HOME TO SCHOOL?

ANSWER: THERE ARE __ DIFFERENT PATHS.

$\qquad$

* 1. COLOR:

$\star \star \star$ 2. use the tax chart to find the total that each person spent.


|  | SPENT TAX TOTAL |
| :--- | :---: |
| SUE | $50 \xi+\ldots=\square$ |
| ED | $10 \xi+\ldots=\square$ |
| SAM | $1 \xi+\ldots$ |
| JANE | $5 \xi+\ldots$ |
| MIKE | $25 \xi+\ldots$ |

** 3. A. IS 32 CLOSER TO 30 OR 40?
B. IS 49 CLOSER TO 40 OR 50?
C. IS 38 CLOSER TO 30 OR 40?
D. IS 44 CLOSER TO 30 OR 40?
$\qquad$
$\qquad$
$\qquad$
D. IS 44 CLOSER TO 30 OR $40 ?$ $\qquad$

* 4. the movie started at 3:30. it is 2 hours long. draw the hands to show how the clock will look when the movie ends.


ENDING
TIME
$\star \star \star \star$ 5. PRACTICE ADDING IN YOUR HEAD ON THE PROBLEMS BELOW, YOU SHOULD FIND NUMBERS THAT ADD TO TEN, TO MAKE YOUR WORK EASIER.


WHEN YOU TURN IN YOUR PAPER, YOU WILL BE GIVEN A PROBLEM LIKE THOSE ABOVE, AND YOU'LL HAVE TO DO IT IN YOUR HEAD TO GET YOUR STARS, YOU CAN PUT YOUR ANSWER IN THE BOX BELOW, AS YOU TURN IN YOUR PAPER.

ANSWER:

$\star * 1$.


YOU FED HIM ON MONDAY, TUESDAY, WEDNESDAY, AND THURSDAY. HOW MANY $s=12$ EATEN? ANSWER: $\qquad$

$\star \star$ 2. dRaw the missing shapes on the lines:

$\square \square$
$\Delta$

$\square$ $\longrightarrow$
$\star \star \star$ 3. DRAW A RED BALL AT $(1,2)$. draw a green ball at $(4,1)$. draw a blue ball at $(2,4)$.

$\star \star 4$. BILL SHOT 5 ARROWS. HE SCORED 16 POINTS. ON WHAT NUMBERS DID HIS ARROWS LAND?

ANSWER: $\qquad$ , $\qquad$ , $\qquad$
$\qquad$


* 5. how many small cubes does it take TO MAKE THIS SOLID?

ANSWER: _ CUBES

$\star \star \star \star$ 6. THE SUM OF THESE THREE BLOCKS is 15.

CHOOSE YOUR NUMBERS FROM THE blocks below. make two more piles that have sums of 15.
 you can use a block only 1 TIME!

$\star$ 7. how many more - 's are there than O's in the box?

ANSWER: $\qquad$ MORE $\qquad$
$\star \star \star$ 8. PUT EIther " $\zeta$ " or "\$" beside each number below, so the sentence MAKES GOOD SENSE.
(A) A NEW DRESS MIGHT COST 24.
(b) A battery for a toy might cost 98 .
(c) A SCHOOL LUNCH MIGHT COST 80 .

STAR PROBLEMS
Grade 1, XIX

I did this work myself.
$\qquad$

* 1. Drai the next shape.
$\square \triangle O \square \triangle O \square \triangle O$
?
** 2. The number 4 has a family. Here it is.


DRAW A FAMILY FOR 5.

** 3. Here is a paper clip.
 If you make a chain of them, how many paper clips would you Need to be as long as this pencil?

ANSWER: $\qquad$ PAPER CLIPS


* 4. Fill in the missing dots.

** 5. Put in the missing numbers.

* 6. What is this number?


Answer $\qquad$

* 7. circle the animal who ate the most peanuts.

¥ $¥ \mp$ 8. You have a deck of playing cards. About how many cards would it take to cover this paper? (No overlapping!)

$\qquad$ grade 1, XX
$\star \star$ 1. makf happy faces next to each name to show how many each CHILD EARNED.

$$
\begin{array}{ll}
\text { TOM } & -4 \\
\text { JANE } & -3 \\
\text { SUE } & -2 \\
\text { BILL } & -1
\end{array}
$$

| Jone |  |
| :--- | :--- |
| Bill |  |
| Tom |  |
| Slue |  |

* 2. dRaw a circle around the figure that you can trace without LIFTING YOUR PENCIL OR GOING OVER THE SAME LINE ONCE YOU START.


b
* 3. huw many square centimeters are in the shape below?


ANSWER: $\qquad$
** 4. roll a die 20 times, make a tally mark each time below the face that lands "up."

$\qquad$ HOW MANY EDGES DOES A DIE HAVE? $\qquad$ how many vertices (sharp points) does a die have? $\qquad$

*** 6. a bad storm hit tampa, it rained 1 Inch the first hour, 2 inches the second hour, and 3 inches the third hour. if the STORM KEPT GETTING WORSE, HOW MANY INCHES WOULI JU EXPECT FOR THE FOURTH HOUR? _ INCHES HOW MANY FOR THE FIFTH HOUR? $\qquad$ INCHES
$\star \star \star 7$. THREE GIRLS HAD NEW SHOES THE FIRST DAY OF SCHOOL, AND ONE OF those girls had a new belt also. draw a picture of the girls with new shoes, and the New belt. use this picture to count how many new things turned up at school that day.

PICTURE :

| ANSWER: | THERE WERE _NEW |
| :--- | :--- |
|  | THINGS AT SCHOOL |
|  | THAT DAY. |


$\star \star$ 8. MR. JONES HAD TO BUY NEW TIRES FOR BOTH OF HIS CARS, HOW MANY DID he have to buy to replace all of the tires?

ANSWER: $\qquad$ TIRES
$\qquad$

* 1. circle the figure that does not fit in the box.

* $\star$ 2. how much money does sue have to buy a doll?

ANSWER: $\qquad$ .

$\star \star \star 3$, PUT $>,<$, OR $=$ in the box to make the statement true,

$$
9+6 \square 20-5
$$

$\star \star 4$. you have $\$ 5$ to buy a present for a friend, circle the presents below that you might be able to buy with that much money,
d BICYCLE.
A SMALL TEDDY BEAR.
A TOY CAR.
A COMPUTER.
A COLORING BOOK.
A HORSE.
$\star \star$ 5. hOW MANY TRIANGLES CAN YOU FIND IN THE PICTURE?

ANSWER: $\qquad$

$\star \star \star \star$ 6. a GROUP OF PENNIES IS CALLED EVEN IF YOU AND A FRIEND COULD divide up the group equally, with no pennies left over, if A PENNY IS LEFT OVER WHEN YOU DIVIDE THE GROUP, THAT GROUP is called 0JD.
Write EVEN or OdD beside each group of pennies below.

$\star \star$ 7. the car to the right is about 8 feet long (front to back), circle the SEntence below that makes sense.

(A) the car is about 8 feet high,
(b) the car is about 6 feet high.
(c) the car is about 10 feet high.
$\qquad$
** 1. there are 9 boys and 6 girls at A PARTY, HOW MANY KIDS ARE AT THE PARTY?

HOW MANY MQRE BOYS ARE ARE THERE THAN GIRLS?


* 2. LOOK AT THE PICTURE BELOW, IT SHOWS SOME OF THE CHILDREN WHO WENT TO THE PARTY.


HOW MANY KIDS ARE IN THE PICTURE? $\qquad$
HOW MANY ARE BOYS? $\qquad$
HOW MANY ARE GIRLS? $\qquad$
ARE THERE MORE BOYS, OR MORE GIRLS? $\qquad$
HOW MANY CHILDREN ARE WEARING GL.ASSES? $\qquad$
HOW MANY LOOK HAPPY? $\qquad$
WHICH GROUP LOOKS HAPPIER, THE BOYS OR THE GIRLS?
3. DO THIS PROBLEM ON YOUR


$$
1+2+3+4+5=
$$

$t \rightarrow$ 4. LOOK AT THE SETS OF TENS AND ONES BELOW, WRITE THE NUMBER THAT EACH GROUP SHOWS.


ANSWER ${ }^{\prime}$


ANSWER ${ }^{3}$


ANSWER 5
$\star \star$ 5. DRAW A RED RING AROUND THE TOY THAT YOU CANNOT BUY WITH $\$ 5.00$. DRAW BLUE RINGS AROUND THE TOYS THAT COST LESS IHAN \$1.00.

$\qquad$
$\star \star \star$ 1. help freda the frog hop back across the pond. fill IN THE MISSING NUMBERS ON THE LILY PADS.

$\star \star \star \star 2$ SUBTRACT ACROSS,
2. SUBTRACT DOWN.

FILL IN THE BOXES WITH the missing numbers.


* 3. I AM MR. SHAPO.

$\star \star \star 4$. use the money shown on the left to buy the toys on the shelves. THEN DRAW A CIRCLE AROUND THE MONEY YOU hill get back.

$\star \star \star \star$ 5. USE THE CODE TO COMPLETE THE PATH, WRITE The numbers in each shape,

$\qquad$
ntet 1. HOW MANY WAYS ARE THERE TO PUT 5 BIRDS INTO 2 CAGES?
ANSWER: $\qquad$ WAYS

$\star * * 2$. A gROUP OF PENNIES IS CALLED EVEN IF YOU AND A FRIEND CAN DIVIDE THE GROUP EQUALLY, WITH NO PENNIES LEFT OVER. IF A PENNY IS LEFT OVER WHFN YOU DIVIDE THE GROUP, THAT GROUP IS CALLED ODD. WRITE EVEN OR ODD BESIDE EACH GROUP OF PENNIES BELOW.

* 3. Write the missing number in the square: $\quad 12-\square=5$
$\star \star \star \star 4$. Janice kept up with her new puppy's weight on the chart below. HER PUPPY WAS BORN IN JANUARY.


IF THE PUPPY KEPT GROWING JUST AS FAST DURING MAY, HOW MUCH WOULD HE WEIGH? FINISH THE BAR GRAPH FOR YOUR ANSWER.

* $\star$ 5. Mary added $\$ 5.00$ and $\$ 7.00$ ON her NEW Calculator, AND GOT THE ANSWER SHOWN TO THE RIGHT. CIRCLE THE SENTENCE beLOW that makes THE MOST SENSE.
(A) MARY'S CALCULATOR IS PROBABLY BROKEN.
(b) MARY'S CALCULATOR NEEDS A NEW battery probably.

(c) MARY'S CALCULATOR IS WORKING FINE.
$\star \star \star$ 6. SUBTRACT ACROSS AND SUETRACT DOWN. FILL IN THE BOXES WITH THE MISSING NUMBERS.


STAR PROBLEMS
I DID THIS WORK MYSELF:
GRADE 1, XXV
*太* 1. mary's cat had 6 kittens, and her dog had 5 puppies, she gave away 4 kittens and 2 puppies, how many animals did she have left at home to play with?

Answer: __ ANIMALS
$\star \star \star \star 2$. tell the robot how to find each of the things on the map. tell THE ROBOT HOW FAR TO THE RIGHT FIRST, AND THEN HOW FAR UP TO GO,


| TO GET TO THE: | GO RIGHT: | GO UP: |
| :--- | :---: | :---: |
| SQUIRREL | 2 | 4 |
| BASEBALL |  |  |
| RACCOON |  |  |
| FISH |  |  |
| TRUCK |  |  |

$\star \star$ 3. after going trick-or-treating at halloween, you had 5 orange LOLLIPOPS, 3 GRAPE LOLLIPOPS, AND 9 CHERRY LOLLIPOPS. IF YOU PUT THEM IN THE SAME SACK, AND PICKED ONE OUT WITHOUT LOOKING, What kind of lollipop would it probably be?

ANSWER: IT WOULD PROBABLY BE
$\star \star \star \star 4$. A FROG FELL IN A WELL, AND WAS SCARED. EVERY DAY THE FROG WOULD Climb up 2 feet, but at night he WOULD SLIDE BACKWARDS 1 FOOT. DRAW A DIAGRAM OF HIS TRIP ON THE WELL WALL, AND FIND OUT HOW MANY DAYS IT TOOK HIM TO GET OUT OF THE WELL.

ANSWER: IT TOOK $\qquad$ DAYS
FOR THE FROG TO GET OUT.
5. In the chart below, each THE TEAM.

STANDS FOR 2 gaited won by


* how many games did the BEARS win?
* hon many games did the red SOX win?
$\star \star$ how many more games did the TIGERS win than the PIRATES?

WORKSHEETS
FOR
GRADE 2
$\star \star \star \star$ 1. WHEN JULIO COUNTS HIS PENNIES, HE LIKES TO MAKE 2 piles that are the same height. he knows he has an EVEN number to start with, if he can make the piles the same height. if he can't, he has an ODD number of pennies.

WRITE EVEN OR ODD beside each group OF PENNIES BELOW, USING JULIO'S METHOD.

| NUMBER OF PENNIES: | EVEN OR ODD? |
| :---: | :---: |
| 14 | - |
| 15 | - |
| 16 | - |
| 17 | - |
| 22 |  |
| 25 |  |



$$
16
$$

17


* 2. A Lady's face is hidden in this picture somewhere, color HER FACE RED.

** 3. all insects have 6 legs, and all frogs have 4 legs. if max caught 2 insects and 2 frogs, how many l.EGS WOULD THERE BE ON ALL those CREATURES?


ANSWER: $\qquad$ LEGS
$\star$ 4. USE A

$$
1+2+3+4+5+6+7+8+9+10:=
$$

$\star \star \star$ 5. WHEN JANET WAS IN THE FIRST GRADE, SHE KEPT UP WITH HER WEIGHT ON THE CHART BELOW. IF SHE KEPT GROWing OVER THE SUMM-R JUSt like she did before, draw in the bars on the GRAPH BELOW FOR THE LAST THREE MONTHS.


MY FIRST GRADE $699^{\text {YEAR }}$
$\star \star \star \star$ 1. THE SPIDER CAN ONLY MOVE UP OR ACROSS TO GET TO THE FLY, ONE OF HIS PATHS IS ShOWN. HOW MANY PATHS altogether are THERE FOR THE SPIDER TO GET HIS MEAL?


ANSWER: THERE ARE $\qquad$ PATHS .
$\star \star \star$ 2. DO THESE PROBLEMS ON YOUR CALCULATOR, AND WRITE THE ANSWER ON THE LINE BESIDE THE PROBLEM:
(A) $27+54+75+403=$ $\qquad$
(B) $385-76+541=$
(c) 372

$\qquad$

$+846$

$\star \star \star \star$ 3. COLOR THE MAP TO THE left using only 4 COLORS, NO STATE CAN BE THE SAME COLOR AS One that touches it.

$\star \star$ 4. maria lost a tooth, but got 25 f from the tooth-fairy that NIGHT. THE NEXT DAY SHE BOUGHT ONE OF THESE ANIMALS, AND GOT 2 COINS BACK AS HER CHANGE. WHICH ANIMAL DID SHE BUY?

Answer: $\qquad$


* 5. JOSÉ WANTED to invite 15 friends to his eirthday party, he had the right inumber of invitations and envelopes, but he only had 8 stamps. draw a picture of the 15 envelopes, with stamps on 8 of them, in the correct corner of the envelope,

PICTURE:

* 6. look at your picture above. how many more stamps did josé NEED TO BUY? ANSWER: JOSÉ NEEDED TO BUY ___ MORE STAMPS.
* 7. count the dots:

ANSWER: _ DOTS

$\star \star$ 7. While shopping with dad, you buy a pencil sharpener for 254. PENCILS FOR 30\&, AND ERASERS OR 20६. CIRCLE The amount of tax you will have to pay for your ITEMS, ON THE CHART TO THE RIGHT.


| Sale | Tax |
| :---: | :---: |
| $.01-.10$ | .00 |
| $.11-.27$ | .01 |
| $.28-.47$ | .02 |
| $.48-.68$ | .03 |
| $.69-.89$ | .04 |
| $.90-1.09$ | .05 |
| $1.10-1.29$ | .06 |
| $1.30-1.49$ | .07 |
| $1.50-1.69$ | .08 |
| $1.70-1.89$ | .09 |

$\star \star \star$ 8. 19 is a two-digit number whose digit-sum is 10 , since $1+9=10$. how many other two-digit numbers have a digit-sum of 10 ?

ANSWER:
Hint: make a list
** 9. EACH OF YOUR Three packages of LIfe savers has 8 pieces of candy IN IT, AND COSTS 35\%, if you share YOUR CANDY EQUALLY WITH A FRIEND, HOW MANY PIECES WILL YOU GET?

ANSWER: I'LL GET _ PIECES.
** 10. draw the next shape for the pattern Shown below.

$\star \star$ 7. While shopping with dad, you buy a pencil sharpener for 254. PENCILS FOR 30\&, AND ERASERS OR 20६. CIRCLE The amount of tax you will have to pay for your ITEMS, ON THE CHART TO THE RIGHT.


| Sale | Tax |
| :---: | :---: |
| $.01-.10$ | .00 |
| $.11-.27$ | .01 |
| $.28-.47$ | .02 |
| $.48-.68$ | .03 |
| $.69-.89$ | .04 |
| $.90-1.09$ | .05 |
| $1.10-1.29$ | .06 |
| $1.30-1.49$ | .07 |
| $1.50-1.69$ | .08 |
| $1.70-1.89$ | .09 |

$\star \star \star$ 8. 19 is a two-digit number whose digit-sum is 10 , since $1+9=10$. how many other two-digit numbers have a digit-sum of 10 ?

ANSWER:
Hint: make a list
** 9. EACH OF YOUR Three packages of LIfe savers has 8 pieces of candy IN IT, AND COSTS 35\%, if you share YOUR CANDY EQUALLY WITH A FRIEND, HOW MANY PIECES WILL YOU GET?

ANSWER: I'LL GET _ PIECES.
** 10. draw the next shape for the pattern Shown below.

$\qquad$
$\star \star \star$ 1. SOME farm animals are shown TO THE RIGHT.
how many legs are on all the animals together? $\qquad$ LEGS
how Many ears are there ON ALL THE ANIMALS? $\qquad$ EARS
how many more legs are THERE, THAN EARS? $\qquad$ more légs

$\star \star$ 2. IF A SChool lunch costs you 55\%, about how much will you have to pay to eat at school for a whole week? bubblá-in the best choice.

$$
0 \$ 1 \quad 0 \$ 2 \quad 0 \$ 3 \quad 0 \$ 4
$$

$\star \star \star \star 3$. HOW MANY DIFFENENT WAYS CAN MARY GET FROM HER HOUSE TO SCHOOL? (hint: make a list, starting with "monroe st., green st.")


ANSWER: THERE ARE $\qquad$ ways for Mary to get there.
$\star * * * 4$. PLace the digits from 1 to 9 inside the circles so that the SUM WILL BE 20 along each side. use each digit once.

$\star \star \star$ 5, colint all the triangles you can find in the figure below. how MANY ARE THERE?


ANSWER:
$\star \star \star$ 6. THE CHART BELO'N SHOWS MARTIN'S AFTERNOON SCHEDULE FOR THIS WEEK. USE IT TO ANSWER THE QUESTIONS.

| stant <br> time | $12: 00$ | $1: 00$ PM | 2:00PM |
| :---: | :--- | :--- | :--- |
| MONDAY | MUSIC | MATH | LIBRARY |
| TUESDAY | P.E. | ART | HEALTH |
| MEDNESDAY | MUSIC | MATH | LIBRARY |
| THURSDAY | PIE. | MOYIE | HEALIH |
| GRIDAY | SCIEMCE | MATH | RECESS |

QUESTIONS:
on what days does martin have $P$. $\mathrm{E}_{\mathrm{a}}$ ?
how many afternoon hours will he sfend doing math?
give the day and iIme that he will get to watch
A MOVIE: FROM $\qquad$ $0^{\prime}$ CLOCK TILL $\qquad$ $0^{\prime}$ CLOCK 75
** 1.


LOOK AT THE SHAPES, PUT AN $X$ ON THE SHAPE BELOW THAT GOES IN THE blank,
g

(1)
G

t* 2. JANE HAS 49t. SHE BOUGHT A CUPCAKE AAD AN ICE-CREAM. HOW MUCH DID SHE
HAVE LEFT?


ANSWER $\qquad$
th tat 3. I AM THINKING OF TWO MMBEERS.
WHEN YOU ADD THE TWO MMBERS, THE SLM IS 28.
HEN YOU SUBTRACT THE TWO MMBERS, THE DIFFERENCE IS 6 , What are the Two numbers?

ANSWER $\qquad$
$\qquad$
th t 4. DRAW THE NEXT SHAPE IN THE PATTERN:


* 5. Look at the pigs carefuly.

(ExAPLE) 2 out of 5 pigs have straight tails.
Fill in the blank.
$\qquad$ OUT OF $\qquad$ PIGS HAVE SPOTS.
$\qquad$ OTT OF $\qquad$ PIGS HAVE CURLY TAILS.
tht 6. THIS IS A RIGHT ANGLE:


FOLD THIS PAPER SO THAT YOU MAKE A RIGHT ANGLE AT THE POINT ON THE LINE SEGMENT BELOW.
$\star * * *$ 7. PRACTICE SUBTRACTING ON THESE PROBLEMS, USING YOUR HEAD INSTEAD OF YOUR PENCIL, YOU'LL BE GIVEN A PROBLEM LIKE THESE WHEN YOU TURN IN YOUR PAPER. YOU'LL HAVE TO DO IT CORRECTLY, IN YOUR FEAD, TO EARN YOUR STARS,

$\qquad$
$\star \star \star$ 1. the taxi moves from "start" to another point by going East first, and then NORTH. it gets to the boat by going 1 block East, and then 5 blocks north. follow the taxi's path with your finger.

THL TAXI DRIVER'S SECRET CODE FOR THE bOAT IS ( 1,5 ). WRITE THE SECRET CODE FOR THESE PLACES:

$$
\begin{array}{ll}
\text { boat } & \left(\underline{1}, \mathbb{N}_{i}\right) \\
\text { church } & (\ldots, \ldots) \\
\text { pool } & (\ldots, \ldots) \\
\text { bridge } & (\ldots, \ldots)
\end{array}
$$


$\star \star \star \star$ 2. how many triangles are in the - CAT PICTURE?
$\star \star \star \star 4$. FOLLOW THE FLOWCHART. START WITH 8 AS TIIE FIRST INPUT NUMBER. NEXT use 15 as the input number.


* 5. look at the calendar. if today is January 21 , how many sundays have passed in this month?

*     * 6. :HOW MANY CENTIMETERS long is the piece of YaRN HANGING FROM THE BALL? __ CENTIMETERS


ERIC
79
$\qquad$
$\star \star$ 1. draw a circle around the bank with the most money. put A big " $X^{\prime \prime}$ ON the bank With the least money.

$\star \star 2$. HOW MUCH MONEY is there in all three banks together? $\$$ $\qquad$

* 3. mom had 25 cookies. she ate 2 cookies, frederick ate 6, andy ate 5, and dad ate 6, how many cookies were eaten?

ANSWER: $\qquad$ COOKIES
 make a bar graph as you go, to show how many of each symbol you USE IN THE PROBLEMS.

PROBLEMS

1. $27 \bigcirc 29$
2. $146 \bigcirc 150$
3. $3+9 \bigcirc 10+2$
4. $41+8 \bigcirc 50-1$
5. $79-2 \bigcirc 80-11$
6. $65+25 \bigcirc 100-12$
7. $534 \bigcirc 543$
8. $3+3+3 \bigcirc 5+3$



Number of Symbols

* 5, THIS PIECE OF PAPER IS $8^{\frac{1}{2}}$ INCHES WIDE, USE THIS INFORMATION to estimate the length of the pencil below. circle the best ESTIMATE,


ANSWER:
(A) 7 inches
(B) 10 INCHES
(c) 4 inches
$\star \star \star$ 6. use the telephone below to find the value of the words LISTED. ADD THE NUMBERS TO FIND THE VALUE.

$$
\left.\begin{array}{llllllll}
\text { EXAMPLE: } & F & L & 0 & \text { E } & R & =33 \\
& 3 & 5 & 6 & 9 & 3 & 7
\end{array}\right]
$$


$\qquad$
grade 2, VIII
** 1. how many different triangles can you find in the figure below?


ANSWER: $\qquad$
** 2. CROSS OUT ONE NUMRER in A CIRCLE AND MOVE it TO ANOTHER CIRCLE, so that the sum of the digits in each circle will BE EQUAL.

$\star \star$ 3. the AREA of a figure is the number of unit squares it would take to make the figure. what is the AREA of the figure below, using $\square$ as the unit square?


ANSWER:

$\star \star$ 4, use three 3's to make a number greater thin 200.
ANSWER: $\qquad$
5. MARK WANTED TO ADD $\$ 18$ and $\$ 75$ ON HIS CALCULATOR, WHICH OF THESE KEYS WOULD NOI APPEAR ON HIS CALCULATOR? (CIRCLE YOUR ANSWER.)
A.

B. $\square$
C. +
D.

$\star \star * 6$ 。
the AREA of something is the number of squares it takes to COVER IT UP. THE LINES AROUND THESE WORDS MAKE A SQUARE DECIMETER estimate the area of this whole SHEET OF PAPER, IN SQUARE. DECIMETERS.

ANSWER: THIS SHEET CL PAPER IS ABO'T $\qquad$ SQWRE DECIMETERS, (put either 3, i, or 9 on THE LINE AS YOUR ANSWER.)
$\star \star \star \therefore$ PII. THE RIGHT NUMBER If. The boxes to make true staitemints:

$$
46-\square=23 \quad 18+\square=30 \quad \square-14=24
$$

$\qquad$
** 1. Sandy needed 25 apples to make some apple pies. She had 12 red ripe apples and 8 green juicy apples. How many more apples did she need to buy from the market so she could make her pies?


ANSWER: $\qquad$ APPLES
$\star * * 2$. below are some stairs made of cubes. the highest step is 3 cubes high. it takes 6 cubes to make these stairs. how many cubes would it take to make stairs if the highest step WAS 5 CUBES HIGH?


ANSWER: $\qquad$ CUBES

* 3. 

| DAFLY BOOK CHART |
| :---: |
| MONDAY . . . . . . 12 |
| tuesdar . . . . . - 15 |
| WEDNESDAY. . . . . 10 |
| THURSDAY . . . . 21 |
| FRIDAY . . . . . . 11 |

LOOK AT THE CHART. ON WHAT DAY WERE THE MOST BOOKS READ?

ANSWER: $\qquad$

* 4. again, look at the chart above, on what day were 11 books read?

ANSWER: $\qquad$
*** 5. USE EACH NUMBER ONLY CNCE. CROSS OUT THE NUMBER WHEN IT IS USED.
A) Two numbers whose sum is 3
B) TWO NUMBERS WHOSE SUM IS 8
c) Two numbers whose sum is 12
d) Two numbers whose sum is 15

What number is left?
WRITE YOUR ANSWER IN THE

*6. draw a ring around the picture of an angle:

** 7. how many of these GRID BELOW?

would it take to cover the ANSWER: _ 母's

$\star \star \star$ 8. P'Jt the right digits in the buxes below so the problems will BE CORRECT.

$$
\begin{array}{rrrrr}
2 \square & \square 7 & 83 & 58 & 100 \\
+35 & -46 & +1 \square & \frac{-\square 3}{49} & +\square \square \\
\hline 57 & -\frac{\square}{21} & \frac{\square}{137}
\end{array}
$$

$*$ - 1 USING THE NUMBERS 1 - 9 only ONCE, MAKE TimE SUM ON EACH SIDE EQUAL 17 BY FILLING IN THE EMPTY CIRCLES.


* 2. WHAT IS THE WEIGHT (MASS) OF THE FLOWER POT? CIRCLE THE BEST ANSWER,

A. 5 POUNDS
B. less than 5 pounds
C. MORE THAN 5 pounds
$\star$ * 3. James gets up at 7:15 A.M. to get ready for school, he eats breakfast at 7:45 A.M. What time will he eat luna': if if he WAITS 4 hUURS AFTER EATING BREAKFAST?

ANSWER: $\qquad$
**** 4. estimate the centimeters tue bus took in all to get from "start" to "end" if the bug took the bottom path. circle the best answer.

A. about 80 CM
B. about 160 cm
C. ABOU: 220 cm
$\star \star$ 5. COLOR the CONGRUENT Shapes blue.

$\star \star \star$ 6. PUT THESE DAILY STEPS IN THE RIGHT ORDER. NUMBER THEM 1, 2, 3, AND 4.

$\star$ 7. Which of the inmer circles below is the largest, a or b? CIRCLE THE ANSWER.


A is larger
B is LaRger
they are the SAME SIZE.
$\star \star$ 8. JUDY WORKED A PROBLEM ON HER CALCULATOR. HI IS THE ANSWER SHE SAW WHEN SHE TURNED the calculator upside down, Circle the PROBLEM SHE WORKED.
A. $\quad 14$
B. $\begin{array}{r}6 \\ +8\end{array}$
c. 7
D. $+\frac{1}{4}$

** 1. There were 27 children and 18 adults at the picqic. Twelve OF THE CHILDREN WERE IN THE EGG-TOSS CONTEST. HOW MANY CHILDREN WERE NOI IN THE EGG-TOSS CONTEST?

ANSWER: $\qquad$ CHILDREN
** 2 .


Angela bought a ring, a pencil and a toy duck. The total TAX ON THESE :TEMS IS 8f. HOW MUCH, INCLUDING TAX, DID SHE SPEND?

ANSWER:

* 3. Circle the word that makes this statement true. A large bottle of soda is measured in $\qquad$ .

CELSIUS METERS LITERS GRAMS
$\star \star$ 4. IF YOU TOOK 4 APPLES FROM A BASKET WITH 44 APPLES IN IT, HOW MANY APPLES WOLILD YOU HAVE?

ANSWER: $\qquad$ APPLES

* 5. Circle the correct sign to make this number sentence true,

$$
16+12 \quad ? \quad 23+4
$$

ANSWER: $>=<$
$\star \star$ 6. The movie begins at 2:00 pam. It runs for $2 \frac{1}{2}$ hours. What time will the movie be over?

ANSWER: $\qquad$ P. M.
$\star \star \star \star 7$
SCORE ON TURN 1

| MIME | POINTS |
| :--- | :---: |
| LISA | 2 |
| JOHN | 7 |
| FRAN | 10 |
| MICKY | 5 |
| SUKI | 7 |


a) Who had the highest score on the first turn?
B) John scored how many more points than lisa? $\qquad$
c) Suki had a total of 12 points after her second turn. How many points did she score on her second turn?

ANSWER: $\qquad$
** 8. Find the answer to this problem by using a calculator. 11004-3269

TURN THE CALCULATOR UPSIDE DOWN. What word does it spell?

STAR PROBLEMS
grade 2, XII

I DID THIS WORK MYSELF: $\qquad$
$\star \star \star \star$ 1. FILL-IN THE CHART TO THE RIGHT TO SHOW THE DIFFERENT ways to have 15t, one way-WITH 15 PEMNIES--hAS BEEN DONE FOR YOU ALREADY.

| remirs | micreas |  |
| :--- | :--- | :--- |
| 15 | 0 | 0 |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |


| Same store |  |
| :---: | :---: |
| Pexil | \$.10 |
| Motesook | \$1.70 |
| Enser | \$. 5 |
| Pan | \$.30 |
| Traer | \$ . $\quad 3$ |

$\star \star$ 2. jane has $\$ 2$ that she can SPEND AT THE SCHOOL STORE. Which cf these items can SHE BUY? CIRCLE YOUR ANSWER.
A. 1 notebook and tablet
B. 1 NOTEBOOK AND PEN
C. 3 TABLETS
D. 10 pencils and 1 notebook

* 3. measure the lines shown, and write down the length TO THE CLOSEST WHOLE number of centimeters.

$\star *$ 4. FIND The missing numbers, by adding across and down.


5. WRITE THE STANDARD NUMERAL FOR THESE EXPANDED NUMERALS:

$$
\text { A. } 80+4+300=
$$

B. $4+600+20=$ $\qquad$
c. $100+5+90=$ $\qquad$

* 6. A RIGHT aNGLE LOOKS LIKE This:
 an easy way to find a right angle is to see if the corner of a piece of paper just fits into it. Test the angles below this hay, and circle any that are righi angles.

** 7. the perimeier of a shape is the DISTANCE ALL THE WAY AROUND IT. USE A RULER, AND MEASURE THE PERIMETER OF THIS TRIANGLE, IN CENTIMETERS.

ANSWER: THE PERIMETER IS $\qquad$ CM.
$\star \star \star *$ 8: maria dropped a thumb tack 100 times. her results are shown in the chart. what is the rest judgement she can make about dROPPING A THUMB TACK? (bubbLe-IN YOUR CHOICE.)

O IT IS MORE LIkELY tO LAND UP Than down.
O IT IS MORE LIKELY TO LAND DOWN THAN UP.
O IT IS JUST AS LIkELY TO LAND DOWN AS UP.

## up (b) In mi mu man mull <br> 

** 1. every letter of the alphabet has a money value:

| $A=\$ 1$ | $E=\$ 1$ | $\mathrm{I}=\$ 1$ | $M=\$ 1$ | $\mathrm{C}=\$ 1$ | $\mathrm{U}=\$ 1$ | $\mathrm{Y}=\$ 1$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{~B}=\$ 2$ | $\mathrm{~F}=\$ 2$ | $\mathrm{~J}=\$ 2$ | $\mathrm{H}=\$ 2$ | $\mathrm{R}=\$ 2$ | $\mathrm{~V}=\$ 2$ | $\mathrm{Z}=\$ 2$ |
| $\mathrm{C}=\$ 1$ | $\mathrm{G}=\$ 1$ | $\mathrm{~K}=\$ 1$ | $\mathrm{O}=\$ 1$ | $\mathrm{~S}=\$ 1$ | $\mathrm{~N}=\$ 1$ |  |
| $\mathrm{D}=\$ 2$ | $\mathrm{H}=\$ 2$ | $\mathrm{~L}=\$ 2$ | $\mathrm{P}=\$ 2$ | $\mathrm{~T}=\$ 2$ | $\mathrm{X}=\$ 2$ |  |

What is the money value of your first name? \$ $\qquad$

* 2. "bobby" has the value of \$8. is your first name worth less than "bOBBY," more than "bobby," or the same as "bcbbby?"

ANSWER: MY NAME IS WORTH $\qquad$ .
$\star \star \star$ 3. the letters of the alphabet with a $\$ 1$ value are called "odd." the letters with a $\$ 2$ value are called "even." use the chart ABOVE TO ANSWER THESE QUESTIONS.


* 4. draw a line in the cookie to THE RIGHT, TO SH:OW A FAIR WAY TO SHARE IT WITH ONE OF YOUR FRIENDS.

* 5. dRaw lines in the cookie to the RIGHT, TO SHOW A FAIR WAY TI SHARE IT WITH THO OF YOUR FRIENDS.
* 6. use a calculator to find the answer to the flowchart problem, THEN WRITE YOUR ANSWER.


ANSWER: $\qquad$
*** 7. if Christmas day (december 25th) came on eriday one year, how many sumdays had already passed that month?

93
$\qquad$ grade 2, XIV

*     * 1. if you spin the spinner for this game, what is the chance YOU WILL LAND ON YELLOW? WRITE THE ANSWER USING A FRACTION.


ANSWER:

$\star$ * 2. the point $(3,2)$ has been MARKED FOR YOU. TO FIND $(3,2)$, you start at the BOTTOM LEFT CORNER, GO OVER 3, and up 2, and make a dot THERE.
make dots on these points:
$(3,2)$
$(3,7)$
$(5,7)$


$$
(5,5)
$$

$(3,5)$

* 3. CONNECT the dots foir the problem above, in order, and you'll make a letter if the alphabet. what letter?

ANSWER: $\qquad$

* 4. WRITE the temperature shown on each thermometer, put your answer on the line ber je the the mometer.

$\star \star \star$ 5. If SOMEONE GIVES YOU 6 SMALL SQuares, THERE WOULD BE ONLY TWO WAYS TO MAKE A RECTANGLE. THESE TWO WAYS are shown to the right.


how many rectangles could you make if they gave you 10 small sQuares? how many with 5 small squares? how many with 12 small SQuARES? DRAW THE CORRECT RECTANGLES FOR EACH BOX BELOW.


FOR 12 SQUARES:
** 6. draw a line to show about how much time goes with each event. one OF THEM IS STARTED FOR YOU ALREADY.

** 7. draw the line that is missing in the fourth triangle,



2ND


3RD


4тн


5тн


6TH
$\qquad$
$\star \star$ 1. bill found 7 smakes amd 6 frogs on saturday. that night 3 of the snaíes, and? of the frogs, got out of the cage and got away into tiae woods, hoiw many animals did.bill have leff?


ANSWER: $\qquad$ ANIMALS
$\star \star \star \star$ 2. HELP FREIDA THE FROG HOP BACK ACROSS THE POND. FILL IN THE MISSING NUMBER ON THE FIRST LILY PAD,

$\star$ 3. HOW MUCH MONEY?

ANSWER: $\qquad$

$\star$ 4. WRITE the fraction that shows how much of each circle below is SHADED IN, PUT THE FRACTION IN THE BCX beside the circle.


** 5, USE the pictures in problem 4 to decide which of these FRACTIONS IS THE LARGEST AMOUNT. CIRCLE THE CORRECT ANSWER.
$\frac{1}{4}$ IS THE LARGEST FRACTION,
$\frac{1}{3}$ IS THE LARGEST FRACTION,
$\frac{1}{2}$ IS THE LARGEST FRACTION,

* 6. count the jellybeans in the jar. is the total number of JELLYBEANS AN ODD NUMBER, OR AN EVEN NUMBER?


ANSWER: $\qquad$ (ODD OR EVEN)
7. how many minutes in 2 hours?

ANSWER: $\qquad$ MINUTES
$\star \star \star$ 8. the jones kids got a dime each day they made up their beds, one week marsha earned 40 $\xi$, danny earned 50 $\xi$, molly earned 40 $k$, and bRUCE EARNED 20', MAKE A PICTOGRAPH TO SHOW HOW MUCH MONEY EACH kid earned, use a circle to show "one dime."

$\qquad$
$\star \star \star$ 1. beth has $45 \xi$ IN dimes and nickels. She has the same number OF dimes as she has nickels. how many of each does she have?

ANSWER: SHE HAS _ DIMES AND _ NICKELS.
** 2. tamika has $1 \frac{1}{2}$ cookies, sarah has $2 \frac{1}{2}$ cookies. billy has 3 COOKIES. Ir THEY PUT THEIR COOKIES TOGETHER, HOW MANY COOKIES WOULD THERE BE THEN?

ANSWER: THERE WOULD BE $\qquad$ COOKIES.

*     * 3. eight children compared the number of brothers and sisters each has at home.

| RICKY HAS 3 | TERRY HAS 2 |
| :--- | :--- |
| SHAWN HAS 1 | JUAN HAS 3 |
| CINDY HAS 3 | KEN HAS 5 |
| BRIAN HAS 2 | aNGIE HAS 0 |

(A) WHICH NUMBER OF brothers and sisters occurred most often?

ANSWER: $\qquad$
(b) ALTOGETHER, HOW MANY CHILDREN ARE in ANGIE'S FAMILY?

ANSWER: $\qquad$
$\star 4$.

$\star \star \star$ 5. put the correct numbers in the boxés below to make true statements.
$20+\square=35$
$46-\square=21$
$\square-20=50$
$\star \star \star$ 6. READ THE FOiLOWING LIST OF NUMBERS. CHOOSE ONLY THE EVEN NUMBERS AND ADE THEM TOGETHER, WHAT IS THE SUM?

FOURTEEN
THIRTY-SEVEN
TWENTY-NINE
EIGHTY-EIGHT

ELEVEN
ONE HUNDRED
FORTY-THREE
SIXTEEN

ANSWER: THE SUM IS $\qquad$ .
$\star \star \star \star$ 7. Sam became a whiz at doing addition problems in his head, without USING PAPER-AND-PENCIL. HE WOULD ADD THE LARGER PART OF THE NUMBERS FIRST, AND THEN ADD-ON THE SMALLER NUMBERS TOO, STUDY HOW HE would do a problem like " $76+23$ " by reading the thought cloud SEVERAL TIMES.

practice sam's method on these problems and on some more that you MAKE UP YOURSELF, CHECK TO SEE IF YOU ARE RIGHT ON A CALCULATOR. WHEN YOU TURN IN YOUR PAPER, YOU WILL HAVE A PROBLEM LIKE THIS TO do in your head.
(A) $45+32$
(D) $82+13$
(G) $31+24+13$
(B) $37+61$
(E) $26+42$
(H) $34+26$
(c) $50+43$
(F) $63+27$
(I) $72+18$
$\qquad$
Grade 2, XViI

* 1. following the pattern, Write the missing letters in the EMPTY BOXES BELOW. BE SURE TO WRITE THEM IN THE POSITION THAT FOLLOWS THE PATTERN.

| $A$ | $J$ | $D$ | $R$ |  | 0 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $D$ | $\ddots$ | $O$ |  |  |  | $I$ |
| $\forall$ | $r$ |  | $\mathbf{y}$ | $\pm$ |  |  |

$\star \star \star 2$ 2. SALLY HAD A BIRTHDAY PARTY AND INVITED 6 OTHER GIRLS. SHE HAD A BALLOON AND A HAT FOR EACH GIRL. FIVE BALLOONS WERE IN A PACKAGE, AND TWO HATS WERE IN A PACKAGE, WHEN SHE BOUGHT THEM. HOW MANY PACKAGES OF BALLOONS, AND HOW MANY PACKAGES OF HATS, DID SHE HAVE TO BUY?

ANSWER: $\qquad$ PACKAGES OF BALLOONS AND _ PACKAGES OF HATS
$\star$ 3. THESE COINS


ARE ABOUT AS MUCH AS WHICH OF
these coins? draw an $X$ on the correct coin.

$\star$ 4. USE THE PICTURES OF THE PIES TO hELP YOU, WHICH IS THE MOST PIE; $\frac{1}{2}$ OF THE PIE, $\frac{1}{3}$ OF THE PIE, OR $\frac{1}{4}$ OF THE PIE?

ANSWER: $\square$ OF THE PIE

$\star \star \star \star 5$, HOW MANY DIFFERENT, 2-DIGIT NUMERALS CAN YOU MAKE FROM THE DIGITS TO THE RIGHT? DO NOT COUNT 22, 66, 77, AND 88.


ANSWER: THERE ARE $\qquad$ 2-digit numerals that CAN BE MADE FROM THOSE ABOVE.

* 6. mary left her house at 1:00 p.m. to walk to the movie. it TOOK HER $\frac{1}{2}$ HOUR TO GET THERE, WHAT TIME DID SHE GET TO THE MOVIE?

ANSWER: AT $\qquad$ P.M.
$\star \star \star$ 7. check bob's math paper. use $\boldsymbol{\gamma}^{\prime}$ 's and $X$ 's.


NOW COLOR $\square$ 's to SHOW HOW MANY BOB GOT RIGHT:
number right

$\star$ * 8. 1 PINT


FILLS


SHADE IN THE CUPS YOU CAN FILL WITH $\frac{1}{2}$ PINT


ANSWER:

** 1. juhan made a tic-tac-toe. when he added the numbers under his x's, he got a sum of 100. put juhan's $x$ 's on the game.


* 2. I had 15 pigs in one pen and 10 pigs in another. I sold 4 pigs from one pen and 6 from the other. how many pigs are LEFT?


ANSWER: $\qquad$ PIGS
$\star \star$ 3. how many small cubes does it take to make this solid?

ANSWER: $\qquad$ CUBES


* 4. FIND EACH LETTER BY GOING EASI AND THEN NORTH THE RIGHT NUMBER OF STEPS. THE FIRST 2 LETTERS HAVE BEEN DONE FOR YOU, AS A HINT.

EIRSI HORD:


SECOND HORD:
GO EAST: 30
IHIRD HORD

GO NORTH: 02
LETTER: $\square \square$
go east: 535
GO NORTH: 651
LETTER: $\square \square \square$
$\star \star \star$ 5. USE A CaLCULATOR TO FIND THREE CONSECUTIVE NUMBERS THAT ADD UP To 45. (HINT: CONSECUTIVE NUMBERS ARE LIKE 5, 6, AND 7.)

ANSWER: THE THREE NUMBERS ARE $\qquad$ AND $\qquad$ .
$\star \star \star$ 6. EACH OF THE 25 STUDENTS IN MS. BROWN'S CLASS HAS A DIFFERENT FIRST NAME. how many students were absent at least 1 day dURING THIS WEEK?

| DAYS Of THEMEEK | STInEMTS ARSEMT |
| :---: | :---: |
| mrumay | SUEABHL |
| Trissmay | BHL |
| Menwesmay | AM. Mren mapy |
| THMRSDAY |  |
| ERIPAY | AHL TOMY MMPY LIEA |

ANSWER: $\square$

* 7. hOW MUCH MONEY WOULD YOU EXPECT TO PAY FOR A PACK OF GUM at a store near your house? Circle the best answer.
$\qquad$
* 1. Find the number that was torn from this paper, write it in THE CORRECT PLACE.

$$
\begin{array}{r}
\sqrt{3} \\
+15 \\
\hline 58 \\
\hline
\end{array}
$$

$\star \star$ 2. sam covered the baby's FOOTPRINT WITH HIS
THUMB, HOW MANY OF SAM'S
THUMB PRINTS WOULD IT
TAKE TO COVER THIS FOOT SHAPE?

SAM'S THUMB PRINT:


ANSWER: IT WOULD TAKE ABOUT $\qquad$ THUMB PRINTS.

* 3. ed's ticket for the circus said "seat 344." color in the place WHERE ED WILL SIT.

* 4. PUT IN THE MISSING NUMBER.
पincaja ?
* 5, draw the missing shape,



## ? <br> 

6. here is a fictograph that's not finished,

** 7, put the numbers $4,0,3,1$, 2, and 5 in the circles below so each line has a sum of 10 .


* 8. write the number you WILL SEE ON The CALCULATOR DISPLAY.

$\star \star \star$ 1. how many square centimeters does it take to make the dark figure?

** 2. a rabbit took 6 hops to get from tree a to tree b, 5 hops to GET FROM TREE B TO TREE $C$, AND 3 hops to get from tree $C$ back to tree $A$. draw a picture of all the hops the rabbit made, and then use your drawing to find cid how many hops in all the RABBIT MADE,


ANSWER: $\qquad$ HOPS
$\star \star \star \star$ 3. USE A CALCULATOR TO DO EACH PROBLEM BELOW,

$$
\begin{aligned}
33+29+64 & = \\
105+41+89 & = \\
93-57+16 & = \\
213-94-96 & =
\end{aligned}
$$



106
** 4. Which one of these shapes can be drawn without lifting your PENCIL OR GOING OVER THE SAME LINE TWICE? CIRCLE IT.

$\star \star$ 5. FILL IN THE BAR GRAPH TO SHOW hOW MANY OF EACH PET WAS OWNED BY THIS SECOND GRADE CLASS.

DOGS - 6
CATS - 6
FISH - 3
TURTLES - 2
BIRDS - 1

$\star \star \star$ 6. throw a die 25 times. each time you throw it make a tally mark under the picture of the side that lands "up".


WHICH SIDE LANDED UP MOST OFTEN? CIRCLE IT ABOVE,
$\qquad$

* 1. What could you buy with the money shown? Circle your answer.

$\star \star$ 2. about how many pies are shown? CIRCLE the best answer.

* 3. fill in each blank space by moving down the tape, then compare YOUR FINAL ANSWERS BY PUTTING $>,<$, OR = IN THE bOX BETWEEN THEM.

$\star \star \star$ 4. fill in the numbers that the squares are covering up,
$36+\square=79$

$\square+23=68$
* 5, COLOR EACH PICTURE THAT IS DIVIDED EXACTLY IN HALF.

** 6. SUSIE is having a birthday party in two weeks. she will be 7 years old. how many days is it until her party?

ANSWER: $\qquad$ DAYS
$\star \star$ 7. USE a calculator to find the total cost of these dresses.


ANSWER: $\qquad$
$\star \star \star$ 8. I AM thinking of two numbers that add to twenty-one. ONE NUMBER IS 3 MORE THAN THE OTHER. WHAT ARE THE NUMBERS?

ANSWER: $\qquad$ AND $\qquad$
** 1. there are 8 mothers, 7 fathers, 3 boy SCOUTS AND 5 girl scouts on the bus.
how many females are on the bus? how many males are on the bus? $\qquad$ how many people are on the bus? $\qquad$

$\star \star \star t$ 2. DAVID IS GOING TO SUMMER CAMP, HE HAS 3 NEW PAIRS OF SHORTS, AND 3 NEW SHIRTS TO TAKE WITH HIM, LIST ALL THE DIFFERENT OUTFITS THAT HE CAN WEAR AT CAMP, (THE LIST lb STARTED FOR YOU.)


$\star \star$ 3. WHICH COIN IS CLOSEST TO THE COST OF THESE TOYS?



* 4. howard watches tiv. from 11:15 A.M. till 12:15 P.M. he eats lunch from 12:15 P.M. till 12:30 P.M., and then watches tiv. again until 1:30 P.M. how many hours does howard watch tiv.?


ANSWER: $\qquad$ HOURS
$\qquad$
**1. THIS IS A MAGIC THAT THE SUM OF THREE NUMBERS IN EACH ROW IS 18: USE EACH NUMBER ONLY ONCE.

$\not \approx * 2$. circle the thermometer that shows a temperature of $62^{\circ}$.

$\star \star \star$ 3. USE THE CODE TO HELP FIND THE STARTING NUMBERS IN EACH ROW, FILL THE $\square$ WITH THE NUMBER.

$\star$ 4. Find the triangles below and circle them.

¥ㅜㅜ 5. BUY WHAT IS IN EACH PICTURE WITH 75\%, SHOW HOW MUCH CHANGE YOU WILL GET BACK USING THE FEWEST NUMBER OF COINS.


STAR PROBLEMS
1 HAVE DONE THIS WORK MYSELF:
GRADE 2, XXIV
$\star \star$ 1. MRS. brown had nine eggs. she bought a dozen more and used a half-dozen of them. how many does she have left?

ANSWER: SHE HAS $\qquad$ EGGS LEFT.

*2. bob's dad travels to different towns every day. he leaves at 6:00 A.M. EACH MORNING AND RETURNS AT 7:00 P.M. EACH evening. he traveled 70 miles on monday morning and went 25 miles monday afternoon. how far did he go on monday?

ANSWER: $\qquad$ MILES

$\star \star \star$ 3. MAKE A BAR GRAPH TO SHOW

** 4. Jimmy earns $\$ 1.75$ Each week for HIS ALLOWANCE. HOW MUCH WILL HE have at the end of three weeks?

ANSWER: $\qquad$

$\star \star$ 5. how many weeks must jimay save HIS ALLOWANCE TO BUY A $\$ 10$ TRUCK? ANSWER: $\qquad$ WEEKS
$\star \star$ 6. USING THE MAGICIAN'S WAND AS YOUR UNIT OF MEASURE, ABOUT HOW LONG ARE THE TAILS OF THE STARS?


$\star \star \star$ 1. A SNAIL FELL INTO A 7 FOOT HOLE, EACH hour thf snail crawls 2 feet up the side, BUT THEN STOPS FRR A MOMENT TO REST AND falls back 1 foot. Then he starts CLIMBING AGAIN. HOW MANY HOURS DOES IT take for the snail to get out of the HOLE?

ANSWER: $\qquad$ HOURS

$\star$ 2. draw a line to match each item with how much it might cost AT YOUR LOCAL STORE, THE FIRST ONE IS DONE FOR YOU,

$\star \star \star$ 3. find the area of the dotted figure below, (the area is the number of square centimeters it would take to make the figure,)


ANSWER: THE AREA IS
__ SQ. CENTIMETERS

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$\star \star \star \star 4$ ．WRite the missing digits that have been torn off of the PAPERS BELOW．

＊5．josie did a math problem on her calculator．she was trying TO FIND OUT HOW MANY BIRTHDAYS HER BEST FRIEND HAD CELEBRATED， IF her best friend was in the SECOND GRADE，COULD THE CALCULATOR ANSWER SHOWN TO THE RIGHT BE CORRECT？


ANSWER： $\qquad$ （YES OR NO）
$\star \star \star$ 6，it took marie 10 minutes to saw a board into 2 pieces，if She works just as fast，how long will it take her to saw ANOTHER BOARD INTO 3 PIECES？


ANSWER： $\qquad$ MINUTES
$\star *$ 7．If you counted the kids ahead of you in the lunch line and got 12，and counted the kids behind you and got 8，how many kids Were in the lunch line？

ANSWER： $\qquad$

## WORKSHEETS

FOR
GRADE 3
$\qquad$

1. A class of 22 students goes outside to play softball. If there are 9 members on a tean, and 4 children decide not to play, how many teams can the class forl?

Answer: $\qquad$ teans
tht 2. $\Delta$ frog fell into a 10 foot well, and started to climb out. Each hour, the frog climbed 3 feet up and then stopped to rest for a moment. But the frog slipped back 1 foot each time it rested.

How long did it take for the frog to climb out of the well?

$\star$ 3. Tony earns $\$ 1.50$ each week for helping his father cut the grass and wash the car. If he saves all his money, how much will he have at the end of 6 weeks?

## Answer:

tht 4. Cut a strip of paper this long.


Cut another strip of paper this long. -
Use the strips to measure.

| KIRASURE | About how many <br> hhort stripe | About how many <br> long strips |
| :--- | :--- | :--- |
| Length of this pare |  |  |
| Width of this page |  |  |
| Length of a new pencil |  |  |

**
5. Dse the infornation below to construct a bar graph that shows how many hamburgers, drinks, and orders of french fries a restaurant served altogether last weekend.

|  | Hamburgers | French Fries | Drinks |
| :--- | :---: | :---: | :---: |
| Saturday | 450 | 425 | 525 |
| Sunday | 275 | 325 | 450 |


*
6. What is the mass of the hot dog and bun? Circle your answer.
(a) 50 grams
(b) less than $\mathbf{5 0}$ grams?
(c) more than 50 grams?

$t \rightarrow t$ 7. You have just won $\$ 4000$ on a quiz show. Without using pencil and paper, practice finding the answers. How much change would you get if you bought each of these items with a $\$ 1000$ bill?
a. A bicycle for $\mathbf{\$ 1 7 5 .}$
b. A nes computer for $\$ 450$.
c. A new stereo for $\mathbf{\$ 8 2 5}$.
d. Gifts for Mom and Dad for \$497.

Change $\qquad$
Change $\qquad$
Change $\qquad$
Change $\qquad$
When you turn in your paper, you will be given problem like this to do completely in your head. So practice some more like this so you'11 get the three stars then.

Answer:

Star Problems
Grade 3, II
$\star \star \star 1$.


I have neither given nor received help on these problems: $\qquad$
(a) Kim counted 18 legs. She saw 2 cows and $\qquad$ chickens.
(b) Eric counted 24 legs. He saw $\qquad$ cows and 6 chickens.
(c) Sheila saw 5 cows and 3 chickens. How many legs would she count? $\qquad$
$\$ \star 2$. Each calculator shows the six keys that were pushed to give the answer showing on the display. Figure out what the problem was in each case, and write the equation (like $2+2=4$ ) on the line below each calculator.

3. It takes 2 clothespins to hang up 1 beach towel. If you have more than 1 towel to hang up, you can put the edges together as show in the sketch.


If you have 14 clothespins, how many towels can you hang?

Answer: $\qquad$ towels
$\star \star \star \mid$ 4. Use the clues to write these prices on the tags: $30 \xi, 15 \xi, 10 \xi, 5 \xi$, and $12 \xi$

Clues: $\quad$| A brush and a car |
| :--- |
| cost 25c. |
| A brush and an apple |
| cost 15e. |
| An apple and a pencil |
| cost 17e. |
| A ball and a brush |
| cost $40 c$. |


$\star$ 5. One of the shapes below can be traced without lifting your pencil or tracing over the same line twice. But you have to start in the right place to do it. Find the shape that car be traced like this, and circle the point where you start, with a blue crayon.


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STAR PROBLEMS
Grade 3, III

I have neither given nor received help on these problems: $\qquad$
$\star$ 1. The train brought 6 zebras, 8 elephants, and 4 tigers to the zoo. But the zoo only has enough cages for 15 animals. How many animals will not have a cage?

Answer: $\qquad$ animals

$\star t \star$ 2. Howard, Jeffrey, Sandy and David are two sets of twins. David is a month younger than Howard. Sandy is a month older than Jeffrey. Which pair fis the younger set of twins?

Answer: $\qquad$ and $\qquad$
$\star \star$ 3. Mike wakes up at 6:15 A.M. every morning, and he leaves for school at 7:15 A.M. If he takes 5 minutes to brush his teeth, 15 minutes to take a bath, and 15 minutes to get dressed, how long does he have to eat breakfast?

Answer: $\qquad$
$t \rightarrow t$ 4. Solve the following magic squares. For each one, the sum across each row, and down each column, must be the same as the sum along the diagonal.

5. Write the following in "standard form," without doing any of the addition shown.

$$
20+900+7+60,000+4,000=
$$

$\qquad$
6.

$$
\begin{array}{r}
34500228394817238475 \\
-2550028394817238466 \\
\hline
\end{array}
$$

$t \rightarrow t \rightarrow 7$. Astronaughts landed on the moon and found that they could take much longer steps than they could on earth. Look at the following table and complete the sentences below it.

| Astronaut | Feet In Bach Step |
| :--- | :---: |
| Ions | 10 |
| Friendly | 17 |
| Carter | 15 |
| James | 13 |



Long can cover $\qquad$ feet in 6 steps. Friendly can cover feet in 2 steps. Carter can cover feet in 3 steps. James can cover $\qquad$ feet in 5 steps.

$\star *$ 8. The perimeter of a figure is the distance distance around the outside edge. What is the perimeter of this polygon, in centimeters?


Answer: $\qquad$ centimeters
9. Put the letter beside each step below, into the right box in this flowchart:

## STEPS

(A) Put on your shoes.
(B) Go to school.
(C) Viake up.
(D) Put on your socks.
(E) Get on the school bus.

$\star$ * $\boldsymbol{*}$. You will be asked to do a problem like the one below, in your head, when you turn in your paper. You should practice estimating the answer to this problem, and make up some other problems to practice on by putting different numbers into this problem.


Answer later on:

STAR PROBLEMS
Grade 3, IV

I have neither given nor received help on these problems: $\qquad$
$t$ t 1 . Ericka bought 15 orange popsickles and 13 cherry popsickles. On the way home, 4 of them melted and she dropped another one and got it dirty. How many were left?

Answer: $\qquad$
$\star * 2$. Jim thinks of a number. After adding 5 and then subtracting 6, and then adding 2, he got 20. What number had Jim thought of? Write it in the thought cloud next to his head.

3. How much money altogether?

Answer: $\qquad$

4. Write the fraction for each of the shaded figures below, Put the fraction on the blank space.

5. Is $\frac{1}{4}$ greater than, less than, or equal to $\frac{2}{8}$ ?

Answer: $\qquad$
ttt 6. The odd numbers are $\{1,3,5,7,9,11,13$, and so on $\ldots\}$
The even numbers are $\{2,4,6,8,10,12,14$, and so on ... $\}$
Write "odd" or "even" beside each number below, to show which set it belongs to.
15: $\qquad$ 16: $\qquad$ 23: $\qquad$ $34:$ $\qquad$ 100: $\qquad$

* 7. How many more people are going to Los Angeles than to Chicago?
$\qquad$
PEOPLE FLYING TO FOUR CITIES Each $\mathcal{f}$ stands for 50 people

| Now <br> York |  |
| :---: | :---: |
| Chicago |  |
| Fort <br> Worth |  |
| Los Angeles |  |

the 8. How many seconds are in $2 \frac{1}{2}$ minutes? Answer: $\qquad$ seconds
t 9. The perimeter of the square to the right is 4 inches--this means it is 4 inches around the outside edge.
Since you know the distance around the square, you can make a good guess about the distance around the circle. Circle the best estimate of the distance around
 the circle.
(A) 2 inches
(B) 3 inches
(C) 4 inches
(D) 5 inches
10.

$$
\begin{array}{r}
34206731745 \\
+\quad 5794259366 \\
\hline
\end{array}
$$

11. How many rectangles are there in this figure? Be careful--there's more than 3! Answer: ___rectangles


Star Problems
I have neither given nor received
Grade 3, $V$ $\qquad$
$\star$ 1. Look at the shapes below. How many dots will there be in the next such shape?

Answer: $\qquad$ dots

?
$\star$ * 2. David earned the money below selling newspapers. If he bought a flashlight and battery, how much change should he receive for his money (don't forget the tax, which would be-6f extra)?


Answer: $\qquad$

3. Fill-in the correct number:

4. Fold this piece of paper so that you bisect (cut exactly in half) the line segment below. You can do this if you carefully place one endpoint on top of the other endpoint, before you make the crease.

5. John heard on the weather report that the temperature expected for the weekend was:

$$
\begin{aligned}
& 10^{\circ} \text { C for Friday } \\
& 0^{\circ} \mathrm{C} \text { for Saturday } \\
& 10^{\circ} \mathrm{C} \text { below zero Sunday }
\end{aligned}
$$

Draw in the correct temperature on the thermometers to the right.


Friday


Saturday


Sunday

6. For your birthday, your Mom says she'11 buy you one of the shirts to the left. If she buys one at random (without picking a special one out), what fraction tells your chances of getting a shirt with stripes?
$\star$ * Answer: $\square$
What fraction tells your chance of not getting a striped shirt?

Answer : $\square$

* $\boldsymbol{*} \boldsymbol{*} \boldsymbol{*}$

7. Sally became a master at doing subtraction problems in her head, without ever "borrowing." She would always do a problem that was slightly different from the one given, but which gave the same answer. Study the pictures below carefully, and then practice this method on the problems below.


Practice problems:

| 345 | 526 | 863 | 762 | 682 | 444 | 600 | 800 | 830 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| -98 | $\underline{-97}$ | $\underline{-290}$ | $\underline{-94}$ | $\underline{-190}$ | $\underline{-90}$ | $\underline{-75}$ | $\underline{-150}$ | $\underline{-280}$ |

To earn your stars, you'11 have a problem like these when you turn in your paper. To earn your stars, you'11 have to find a "slightly different" problem, one that's easy to solve in your head.
Answer: Given problem Different problem

I have neither given nor received
Grade 3, VI help on these problems: $\qquad$

1. Guess how many pennies in a pile it will take to be the same height as one penny on edge. Write your guess below, and then try it with real pennies and see if you were correct.


Guess: $\qquad$ Real answer: $\qquad$
2. Your recipe for making some lemonade calls for $\frac{1}{2}$ cup of sugar. You only have $\frac{1}{4}$ cup of sugar. If you go ahead and make the lemonade, will it be as sweet as it should be?

Answer : $\qquad$ (yes or no)
3. Write $40,000+20+3,000+300,000$ in standard form:
4. Write acute, obtuse, or right inside each of the angles below. Use the method shown to the right, to test any that are hard to judge.


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*5. A man's face is hidden in the picture to the left. Circle his mouth to prove you have found him.
tht 6. Rim thought of 1 number. When she added 3 to the number, and then doubled the new number, she had 14. What number did she think of first? Write it in the first thought cloud.

t $\boldsymbol{*}$. You were standing in the lunch line and noticed that there were 12 students ahead of you, and 8 students behind you. How many students were in the lunch line?

Answer: $\square$

| $\sqrt{6}$ |
| ---: |
| +718 |
| +718 |
| 5187 |

* 8. Find the missing digits that were torn off the problem to the left. Write them in the correct place.

9. What fraction of a week would be called "school days?"

Answer:
10. What fraction of a week would be called "weekend days?"

Answer: $\square$
11. Which is the largest fraction, $\frac{5}{7}$ or $\frac{2}{7}$ ?

Answer: $\square$

* 12. Use your metric ruler to find the perimeter of the polygon below:


Answer: The perimeter is
$\qquad$ centimeters.

STAR PROBLEMS
Grade 3, VII

I have neither given nor received help on these problems: $\qquad$
$\star$ 1. When Louise woke up Saturday morning, the clock looked like:

was how the clock looked when she went to bed that night.

How long was she awake on that Saturday?
2. Shannon, Maurice, and Kofi are all the same height, but Shannon weighs 10 pounds more than Maurice. Maurice weighs 68 pounds and Kofi weighs 12 pounds more than Maurice. What is the difference between Maurice's and Kofi's weights?

Answer: $\qquad$ pounds

* $*$ 3. Complete the flow-chart below. Beginning with the first box under "Start," place the letter of the alphabet that shows the correct step in writing and mailing a letter to a friend.


| A | COSE TVE MAILBOX |
| :---: | :---: |
| D | $\begin{aligned} & \text { Muk to } \\ & \text { miligox } \end{aligned}$ |
|  | SER TE ENELOPE |


| $\int_{\text {MaIt ADDRESS }}^{\text {WN ENELOPE }}$ |
| :---: |
| $E_{\substack{\text { STOP AT } \\ \text { MAILSOX }}}$ |
|  |
| 131 |

$\left.\begin{array}{|l|l|}\hline C & \text { PUT LITER In } \\ \text { STMPED EMELDPE }\end{array}\right]$
4. Tamika's family went to her Grandma's house for Thanksgiving. Their car's instrument panel looked like this when they started:


It looked like this when they arrived:


If their gas gauge was working correctly, could they return home without adding more gas?

Answer: $\qquad$ (yes or no)
the 5. Figure out how long their trip was, in miles, and estimate about how many hours it took if they travelled the whole distance on an interstate highway.

Answer: The trip was $\qquad$ miles; it took about $\qquad$ hours.

th 6. Put $>,\langle$, or $=$, in each $O$ below, and then in the correct place on the TIC-TAC-TOE board. Do you wind up with a "tic-tac-toe?"

1. $75 \bigcirc 85$
2. $12+9 \bigcirc 17+4$
3. $3 \times 6 \bigcirc 10+5$
4. 33-6 $3 \times 9$
5. $15+10+8 \bigcirc 2+2+6$
6. 45-8 $30+8$
7. $5 \times 5 \bigcirc 10+10+3$
8. $88 \bigcirc 30+44+14$
9. 15-6-0 O2x4

Answer: $\qquad$ (yes or no)


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STAR PROBLEMS Grade 3, VIII

I have neither given nor received help on these problems: $\qquad$
tt 1. How mach will all of the blocks below weigh, if each block weighs 7 grams?


Answer: $\qquad$
tth 2. Complete the square so that the sum of each row, colum, and diagonal is the same.

|  | 2 | 3 | 13 |
| :---: | :---: | :---: | :---: |
| 5 | 11 | 10 |  |
| 9 |  | 6 |  |
|  | 14 | 15 |  |

* 3. The sun of the digits of a 2-digit number is five. If the digits are reversed, the new number is nine less than the first number. What is the first number?

Answer: $\qquad$
th 4. Draw the missing figure in the box to the right.

5. Julio added the cost of some things he bought for school on his new calculator. The total is shown on the calculator to the right. How much did he spend?

Circle the correct answer:
(a) $\$ 4.50$
(b) $\$ 4.06$
(c) $\$ 46$
(d) $\$ 0.46$


* 6. On the grid below, draw 4 rectangles that have different lengths and widths, but each has area 24. (The area is the total numbe: of squares inside the rectangle.)


7. Barry found a rusted, antique clock in his Grandmother's attic. How many hours will this 4-day clock run, without winding it?

Answer: $\qquad$ hours


* 8. Mario had three stacks of pennies--one stack had $30 c$ in it, the next stack had $25 c$ in it, and the last stack had 35c in it. How many pennies would be in each stack if Mario made them all the same height?


I have neither given nor received help on these problems. $\qquad$

1. A school bus holds 42 students. It took 4 fully-packed buses, and a car holding 5 extra kids, to get the entire school to an end-ofyear party. How many students attended the school?

Answer: $\qquad$
$t+$
2. Cowboy Joe wants to build a 100-foot long fence for his horses. How many posts will he need if he places them 10 feet apart?


Answer: He '11 need $\qquad$ posts.
t 3. Greg's bedtime is 9:00 p.m. He wants to watch television before going to bed. Which show will he be able to finish watching and get to bed on time?


Answer: $\qquad$
the 4. Find the sum. Round your answer to the nearest tenth.

$$
\begin{array}{r}
0.22 \\
+0.56 \\
\hline
\end{array}
$$

Answer rounded to nearest tenth: $\qquad$
the Put the missing digits in the boxes to the right.

. Draw a ring around the picture of a right angle.

t 7. Count the cubes to find the volume.


Answer: $\qquad$ cubes

* $*$ 8. Mark counied his pennies one night. When he put them in groups of 4, he had 2 pennies left over. When he put them in groups of five, he had 1 left over. What is the smallest number of pennies he could have, if he has more than 10 ?

Answer: He has $\qquad$ pennies.

* 9. How many rectangles are there in the figure to the right?

Answer: $\qquad$

$\qquad$
$\star \star *$ 1. Circle the figures below which contain this shape:

tt 2. Fill in the missing digits.

| 3 | 4 | $\square$ | 1 |
| :---: | :---: | :---: | :---: |
| 8 | $\square$ | 6 | 0 |
| 5 | 4 | 2 | $\square$ |
| 7 | 8 | 0 | 6 |
| $2 \square$ | 2 | 8 | 0 |

$\star *$ 3. Use the pattern to draw the circle and triangle in the fourth box.

4. What is the mass of the flower pot? Circle the answer.

A. 40 grams
B. less than 40 grams
C. more than $\mathbf{4 0}$ grams

* 5. School begins at 8:30 A.M. and ends at 2:45 P.M. How many hours and minutes must George plan on being at school?

ANSWER $\qquad$
$\star+6$. Use $\mathbf{a}$


Bob worked a problem on its calculator. When he turned the calculator upside down, he was surprised to see this message, f 1808 (hi Bob). witch problem made this message? Circle it.
i. 45547
B, 99777
C. both
$+35267$
$-18963$

* $\boldsymbol{*} \boldsymbol{*} \boldsymbol{*}$ 7. Est mate the area of the mitten if one square unit is equal to one square centimeter. Circle the answer.


8. Follow the flowchart, When you come to the missing step, choose the activity that best fits the flowchart. Circle the answer.
A. Make a sandwich
B. Watt for the toast to pop up
i. Butter the toast
D. Eat the toast


STAR PROBLEMS
Grade 3, XI

I have neither given nor received help on these problems: $\qquad$

* 1. The par' is 25 kilometers from Kay's house. The store is 33 kilometers from her house, and the lake is 42 kilometers from her house. How much farther is the lake than the park from Kay's house?

Answer: $\qquad$ kilometers

$\star t$ 2. Ella bought a hamburger, french fries, and $z$ soda. How much, including tax, did she pay for her lunch?

Answer: $\qquad$

MENU
Hamburger...... . \$1. 30
Hot Dog......... . 85
Ham Sandwich... 2.00
French Fries... . 75
Milk........... . 50
Soda............. . 50
TAX TABLB

| SALE AMOUNT | TAX | SALE AMOUNT | TAX |  |
| :---: | :---: | :---: | :---: | :---: |
| $\$ .01-\$ .25$ | $\$ .01$ | $\$ 1.51-\$ 1.75$ | $\$ .07$ |  |
| $.26-$ | .50 | .02 | $1.76-2.00$ | .08 |
| $.51-$ | .75 | .03 | $2.01-2.25$ | .09 |
| $.76-1.00$ | .04 | $2.26-2.50$ | .10 |  |
| $1.01-1.25$ | .05 | $2.51-2.75$ | .11 |  |
| $1.26-1.50$ | .06 | $2.76-3.00$ | .12 |  |

3. Put one of these words into the blank to make a true statement: celsius meters liters grams

Statement: The mass of a banana would be measured in $\qquad$ .

* 4. Fill in the missing digits:

* 5. To the right is a picture of what the PacMan 2 game board looks like. Each is worth 1 point, and each $O$ is worth 5 points. If you clear the whole board of dots, without catching a flickering ghost, how many points will you score?

Answer: $\qquad$

6. Circle the correct sign to make this number sentence true.

$$
34-28 \quad ? \quad 78-69
$$

Answer:


* 7. Mark left home at 7:30 A.M. It takes him 35 minutes to walk to school. School starts at 8:00 A.M. Was Mark late for school?

Answer:
tr it 8. Use the graph to answer the questions below.

A) Which children read at least 18 books?

Answer:
B) How many more books did Mary read than John?
C) If A1 read 12 books total for May and June, how many books did he read in June?

Answer: $\qquad$
th 9. Find the answer to this problem by using a calculator.

$2 3 \longdiv { 1 1 7 , 4 6 1 }$

Turn the calculator upside down.
What name does the answer opel?

I have neither given nor received help on these problems: $\qquad$


1820
※4.3. You saved your allowance and bought a baseball and glove. How much did you pay the sales clerk? Don't forget-sales tax is $5 ¢$ on every dollar spent.

Answer: $\qquad$
4. What is the mass of the friendly Blob? Circle the correct answer.
A. Equal to 3 grams
B. More than 3 grams
C. Less than 3 grams


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5. Bob bought a notebook for 89 c and a pencil case for 93c. He gave the clerk one five-dollar bill. About how much change should he get back? Circle the best estimate below:
(a) about \$1
(c) about $\$ 3$
(b) about \$2
(d) about \$4

* 6. According to the chart, who had perfect attendance?

Answer : $\qquad$


KEY: $)=30$ days.
perfect attendance $=180$ days
$\star \geqslant$ 7. $A \operatorname{dog}$ and cat together weigh 27 pounds. If the dog weighs twice as much as the cat, how much does each weigh?


Answer: The dog weighs $\qquad$ pounds. The cat weighs $\qquad$ pounds.
8. Which is heavier, a pound of cotton or a pound of lead?

Answer: $\qquad$

$t \rightarrow t$ 9. You opened your reading book and saw that the sum of the facing pages was 53. What were the two pages you opened to?

Answer: $\qquad$ and $\qquad$ 142

STAR PROBLEMS
Grade 3, XIII
I have neither given nor received help on these problems: $\qquad$
$* * 1$. Find the area of the figures to the right:

Answer: The house is $\square$ 's. The tree is $\square$ 's. The bush is

$\star \geqslant 2$. The chart to the left shows four animals, and the number of times per minute their hearts beat. Look at it carefully, and then fill-in a word below that makes good sense.

A big animal's heart beats $\qquad$ than à small animal's heart.
$\star \star$ 3. Jane boight a milkshake for $\$ 1.39$, and paid for it with a five-dollar bill. Circle the correct amount of change she should receive:
(a) 1 penny, 2 quarters, 3 one-dollar bills
(b) 9 pennies, 1 quarter, 4 one-dollar bills
(c) 1 penny, 1 dime, 2 quarters, 3 one-dollar bills
(d) 1 penny, 1 dime, 2 quarters, 4 one-dollar bills
4. Put the correct symbol $(>,<;$, in each circle to the right, to make the statement true.

$$
\begin{aligned}
& { }_{2+2+2}^{2} \bigcirc_{2 \times 3} \\
& 12+11 \bigcirc_{21-3} \\
& 17+56 \bigcirc_{100-43} \\
& (4+7)-1 \bigcirc_{4+(7-1)} \\
& 2 x(6-4) \bigcirc_{(2 \times 6)-4}
\end{aligned}
$$

* 5. Amy has a machine that squares every number that goes into the machine. If 5 goes in, for example, $5 \times 5$ or 25 comes out. If 6 goes in, $6 \times 6$ or 36 comes out. Fill in the chart to show what numbers come out of the machine:


INPUT NUMBER OUTPUT NUMBER

| 1 | 1 |
| :--- | :---: |
| 2 | 4 |
| 3 | $\square$ |
| 5 | 25 |
| 6 | 36 |
| 7 | $\square$ |
| 8 | $\square$ |

6. The three clementary schools in St. Lucie County have enrollments of 2,413 students, 1,946 students, and 3,012 students. What is the total number of elementary students in St. Lucie County, rounded-off to the nearest hundred?

Answer: $\qquad$ students
7. What is the answer if you do the steps below, in order?


Answer: $\qquad$
tht
8. If you start with a certain number, and follow the directions indicated by the flowchart below, you'll get 24 at the last step. What number must you start with? Write it in the first hox below.

** 9. Do these two problems, please.

749505748859977088801

- 9728351085999349024

I have neither given nor received help on these problems: $\qquad$
*** 1 .


Look at the spinner at the left and answer the following questions.
(A) What is the probability that you will spin a green?
(B) What is the probability that you will not apin a green?
(C) What is the probability that you will spin a yellow?
$+2$.


To find out what is for lunch, use the secret code. Go EAST and NCiTH to find each letter.

$\mathbf{s}$
tt 3. Draw the shapes that are missing in each of the blank blocks bolows
(A)

(B)


* 4. Look for the pattern and fill ine missing number in each jank below:

$$
\begin{array}{llllllll}
1 & 4 & 7 & 10 & \ldots & 16 & \ldots & 22
\end{array}
$$

tht 5. The thermometers at the right show the temperature in Cocoa Beach on two days. Look at each and answer the questions belows
(A) Compared to Monday, did Tuesday's temperature rise or fall?
(B) If the temperature on Friday rose $15^{\circ}$ above Tuesday's temperature, what temperature would it be?
(C) Would you be likely to need a heavy coat Friday?


Monday


Tuesday

Tenperature in Celsius

* 6. Ink was spilled on the patterns below. On the line above each ink spill, draw the hidden shape.
(A)



(B)

$t \star$ 7. The problem below is an example of an "estimated" answer,

$$
\begin{aligned}
& 684 \text { estimated to be } \\
& 210 \text { estimated to be } \\
&+300 \\
&+397 \text { estimated to be }+\frac{400}{1300} \\
& \hline
\end{aligned}
$$

When you turn in your paper, you will be given a problem like this and asked to estimate the sum in your head. Practice problemg like this before then.

Answer goes here as you turn in paper: $\qquad$

* 1. The sun shone every day last week. The class kept a record of the hours of sunlight.

| Days of the Week |  | Hours of Sunshine |
| :--- | :--- | :---: |
| Monday |  | 10 |
| Tuesday | 10 |  |
| Wednesday | 5 | 10 |
| Thursday | 5 |  |
| Friday |  | 5 |

To find the average (mean):

1. Find the sum of the hours.
2. Divide the sum by the number of days.

Answer: average hours of sunshine $\qquad$

Wt 2. Use 4 different color crayons to color the map below. No state can be the same color as another state that touches it along a border. Two states can be the same color, if they only meet in a point.

3. What number should the
 be to make this sentence true?

$$
67-\square=28
$$

th 4. Jane noticed that she was a little shorter than half of her friends and taller than half of them. Guess how tall Jane was.

| Jane's Friends | Height |
| :--- | :--- |
|  | 48 inches |
| Sue | 47 inches |
| Harry | 43 inches |
| Ted | 51 inches |
| Mary | 44 inches |
| Betty | 45 inches |
| Jerry |  |

Answer: Jane was __ inches tall.
5. If $316+X=538$ then $X$ must be what number?

Answer: $X=$

* $\$$ 6. To be a simple closed curve there must be only one inside and one outside and the curve itself must be closed.

simple closed curves

not simple
closed curves

not simple closed curves

Look at the pictures below. With a crayon color the inside of each simple closed curve. Do not color any curve that is not a slmple closed curve.


I have neither given nor received help on these problems:
$\qquad$
th 1. A cat cost $\$ 5.95$, and a litter box cost \$2.95. Enough food for a month cost $\$ 3.98$, and enough litter for a month cost \$1.89. Estimate how much it cost to buy the cat, and keep it the first month.Between \$5 and \$10.

- Between \$11 and \$16.

Between \$16 and \$21.
O Between \$21 and \$25.
tht 2. Estimate the cost of buying such a cat, and keeping it for a whole year. Bubble in the best estimate below:

$$
\begin{aligned}
& \text { Between } \$ 170 \text { and } \$ 190 . \\
& \text { Between } \$ 55 \text { and } \$ 75 . \\
& \text { Between } \$ 80 \text { and } \$ 85 . \\
& \text { Between } \$ 100 \text { and } \$ 120 .
\end{aligned}
$$


th 3. The volume of a solid shape is the muber of blocks it would take to build it. What is the volume of the solid shape to the left?

Answer: $\qquad$ blocks
th 4. Fill in the table to show which coins could be used to equal the total anount. The first one has been done for you, as an example.

NO. OP
COINS

| AMOUST | USED | QUARTER | DIMP | NICREL | PENNY |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 324 | 4 | 1 |  | 1 | 「3 |
| 264 | 2 |  |  |  |  |
| 45 | 9 |  |  |  |  |
| 154 | 2 |  |  |  |  |
| 194 | 7 |  |  |  |  |
| 384 | 5 |  |  |  |  |
| 204 | 2 |  |  |  |  |

t 5. The atudent who did the problems below made the same mistake in each one. Find the mistake, and work the last problem WRONG just like the other three. (Don't get in the habit of subtracting this way!)

$$
\begin{array}{rrrr}
46 & 84 & 91 & 63 \\
\frac{-37}{11} & \frac{-57}{33} & \frac{-42}{51} & \underline{-25}
\end{array}
$$


*tt 7. If $A=1 c, B=2 c, C=3 c$, and $s o$ on till $Z=26 c$, what would be the value of your principal's last name?

Answer: $\qquad$
*8. Odd numbers are the numbers $\{1,3,5,7,9,11,13$, and so on $\}$. Even numbers are the numbers $\{0,2,4,6,8,10,12$, and so on $\}$.

Is the value of your principal's last name an odd number, or an even number?
Answer: $\qquad$
thting. Use the chart to the right to find these answers:
(a) What time does Channel 17 come on the air? $\qquad$
(b) How long a program is Billiards? $\qquad$
(c) How long is Sesame Street on the air each day?


I have neither given nor received
Grade 3, XVII help on these problems: $\qquad$
tt 1. Find an ordinary drinking glass in your house, and make a guess as to whether it's longer around the rop than it is high. Then figure a way to measure those two lengths.

Which is longer, the height of the glass, or the distance around the top edge?

Answer:
2. Find a way to put $1,2,4$, and 7 in the boxes below, to produce a true sentence. Then check your work on a calculator.
$\square \oplus \square \square \square$
区

E 1
t 3. Now use the same numbers as in problem 2, and find a second way to socve the problem.
5 5 $\square$ [x]

$\square$ B 1

Wtty 4. Bob got $\$ 2$ each week for cleaniug ins room, but he spent 25 cach afternoon after school for a si 3ck. How long would he have to save to buy a stereo tape that costs $\$ 8$ ?

Answer: He'd have to save for $\qquad$ weeks.
5. If line $A B$ represents ten yards, about how long would line $B C$ measure? Bubble in the best answer.

$$
\begin{array}{lll}
C & 2 & \text { yards } \\
0 & 4 \text { yards } \\
C & 7 \text { jards } \\
0 & 12 \text { yards }
\end{array}
$$


6. Add, if you have a strong he $:=t$ :

恬
$t$ tit 7. How many ways can you put these three hamsters into the two cages?


Cage 1


Cage 2


A

$\rightarrow$ 8. Name the three different kinds of angles found in the figure below. Use three letters in naming each angle.

Answer: A right angle is: $\qquad$ An acute angle is: $\qquad$
An obtuse angle is : $\qquad$


* 9. Write the letter for each number pair to find out what the teacher is saying.

1st word: $(1,8)(1,2)(3,3)$
$\therefore$ Ina word: $(11, ?)(8,7)(10,4)(11,1)$

- 3rd word: $(3,9)(10,9)(5,4)$
- th word: $(8,9)(4,1)(7,4)$
- Fth word: $(6,7)(6,1)(8,2)(1,5)(4,6)$


STAR PROBLEMS
Grade 3, XVIII

I have neither given nor received help on these problems: $\qquad$

Which show is on the air for the longest time?

Answer: $\qquad$
How many minutes longer is the music program than the sports report?

Answer: $\qquad$
thtit 2. Alice and Andy are twins. Their Mow is 24 years older than they are. If you add the age of all three of then together-Alice's age + Andy's age + Mom's age-you get 60 years. How old are the twins?

Answer: $\qquad$ years old.
3. How many blocks were used to make this solid design?

4.


There is a bag with two white marbles and one black marble. Without looking, you take a marble from the bag. What are your chances of NOT getting the black marble?

Answer: $\qquad$
$t$ 5. If you are 11 years old and I am 36 years old, how old will I be when you are 29 years old?

Answer: $\qquad$ years old.

* 6. In the land of Tur, each person has one and only one car. The license plate of each car is different and has one letter and one numeral on it. To date, the letters $A, B, C$, and $D$ have each been used with each of the numerals $1,2,3,4$, and 5 . Complete the list of license tags.

* 7 7. Mark the coordinates and connect then in order.

| a. $(0,1)$ | f. $(6,2)$ |
| :--- | :--- |
| b. $(1,2)$ | k. |
| c. $(6,4)$ |  |
| c. $(1,1)$ | 1. $(8,4)$ |
| d. $(2,1)$ | m. $(8,3)$ |
| e. $(3,2)$ | n. $(7,3)$ |
| f. $(4,2)$ | o. $(6,2)$ |
| g. $(4,1)$ | p. $(4,5)$ |
| h. $(6,1)$ | q. $(1,5)$ |
| 1. $(5,2)$ | r. $(0,1)$ |


8. You are going to eat a normal lunch. About how long would you expect your submarine sandwich to be? Circle the answer.
a. 3 cm .
b. 25 cm .
c. 100 cm .
d. 75 cm .

STAR PROBLEMS
Grade 3, XIX

I have neither given nor received help on these problems: $\qquad$ $\begin{array}{r}9 \square 82 \\ -38 \square 6 \\ \hline 5836\end{array}$
tit 2. Study the number pattern. The dots mean that the numbers continue in this pattern.
a. Fill in the missing number in the box in colum $C$.
b. In what column is number 22 ?

Answer: 22 is in column $\qquad$ .
c. In what column is number 96?

Answer: 96 is in column $\qquad$ -

the 3. Draw the sixth shape:


th 4. Answer these questions about the pictogram below.
a. How many students are in Mr. Smith's class? Answer: $\qquad$
b. How many 3rd grade students attend Center Elementary School? Answer: $\qquad$

$\star \star 5$.

$\square$is a .quatre centimeter. About what is the area of the shape to the right, in square centimeters?


Answer: $\qquad$ square centimeters
$\star \star$ 6. You have put this program into your computer, in BASIC.
10 Print "bella"
20 print "heat is your nave?"
30 END
If you now run the program, what will you see on the display screen to the right?

$*$ 7. Use the numbers $1,2,3,4$, and 5. Place them in the $O$ 's on the figure below. Be sure that no number is connected to its neighbor. For example, 3 cannot be connected to 4 .


* 8. Using centimeters, estimate correctly to fill in the sentences below.
a. The length of the arrow is about $\qquad$ centimeters.
b. The perimeter of the arrow is about $\qquad$ centimeters.


156

STAR P ROBLEMS
Grade 3, 2X

I have neither given nor received help on these problems: $\qquad$
tht 1. Marvin the Magnificent could pull rabbits out of hats. He could also pull doves from his sleeves. He had 9 hats and (of course) 2 sleeves. One day he got carried away. He pulled 15 rabbits from each hat and 29 doves from each aleeve. Marvin had encugh food for 125 rabbits and 75 doves. Use your calculator to decide what Marvin had to buy on the way home.

Circle your answer: a. rabbit and dove food
b. rabbit bood only
c. dove food only
d. nothing
trt 2 。

3. In a baseball diamond there are 90 feet between bases. Airhead McFleetfoot hit a home run out of the park. As he touched second base, he realized he . not tagged first base. After returning to correct his mistake, he c mpleted the trip to home plate. Make and label a diagram to show the path and distance he ran.

MY DIAGRAM
ANSWER
Airhead ran $\qquad$ feet.

* 4. You can trace a path through the house below so that you go through each door exactly one time. But you have to start in the $i$ ight room to do so. Find the right room, and make a check mark ( $\sqrt{ }$ ) there-show your path also. (It's ok for the path to go outside the house, too.)

tht 5. Toss a coin 25 times and record the number of times it lands on heads and the number of times it lands on tails. Now toss the coin 25 times again and record your results. Use the chart below to record your data.

|  | Number of heads | Nunber of tails |
| :--- | :--- | :--- |
| First: $1-25$ tosses |  |  |
| Second: $1-25$ tosses |  |  |

After 50 tosses, the number of heads is closest to which number? Circle your choice.
(a) 10 heads
(b) 25 heads
(c) 40 heads
6. Cathy poured a handful of $M \& M^{\prime} s$. She got 7 brown, 2 green, 4 orange, and 6 yellow. Make a bar graph to show how many $M \& M^{\prime} s$ of each color she had.

$t+t \rightarrow$ 7. Twenty five children are in a class. $\frac{3}{5}$ ate pizza; $\frac{2}{5}$ ate hamburgers, Which answer best fits this class? Circle your choice.
a) 10 ate pizza and
15 ate hamburger
b) 2 ate pizza and $\begin{aligned} & 3 \text { ate habburger }\end{aligned}$
c) 15 ate pizza and 10 ate hamburger
d) 3 ate pizza and 2 ate h-mburger

STAR PROBLEMS
Grade 3, XXI

I have neither given nor received help on these problems: $\qquad$
tht 1. Think about a Rubik's cube for this problem, and answer the questions below:


How many of the small cubes have colors on 3 faces?
How many of the small cubes have colors on 2 faces only?
How many of the small cubes have colors on 1 face only?
tht 2. Annie has $\$ 2.45$ in dimes and quarters. She has the same number of dines as quarters. How many of each coin does she have?

Answer: Annie has $\qquad$ dimes and $\qquad$ quarters.

* 3. The lunchroon baked seven ples. Our class ate $2 \frac{4}{9}$ pies at lunch. About how mich pie is left? Circle the best answer.

a. 3 pies
b. $4 \frac{1}{2}$ pies
c. $5 \frac{4}{9}$ pies
d. 6 pies
* 4. Put $>,<$, or $=$ between each set of numbers below
a. $2371+481 \bigcirc 416 \times 6$
b. $3976-225 \bigcirc 3752 \times 1$
c. $60 \div 3 \bigcirc 60 \div 4$

5. Fill in the number that the square is covering up.

6. Draw the line (s) of symmetry for each figure. Some figures will have more than one line of symmetry. If there is no line of symmetry, do not mark the figure at all.

$\star$ 1. John started his homework when he got home from school at 3:30. It took his 45 minutes to complete his work. Draw the hands on the clock to show what time he finished.

th 8. Compute the following with a calculator. Turn the calculator upside down. Who is the famous mother written there? Write your answer below.

$$
2 \times(4962+12541)
$$

Answer: $\qquad$


STAR PRODLESS
Grade 3, XXII
** 1. Stare at the picture to the right until you see 2 different people. One is a young lady with a black ribbon around her neck - the other is an old witch.

Once you've seen both of them, put a $r$ on the young lady's chin and circle the old witch's mouth.

I have neither given nor received help on these problems: $\qquad$


|  | tax chart |
| :---: | :---: |
| . 01 | . 20 ------1c |
| .21 t | . 40 --m $2 ¢$ |
|  | . 60 -m-me- 3c |
| . 61 | . $80-3$ |
|  | 1.00 - - 5¢ |

* a. San bought one scoop of chocolate ice cream. How much did his ice crean cost with tax?

Answer $\qquad$
tb. Jake had 2 scoops of cherry and one scoop of rainbow ice crean. How much did he pay with tax?

Answer $\qquad$

* c. Paul had a acoop of vanilla and a scoop of raspberry ice crean. How much did he pay with tax?

Answer $\qquad$
ttd. Paul gave the clerk 50c. How much was his change?
Answer $\qquad$
3. Mother baked an apple pie. Dad ate $1 / 2$ of the pie at lunch. Pete ate $2 / 4$ of the pie after school. Who ate the moat?

Answer $\qquad$

4. The cuckoo bird is laughing at the time on the clock. But he wasn't laughing 3 hours and 10 minutes ago. What time was showing on the clock then?

Answer: 3 hours and 10 minutes ago, the time was $\qquad$ -

$\star$ 5. Think of a way to draw the matching half for the shape below. Hint: use the line of symetry show-you can fold the paper if you want to.

6. Find someone who will flip a coin with you for an experiment. Then each of you get a coin, and flip them together forty times and notice on each $£ 11 \mathrm{p}$ whether your coins match or are different. (They match if you both get heads, or both get tails; otherwise they are different.)

Each time you flip the coins, make a tally mark in the first space below. Each time you get a match, make a tally mark in the second space below.


FLIPS: $\qquad$
MATCHES: $\qquad$
7. Think about the experiment above, and then choose the best sentence below that describes what happened. Bubble-in your choice.My partner and I got a match about one-fourth of the time.My partner and I got a match about one-half of the time.
OMy partner and I got a match about three-fourths of the time. O My partner and I got a match almost all the time.

I have neither given nor received help on these problems: $\qquad$
\&\% 1. What is the starting number?

tt 2. Color the flowers whose products are even numbers.


th 5. John has $\$ 3.00$. He buys:


Draw a circle around the group of money below that he will have left.


* $*$ 6. Pretend that this thermometer is hanging on a tree outside your bedroom wi:adow. Wher you looked out in the afternoon the thermometer looked like the one below. Later on that night you looked out again and the temperature had dropped $15^{\circ}$. What was the temperature then?


Answer: $\qquad$
$t \star$ 7. A bag of marbles has 25 marbles in it, and costs 35c at R-Mart. How much will 150 marbles cost?

Answer: $\qquad$
$\star \star 8$. Write the missing sign ( + ,,$- x$, or $\div$ ) in each circle to make true statements going both across, and down, the puzzle.


I have neither given nor received help on these problems: $\qquad$

* 1. Circle the letters of the alphabet below tiat are made only of line segments. These will be the ones that do not have any curves in them.


## ABCDEFGHIJKLMNOPQRSTUVWXYZ

Look now at the ones you circled above. Place a $V$ on any of them where there are perpendicular line segments somewhere in the letter.

* 2. A can of cola has " 354 mL " written on its side, to tell how uuch cola is in the can. Tow many milliliters of cola would there be in a 6 -pack that costs $\$ 1.59$ ?


Answer: $\qquad$ mL
t 3. The first few triangular numbers are 3, 6 , and 10 . Can you see why?

| 0 | 0 | 0 |
| :---: | :---: | :---: |
| 00 | 00 | 00 |
|  | 000 | 0000 |

What are the next two $t_{1}$ 'ngular numbers?
Answer: $\qquad$ and $\qquad$
$t+1$ 4. Draw a line through the clock face below so that the sum of the numbers on each side is the same. An example that doesn' $t$ work is shown the the far right below.


* 5. The same digit goes in each box below, to give the correct answer. Write the correct digit in the boxes.

$\star$ t $\boldsymbol{t} \boldsymbol{*}$ 6. Tamika found a new way of adding numbers mentally. For a problem like $28+46$, she would "add a little" to turn one of the numbers into one she could add in her head. Then when she got the answer, she would mentally "take away the little" that she had added. Study how she would do this problem.


Practice adding this way on the problems below. After you have the answer in your head, you can check to see if you are right using your calculator. When you turn in your paper, you'll be given a probler like these and you'll have to find the answer mentally, to get your stars.

Practice problems:
(a) $37+46$
(c) $65+27$
(e) $46+35$
(g) $58+26$
(b) $48+29$
(d) $54+28$
(f) $69+24$
(h) $29+37$

Answer for the problem when you turn in your paper: $\square$

I have neither given nor received helf on these problems: $\qquad$


* 2. Circle the letters of the alphabet that are made only of line segments. These will be the ones that do not have any curves in them.

ABCDEFGHIJKLMNOPQRSTUVWXYZ
Look at the ones you circled above. Place a $\checkmark_{\text {on any of them where there }}$ are parallel line segnents somewhere in the letter.

* 3. How many rectangles are there in the figure below?


Answer: $\qquad$ rectangles

* 4. Find a thumb tack and toss it in the air 40 times. Make a mark in the the right place on the chart, to keep up with the way it lands each time.


5. Use the information you collected above to answer this question.

If you toss a thumb tack in the air, which way is it more likely to land? Circle the answer below.

$\star \star$
6. Charles used his calculator and decided that the ice cream cone he wanted would cost a little more than 65 , once tax had been added. Was his answer reasonable, or do you think he made a mistake on the calculator?

Answer: $\qquad$


* 7. The perimeter of the square below (the distance around the square) is 12 JEXIMS. Which of these answers would be the best estimate of the distance eround the circle? Bubble-in the best answer.
- 10 Jexuns
- 13 JExums
- 20 Jexums


8. Shirley got her teddy bear when she was 5 years old, and that was 3 years ago. If the teddy bear cost $\$ 14.99$, how old is Shirley?

Answer: $\qquad$ years old

## TEACHER COMMENTARY

## (Primary)

# STUDENT PERFORMANCE STANDARDS OF EXCELLENCE 

 IN
## MATHEMATICS

1984-85 through 1988-89

Division of Public Schools Florida Department of Education

## STAMDARDS

## A. THE STUDENT WILL APPLY PROBLEMSOLVING TECHNIQUES.

B. THE STUDENT HILL APPLY MATHEMATICS TO EVERYDAV, REALWORLD SITUATIONS.

SKILLS - The student will:
1001. Solve word problems requiring multi-step computation.
1002. Solve problems appropriate for a table, chart, or list organizational plan.
1003. Solve problems appropriate for drawing a diagram.
1004. Solve problems appropriate for a guess (or estimate)-checkrevise technique.
1005. Solve problems appropriate for $3 \quad 5$ a working backwards technique.
1006. Solve problems requiring visual 35 discrimination.
1007. $\left.\begin{array}{l}\text { Solve problems iavolving } \\ \text { sequential numpric and geometric } \\ \text { patterns. }\end{array} \quad \begin{array}{ll} & 5\end{array}\right)$
1008. Check the results of a prodiem35 solving attempt in terms of the original problem.
1009. Solve word problems that include 5 extraneous information.
1010. Form tentative hypotheses in
problem-solving situations.
1017. Compute the value of a set of coins and bills, and write it in decimal notation using the dollar sign.
1018. Compute the total cost of 35 several items including tax.
1019. Compute the change which would be received in making purchases.
1020. Solve problems related to manag-

35 ing personal income.
B. (continued) THE
STUDENT WILL APPLY
MATHEMATICS TO EVERY
DAY, REAL-WORLD SITU
ATIONS.

C. THE STUDENT WILL
DEMONSTRATE ESTIMA-
TION AND APPROXIMA-
TION PROCEDURES.
D. THE STUDEN T MILL PERFORM MATHEMATical computations.
1021. Solve problems related to manag-ing personal time.
1022. Solve problems which requir interpreting time schedules from a chart.
1023. Compute the sale price of an item discounted by a fraction.
1029. Estimate the solution to compu- tational exercises involving whole numbers.
1030. Estimate the solution to money problems.
1031. Estimate linear measurements.
1032. Round any decimal number less than 1, with up to 3 decimal places, to the nearest designated place.
1033. Estimate t..e solution to compu- tational exercises involving and - of mixed decimal numbers.
1034. Estimate the solution to compu- tational exercises involving + and - of mixed fraction num- bers.
1035. Give reasonable responses based on personal knowledge of a situ- ation rather than rounding and computing.
1036. Estimate any appropriate measure ..... 5 (length, area), given geometric figures of two dimensions.
1037. Determine whether or not a pro- ..... 5 posed answer is reasonable in a given problem situation.
1046. Determine the relationship (>, ..... 3 <, $\Rightarrow$ between expressions using + and - of whole numbers.
1047. Add or subtract multi-digit ..... 3 whole numbers, using standard algorithms.
D. (continued) THE STUDENT HILL PERFORM MATHEMATICAL COMPUTATIONS.
E. THE STUDENT WILL USE MATHEMATICAL SYMBOLS AMD CONCEPTS TO SOLVE PROBLEMS mithin mathematical SYSTEMS.
1048. Add or subtract multi-digit ..... 3
whole numbers, using alternative methods.
1049. Multiply or divide a 2 - or more digit whole number by a 1 -digit number.
1050. Solve computational puzzles for whole numbers that demonstrate understanding of, and ingenuity with, computational principles.
1051. Determine the relationship (>, ..... 35
<, $=$ ), between proper fractions.
1052. Multiply or divide multi-digit ..... 5 whole numbers, using standard algorithms.
1053. Multiply or divide multi-digit ..... 5
whole numbers, using alternative methods.
1054. Compute sums, differences, pro- ..... 5 ducts and quotients in exercises that involve parentheses.
1055. Add or subtract two mixed numbers. ..... 5
1056. Multiply 2 decimal numbers. ..... 5
1072. Write the standard base-ten ..... 3numerals for an expanded numeral.
1073. Dezermine whether any given ..... 3whole number is odd or even.
1074. Solve simple equations of the ..... 35 form $a \pm x=b$ for $x$ a whole number.
1075. Rename a base-ten numeral as a ..... 5bare-two numeral, or conversely.
1076. Classify the sum, difference, product or quotient of odd or even numbers as odd or even.
1077. Solve equations of the form ..... 5 $a \bullet x=b$ or $x i a=b$, for $x$ a whole number.

> E. (continued) THE STUDENT WILL USE MATHEHATICAL S:MBOLS AND CONCEPTS TO SOLVE PROBLEMS WITHIM MATHEMATICAL SYSTEMS.     F. THE STUDENT WILL RECOGNIZE AND APPLY GEOHETRIC CONCEPTS.
G. THE STUDENT MILL RECOGNIZE AND APPLY MEASUREMENT CONCEPTS.
1078. Solve simple algebraic inequalities involving + and -.
1079. Determine if a given number is
prime or composite.
1080. Write composite numbers as the product of prime numbers.
1081. Determine the Greatest Common ..... 5 Factor (Divisor) and Least Com- mon Multiple for 2 whole numbers.
1107. Identify fundamental geometric ..... 35 figures.
1108. Recognize fundamental geometric ..... 35 concepts.
1109. Classify geometric figures. ..... 35
1110. Recognize and apply topological concepts.
1111. Perform basic line and angle constructions.
1122. Convert within given units of ..... 3 measuring time.
1123. Apply the concept of measuring ..... 35 elapsed time.
1124. Apply the concept of measuring ..... 35 temperature.
1125. Apply the concept of med uring ..... 35 length.
1126. Apply the concept of measuring ..... 35 area.
1127. Apply the concept of measuring volume and/or surface area.1128. Apply the concept of measuringmass.1129. Convert given measures of massto equivalent answers.1130. Convert given measurcs of lengthto equivalent answers.
6. (continued) THE

STUDEMT WILL RECOGMIZE AND APPLY MEASUREMEN' CONCEPTS.
H. THE STUDENT MILL COLLECT DATA AND CONSTRUCT, INTERPRET AND DRAM COMCLUSIONS FROM DESCRIPTIVE TA BLES, CHARTS AND GRAPHS.
1131. Determine the degree measure of ..... 5
an angle.
1144. Read, interpret and construct pictographs.
1145. Read, interpret and construct ..... 3 bar graphs, line graphs and tables.
1146. Graph ordered pairs of numbers ..... 35 using a Cartesian coordinate system.
1147. Collect, organize and represent ..... 35 data using an appropriate picto- graph, bar or line graph, or table.
1148. Read, interpret and construct circle graphs.
1149. Predict specific outcomes from a set of data, given that the pre- sent trend continues.
1150. Read and determine relationships represented by multiple line and bar graphs.
1153. Collect and record data for a simple probability experiment.
1154. Determine measures of central ..... 3 b
tendency for a set of data.
1155. Use common fractions to describe ..... 5 the probability of an event.
1156. Use common fractions to describe ..... 5 the probability of the complement of an event.
1157. Design a simple experiment, col- lect data and draw appropriate concl usions.
J. THE STUDEMT MILL DEMONSTRATE KNONLEDEE OF CALCULATORS AND COMPUTERS AS APplied to mathematics.
1166. Organize, complete, or follow the logic of a flowchart for a daily activity.
1167. Perform the computation involved in a mathematical flowchart with specific input.
1168. Use a calculator to perform computations.
1169. Determine whether an answer on a calculator or computer is reasonable for the given problem.
1170. Demonstrate knowledge of calculator and computer input and output displays.

35

35

35

35

# TEACHER COMMENTAKY 

## FOR

GRADE 1 WORKSHEETS
$\qquad$
TEACHER COMMENTARY

| Problem | Skill of Excellence | Corment |
| :---: | :---: | :---: |
| 1 | -- | This problem is a simple "union of sets" interpretation of addition. |
|  |  | ANSWER: 11 |
| 2 | -- | "Comparison of sets" is the subtraction interpretation for this problem. Students should solve it by matching up the snails and rocks $1-$ to-1, and counting the extra, unmatched snails. Later on this problem can be interpreted as "7-5." |
|  |  | ANSUER: 2 |
| 3 | $\begin{aligned} & 1020 \\ & 1144 \end{aligned}$ | This problem involves both personal income, and interpreting a pictograph. For the small-group session, you might place a dime over each smiling face, and have tive kids count by 10 's for similar type problems. |
|  |  | ANSWER: 50¢ |
| 4 | 1031 | Students can either use a personal unit to represent a centimeter (perhaps a paper clip), or a ruler. In any case, the pictures are close to, but not exactly, whole number units. So the question is "which unit is a picture rlosest to, in length?" (If students use a ruler, be sure they place the end of the ruler at one end of the picture; it would also help if their rulers did not have millimeters apparent.) |
|  |  | ANSWERS: 4, 2, 3 |
| 5 | -- | "Movement on a number line" is the addition interpretation for this problem. |
|  |  | ANSHER: $10+2=12$ |

[^1]Skill of

Problem
1 Excelience

1002

This problem involves mentally "working backward" for the student, since he or she knows how much money was spent, and must find out the items that led to spending that much money. Notice that the student might also solve the problem by "guess-check-revise." In your small-erroup session, you might take the same toys and their prices, but a different sum, and as! ther: 0 find the toys. Or you might let students write a problem for the group to solve, using this information.

ANSWER: car, drum, boat

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1004 | Students will probably solve this problem by counting |
|  |  | (or adding) the numbers that are visible--7,3,2, and |
|  |  | 1--and count 4 more times tili they get to 17. This |
|  |  | is similar to a mmissing addend" type problem. They |
|  |  | could also solve it by "guess-check-revise" although |
|  |  | this is an inefficient way to solve this particuiar |
|  |  | problem. To do so, they would simply guess numbers |
|  |  | to go in place of the "?," and add each time to see |
|  |  | if they get 17--if not, they revise the guess either |
|  |  | up or down. |

ANSWER: 4

The purpose of this problem is to cover the concept of mass, in a "balance board" situation. If students have trouble realizing that the lower end indicates a heavier object, have them think of a playground "teeter-totter" situation. Be sure to bring out that a large object is not always heavier than a small one, as in a "balloon, coffee cup" example. They must look at the position of the board to decide.

ANSWER: The bunny should be colored.

The idea behind the graph is to introduce "pictographs."

ANSWER: Florida

1001 This is a multi-step word problem involving a realTife situation. The student will probably solve the problem by counting, rather than adding. They will get the total for 1 day, and then count that same amount for 5 days. Note: If a child got 21 as an answer, they proisably didn't read carefully or understand about "school days."

ANSWER: 15 hours

This problem requires visual discrimination as the student searches for the pattern. The hard part of the problem, for some students, is that the numbers are in "descending order."

ANSWER: 2 dots, then 1 dot in the boxes

7 --
Students are using several concepts if they correctly solve this problen-ordinal numbers, "left," "last," etc.

AMSMER: The 1st star

## TEACHER COMPENTARY

Comment
This problem reinforces the term "triangle" and visual discrimination. Students should be encouraged to look first at the smallest-sized triangles, and count them ( 4 such). The child can then look for larger-sized triangles, and count all of a particular size he finds, moving up to the largest possible. In this case, the next-sized triangle is the largest possible, so there's only 1 more than the little ones.

ANSWER: 5

This problem lays an intuitive foundation for a word problem, using the partition interpretation of division (later in life, kids will solve this problem by " $12 \not 22=6^{\prime \prime}$ ). At this stage, they can solve the problem by drawing lines from the fish to be moved, to the other bowl. Then they can count and see how many they moved. For students who have difficulty, model the problem with an ordiaary container, and 10 pencils.

ANSMER: 6
$4 \begin{array}{r}1050 \\ 1004\end{array}$
41050
This problem combines a "story problem" situation, with visual discrimination. Students can find the answers to the two problems by counting, but the challenging part is that they have to count legs and ears that aren't visible.

AMSWER: 16 ears
32 legs

This computational puzzie requires some ingenuity. The students who solve it will probably do so using some form of "guess-check-revise." One solution is shown below:

ANSMER:


This problem is an extension of problem 1, worksheet II. The student is asked to deal with 7 fish instead of 5 , and also write the final answer in addition to filling-in the chart.

ANSWER: 8 ways
$6 \quad 102$
This problem gives a chance to talk al uut "estimating the solution to money problems." The students who get this problem correct probably spend time shopping with their parents, and haje gained knowledge through real-world experiences.

ANSUER: 2
$\qquad$

## TEACHER COWMENTARY

## Problem

1
Skill of Excellence

1007

1074
i. Omment

This problem involves a sequential geometric pattern. The child should notice that the circ': ss are divided into " 1 additional piece," moring from left to right. The answer, then, would be a circle that's lirger than the last one shown, and which is divided into 6 pieces. (Don't count off if the child didn't make the pieces equal in size, or if he or she didn't draw a true circle.)

AMSWER:


The student is to complete this intuitive introduction to an algebraic equation of the form $10=x+6$ in which the child "solves for $x$." If students have trouble with it, check to see if they understand what " $=$ " really means. Then make up some problems like this on $3 \times 5$ cards, with all 3 numbers shown, as in $7=5+2$
Make a square big enough to cover up a number, and go through the cards, covering up a different number, position wise, each time, as in

$$
7=5+\square
$$

AMSWER: 4

3,41124
Both of these problems have students deal with a realistic, measuring situation. The fact that the scale goes up in increments of $5^{\circ}$ instead of $1^{\circ}$ will give many students difficulty. Go over with them that the intermediate increments are half-way between the multiples of ten, and so they muet represent numbers that are half-way between those numbers. Use a much larger thermometer than the one pictured, and have them move their fingers to touch various temperatures you give them.

ANSWER: (3) $-0^{\circ}, 30^{\circ}$
(4) - The left-hand thermometer should te marked at half-way between $70^{\circ}$ and $80^{\circ}$--the right-hand thermometer at $50^{\circ}$ exactly.

185

This problem involves getting change. Students might find the answer either by subtraction, or by "counting up" from $\$ 7$ to $\$ 10$, the way a store clerk would do. If students don't have the concept of what "getting change" means, go through some similar problems with the students "acting out" the two roles.

AMSUER: \$3

Students can be introduced at an intuitive level to geometric constructions in problems such as this. If the student folds the paper correctly, he or she has actually made the "perpendicular bisector" for the line segment. Be sure to show them how to hold the paper up to the light, so they can match up the end points, before making the crease. Then have them measure to be sure the line has been cut exactly in half.

ANSMER: Observe to see if it is correct.

This problem has students doing addition problems mentally, using an "easier method" than adding straight down the column. Hopefully they'll realize that mental arithmetic allows them to "play games" with the standard way of adding, and that's necessary at times. Give them this problem which is written out and taped to the table or desk. Have the stuJent work the problen and write answer on his/her paper. Hatch and be sure they use no visible crutches--fingers, etc. --and that they only write their answer down, with no intermediate steps:

1
3
7
9
$+4$
ANSWER: 24

TEACHER COMFENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1125 | The student has an opportunity to lemonstrate knowledge about measuring length in this problem, in a challenging manner (for a lst grader). They will also have to use some "approximation" skills, since the parts of the giraffe do not exactly match up with the lines on the vertica! axis. |
|  |  | The height of the giraffe is straight forward--13, but for the other lengths, the student will have to either start counting at a number other than zero to find the length, or else subtract the beginning point from the end point. The answers below are approximations. |
|  |  | ANSWER: 13 <br> 6 (from 7 to 13); perhaps 3 or 4 (neck up to, but not including, the head) <br> 5 (some child might say " 20 "--counting all 4 legs) <br> 3 (7 to 10) or perhaps 4 ( $61 / 2$ to $101 / 2$ ) |
| 2,3 | 1072 | These prcblems give students experience with whole number numeration, but in a way different from the usual textbook presentation. Before the student can write the correct numeral, he or she must "reorder the groups," or the numerals, with the hundreds to |
|  |  | In the small-group session, go over similar problems, but with real (not pictured) manipulatives. |
|  |  | ANSVERS: (2) 256 <br> (3) 184 |

This problem has students follow the steps of a mathematical flowchart. It also "sets the stage" for the higher-level question to follow.

ANSWER: 2

Students can find the answer to this problem by "working backward." If so, they would start with 12, and ask themselves "what did I have to have in the previous step (before adding 3)?" They would continue this process, "working backward," till they found what number was in the first box.

Note that many of them will also solve this by "guess-check-revise." They'll simply guess a number for the first box, and check it out and see if it works when they add 4, then 2 , then 3 and get 12. If not, they will revise their guess to another number.

To help those having difficulty, put some problems like this on $3 \times 5$ cards, but with all the numbers included. Take a card at random, and cover up one of the numbers, and have them guess what it is. Check their guess by adding, and then revising the guess up or down.

ANSWER: 3

6,7 1146
These two problems are designed to introduce students to the Cartesian Coordinate system. In going over the problem with students, be sure that they understand that they always go East first, and then North. Tell them that we could have chosen to do the opposite (North first and then East), but a long time ago people decided to all do the same thing, and it was decided that East, then Morth in that order. At this point, do not push the students into "ordered pairs," but concentrate rather on the concept of moving from "start" to another point, in a standard fashion. Have them follow such trips with their finger.

ANSUERS: (6) 1,3
2,2
4,0
4,3
(7)
-

These three problems are actually designed to reinforce wie terminology associated with geometric fi-gures--triangle, circle and rectangle. In covering this with a group of student:, you might extend the problem cautiously by asking questions such as:

How many stars are in the rectangle, but not in the triangle?
How many stars are in both the triangle and the circle? (etc.)

ANSWERS: (8) 8 (if a child answers "3" or "5," they might be lroking at one of the smaller triangles. This would be acceptable.)
(9) 13
(10) 6

## TEACHER COMMENTARY

Skill of
Problem

1

Comment
This problem has students find the value of a collection of coins, and write it using the "\&" symbol. If children are having trouble with this, it might be that they aren't able to see the coins very cle.. 'y-start by having them find real coins that $100^{\prime}$ : exaclily like the pictured ones. At this point, they can find the value of the entire collection by counting (starting with the biggest values first) rather than adding. Or, they can solve this problem by adding the coin values on a calculator. There are 2 quarters, 2 dimes, 2 nickels and 2 pennies.

ANSWER: 82¢

This problem involves getting change from a purchase. Students should find the answer to this problem by counting the value of coins, to get from $82 \&$ up to $\$ 1$, rather than by subtracting.

ANSUER: 18́

The student is to fill in a . le, using the concept of greater than, less than, or equal to. In going over this problem with the students, note that some will have put "one more than" or "one less than" as the answer to the problems--perhaps they're reading in an extra condition--and others will have enjoyed putting in any answer that will work.

ANSWER: Any answers that result in true, line-by-line statements, are acceptable.

Making a bar graph is the skill covered in this problem. In your small-group session, do just one of the names is an example, and allow them to finish it later.

ANSWER:

"Elapsed time" is being covered in this problem. Nost students will recognize $8 o^{\prime} \mathrm{clock}$, Lut some might have trouble with $120^{\prime} \mathrm{clock}$ since the 2 hands are together on the clock. Use a clock with moveable hands, and actually rotate the hour hand from 8 io 12, to show those children having difficulty.

ANSWER: 4 hours
"Estimating linear measurement" is the skill being covered in this problem. The student might measure the snake with a ruler, without going "around the curves," and get length of about $81 / 2 \mathrm{~cm}$. If the student follows the snake's body, either with a ruler or with a piece of string to be measured later, they will get a length of about $101 / 2-11 \mathrm{~cm}$. In either case, the answer that's closer than the others is 10 cm.

ANSUER: 10 cm . is closer.

This problem addresses the skill on visual discrimi-nation--the studert must observe closely to notice that tr? scale is balanced, and that the pans have 1 circle, and 2 squares.

Another area involved in finding the correct answer is that of "measuring mass." The student must realize that, since the scale balances with 1 ball vs. 2 squares, the ball must be heavier than the squares. If children have trouble understanding this concept, discuss with them a see-saw in which 2 small kids are on one end, and a bigkid on the other. Which is heavier, the one big kid or the two smaller ones?

ANSWER:

TEACHER COMMENTARY

Skill of
Problem
1

21050

Students are being introduced to theconcept of area. In the small-group session, stress the term unit square, and introduce the word "area" informally as "the number of unit squares present."

Point out to the students how this problem is different from problem 1 since we're talking just about unit squares. Challenge them by asking "how many squares altogether, unit squares and bigger ones also, can you find in the first shape?" (5)

ANSWERS: 4, 6, 7 and 19

Numbers that do not belong in a barrel34, 29, 31

You might even get more concrete than this by placing
glasses on top of a number line with removable numb-
bers, and physically move some of the numbers to the
You might even get more concrete than this by placing
glasses on top of a number line with removable numb-
bers, and physically move some of the numbers to the
You might even get more concrete than this by placing
glasses on top of a number line with removable numb-
bers, and physically move some of the numbers to the right glass.


This problem involves using the concept of inequalities. You might show them a large number line, and mark off on the number line where each barrel would be:


Students are to solve this problem through visual discrimination. They should notice clues such as the sun shining with the boy stretching, the moon, the clock showing 5 o' clock, etc.

ANSWER:

$\square \quad 6$
$\square \quad 3$
$\qquad$ $\square 4$

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1001 | This problem requires multi-step computation. The computation involves adding two numbers and then subtracting to arrive at the answer. The child may solve the problem by crossing out 3 bags, 7 bags and counting the remaining bags. Give several similar problems in the small-group session. <br> ANSWER: 10 |
| 2 | 1003 | This problem is designed to have students solve a problem by drawing a diagram, and then counting to find the answer. <br> ANSWER: 8 |
| 3 | 1050 | The intention of this item is to have children solve a computaitional puzzle for whole numbers that demonstrates an understanding of computational principles. Hopefully students in the problem-solving session will notice that different answers are all correct, and conjecture that perhaps any number will work. (Any number will work, since you're adding 4 and subtracting 4.) |
|  |  | This problem also uses a flowchart--some children might still need practice on this, even though it was introduced in worksheets I and VI. <br> ANSWER: Any number |
| 4,5 | 1022 | These items require the interpretation of information from a chart. |
|  |  | ANSWERS: 4. March <br> 5. April |

ANSWER:


The child may choose to use repeated addition to arrive at the answer, or count by two's, four times. For students having trouble, demonstrate the problem using 2-liter cola bottles and a large container. Do several pouring problems similar to, but not exactly like, this one.

ANSUER: 8

This problem requires the student to understand basic computational principles to fill-in the circles. This could be solved by the "guess-check-revise" method. Most students will remember that they did a similar problem a few worksheets back.

ANSWER: ... Accept any arrangement
 just so the numbers in opposite circles total 10.

21128 The student must determine the relative mass of two objects on the balance scale. For students having trouble, have a pan balance available for experimenration.

ANSWER: A. tiger

This problem involves elapsed time.
ANSWER: 10:00 A.M.

4
1108
The concept of lines of symmetry is introduced in this problem. For the small-group session, have a large number of other shapes for students to consider.

Ai:SWER: heart (first figure only)

This item provides reinforcement in estimation. Students can decide by making 9 path out of string from Susan's to George's house. The string will have to be used twice to get from George's house to Barry's.

ANSWER: B. about 4 meters
$6 \quad 1170 \quad$ The student should use a calculator for this problem.
ANSWER: 8
$7 \quad 1166$
This problem is designed to help a student follow the logic of a flowchart. For the small-group session, have some $3 \times 5$ cards with steps on them for similar situations, like: Eating an apple.

Washing your dog.
Making the bed.
Getting dressed.
ANSWER: eat breakfast

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1009 | This word problem includes extraneous information (8 hats). |
|  |  | ANSWER: 14 |
| 2 | 1009 | This problem also involves extraneous information (the yo-yo). Computation uses column addition of 2-digit numerals with no regroupings; students can use a calculator if they want to. |
|  |  | ANSWER: 88\% |
| 3 | 1035 | The student must use his personal knowledge of measurement to give a reasonable response. Computation or estimation will not help the student derive an answer. In the small-group session, have models of the metric units given, and let them discuss which makes sense to use here. |
|  |  | ANSWER: meters |
| 4 | -- | This word problem iequires the student to read carefully. Hopefully such problems will encourage them to think about each protilem, rather than to rely on "key words." |
|  |  | ANSWER: 1 |
| 5 | -- | This problem involves the equality symbol in a way that might be new to students. Previously, "=" seemed to mean "do something," as in "7+2=?." But now it means "what's on the left is the same as what's on the right, mathematically-speaking." |
|  |  | ANSWER: True |

The student must apply the concept of measuring elapsed time given in a real-world problem situation. ANSWER: 4:30 P.M.

71145

8
1168

The student must be able to read and interpret a table in this problem.

ANSWER: A) 8
B) Purple
C) Red

A calculator should be used to perform this computation, at the first grade level.

ANSNER: 5537
LESS

TEACHER COMMENTARY

1 Excellence

1002

1001

1125

1005

## Comment

This problem introduces the problem-solving strategy of "making a list." In the problem-solving session, have students do the same problem, with different digits.

ANSWER: 9

The two parts of this problem, when taken together, lay the foundation for a multi-step word problem.

ANSUER: \$7 and \$2

Measuring length is the essence of this problem. If students are having trouble, it's possibly because they don't know to place the end of the ruler--or the "zero" mark--next to one end of the pencil. It might also be that they're trying to use a ruler that's too complicuted for them--i.e., one that has too many divisions, other than centimaters-indicated on the ruler.

ANSWER: (C) 10 cm

This puzzle requires some computational ingenuity for a 1st grade student. Most of the students who solve it will start on the top line, where they already know 2 of the 3 numbers whose sum is 11; they will get the 3rd number either by subtraction (working backwards) or by guess-check-revise. Once they know this number, they can then get the botton, middle number in similar fashion, and they're then on their way!

In the small-group session, give them this problem to show the technique:

| 6 |  | 2 | $=16$ |
| :---: | :---: | :---: | :---: |
|  | 4 |  | $=16$ |
|  |  | 5 | $=16$ |
| 16 | 16 | 16 |  |

ANSWER:


Numeration--is being reinforced in this problem. The difificult part for students is that the groups of ten are not al ready ordered to the left of the ones. This is different from the typical textbook situation. Have similar problems to these in your small group session, but with real manipulatives.

ANSWERS: 43 and 58

Fundamental geometric figures--in this case, angles-are being reinforced in this problem. In the smallgroup session, use figures other than a hexagon to show this concept.

ANSWER: 6

This problem is similar to problem 3 above, in that it has the student deal with measuring length.

ANSWER: Make or mark off a $10-\mathrm{cm}$ length, to use in checking the answer.

The student is to collect and record data related to a probability experiment in this problem. In the small-group session, go over the experiment twice as a group, actually flipping a coin and recording the data, and making the concluding statement. Stress that they'll probably all get different answers on their own, just as you get doing it twice in a group.

ANSNER: The answer should match the data the child collects.

TEACHER COMMENTARY
Skill of
Problem
1 Excellence

## Comment

This is a simple counting problem, and hence not directly related to one of the skills of excellence. However, in discussing the results with children, lay an intuitive foundation for multiplication of whole numbers by saying:
"Look, there are 5 groups, with 4 in each group. How many will that be altogether?"
"There are also 4 groups when you look at it another way, with 5 in each group."

ANSWER: 20 (pennies)

This problem lays the foundation for division of whole numbers--for a child to solve it, they could make use of skill 1003 (drawing a diagram). They might circle groups of 7 pennies till they don't have enough left to buy another pencil. Or they might actually take 20 pennies and remove them 1 at a time, replacing them with a pencil, as far as they can.

ANSWER: 2

This problem must follow the one above it in sequence, for the cilild to be successful. For any that are, the foundation is being laid for multi-step word problems. If they drew a diagram as described above for $\% 3$, they could merely count the pennies not circled, to find this answer. Note: You might mention addition and subtraction here, for those who know it, but don't emphasize tinese operations as much as the counting method.

ANSWER: 6

This problem involves the sort of real-world situation the child would meet every day, and hence reinforces managing personal income.

ANSWER: wagon and frisbee

6 -- This problem is straight computation, and does not directly support one of the skills under the standards of excellence.

ANSWER: See child's worksheet

## TEACHEF. COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1146 | For students having trouble with this cartesian coordinate problem, have them make some pretend trips with their fingers. The first number always tells how far to the right (or East, in this problem) to go; tihe second number tells how far up to go (or, to the North). |
|  |  | ANSWER: <br> B = Blue <br> $\mathrm{G}=\mathrm{Green}$ <br> R = Red |
| 2 | 1124 | This problem involves simply reading a thermometer, and the readings are both positive numbers and do not require interpreting "between visible numbers." Because of future problems, however, take the opportunity (in your small-group session) to expand the problem to readings like $25^{\circ}, 45^{\circ}$, etc., and even $-10^{\circ}$. |

ANSWER: $10^{\circ} \mathrm{C}, 50^{\circ} \mathrm{C}$

Students are asked to interpret information from a bar giaph in this exercise. In your small-group session, you could have a similar graph made for your particular class, and discuss these same sorts of questions.

ANSWER: 5, 3, 4

TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | -- | "Rounding off" is a skill that is being introduced in this problem, in the form of "closer to." |
|  |  | ANSWER: Shoes |
| 2 | -- | There are a large number of correct answers to this problem. In the small-group session, you might offer an extra star to the one who finds the me t. number of sums to ten. (If you do so, limit the ch.ldren to using number pairs that are adjacer: ). |
|  |  | ANSHERS: <br> These are just a few of the combinations +otaling ten. |
| 3 | $\begin{aligned} & 1074 \\ & 1004 \\ & 1005 \end{aligned}$ | Solving an al gebraic equation is being intuitively introduced in this problem. Students might solve it by "guess-check-revise," or by "working backward" if they know to subtract 8 from 12. |
|  |  | ANSWER: 4 |
| 4 | 1007 | Numeric and geometric patterning are being reinforced in this problem. Most students will see the pattern as $2,2,3,3$,_,_, $5,5,6,6$, but a few might see it as 4, $\qquad$ ,10,12. |
|  |  | ANSWER: |
|  |  | $\bullet \bullet$ $\bullet$ <br> $\bullet \bullet$ $\bullet \bullet$ |

"Vertex" (pl: vertices) is a topological term being introduced intuitively at this time. You might extend the meaning, and make a distinction between "vertex" and "angle," in the smell-group session by looking at networks like and counting the vertices.
(All corners are considered vertices of a network, but there are some vertices that are not located at cornets.)

ANSWER:


Students can go through problems similar to this one in the small-group session, as an introduction to addition of 2-digit numerals without regrouping.

ANSWER: 59

7 --
Students might solve this by drawing the paths they could take. In the small-group session, extend the idea to a situation like:


| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1001 | The foundation is being laid in this problem for a two-step word problem. The student should think of putting together the ducks and bunnies, and then removing 1 animal. In the small-group session, go over this process with different objects and different numbers, acting out the physical movement. |
|  |  | ANSWER: 4 |
| 2 | $\begin{aligned} & 1004 \\ & 1005 \end{aligned}$ | This problem is set-up to encourage "working backwards" mentally. The students can figure "to wind up with 2 after subtrocting 7 I had to have 9 as an intermediate step. So I needed to have 9, after I added 6. So I needed to start with 3." |
|  |  | A student might also find the answer by simply guessing the missing number, and checking to see if they get 2 as the answer. If not, they revise the guess; this process is continued till they are successful. |
|  |  | Go over similar, but not exactly the same, problems in the small-group session. |
|  |  | ANSWER: 3 |
| 3 | 1017 | Have students practice counting various coin collections like this one. They should start with the largest coin value ( 25 f in this case) and add on the next lowest value, etc... Here they would count: |
|  |  | 25¢, 35¢, 40¢, 45¢. |
|  |  | Note that students do not have to add to find the answer, although this is acceptable. |
|  |  | ANSWER: 45\% |
| 4 | 1051 | The student is being introduced to the concept of a fraction being larger than another fraction, in this problem. |
|  |  | ANSWER: B |

Students will usually solve this problem by counting (possibly on their fingers) rather than by adding 7+7. If they have trouble, they can use a calendar and touch the days with their fingers.

ANSWER: 14

A number pattern is involved in this problem - counting by 5 's starting with 3 . Have students experiment with this sort of patterning in the small-group session, starting with various numbers (other than 3), and counting with numbers other than 5 . Have them use a number line to make jumps of a certain size.

ANSWERS: 13, 23

This problem is a simple, one-step word problem. The addition involves three 2-digit numbers, without regrouping.

AMSWER: 39¢

8
1003
Students have seen a similar problem to this one, on worksheet XV. They will likely solve it by drawing the paths, and counting them.

ANSWER: 6

## TEACHER COMMENTARY



# The student is asked to use an alternative method to compute these sums (other than paper-and-pencil). Have them practice such problems together in the small-group session, and perhaps give them a teachermade practice sheet for overnight drill. 

When they turn in their paper, give them this problem which is taped to the table or desk and watch to be sure they don't count on their fingers, or on the desk top, or whatever. They get credit only far doing it mentally.

Problem: 8
6
7
4
$+2$
ANSWER: 27

## TEACHER COMMENTARY

 figure; you might intuitively introduce this terminology in the small-group session. Some students will not be able to visualize the entire set of cubes needed since some aren't visible--such students need to take other 2-dimensional drawings similar to this one, and try to get the answer, and then actually build the figure to see if they are correct.

ANSWER: 8

Students will also solve this via "guess-checkrevise."

ANSWER: 8

| 8 | 2 |  |
| :--- | :--- | :--- |
| 3 | 7 | (any order) |
| 4 | 6 |  |

This is a simple, comparison-of-sets interpretation of subtraction.

ANSWER: 3

Students are to answer these 3 problems based on their own knowledge about the cost of common items. They should reason along the line of "I know a new dress won't cost as little as 24f, but it might cost \$24, so $\$$ is the correct symbol to use." Go over similar problems in the small-group session, using objects familiar to the students (bikes, candy bars, etc.).

Note also that students might put "\$" to the right of the numeral, as they would " $f$," and to go along with the way it's read. This is a common mistake, based on a logical choice by the child.

ANSWER: (A) \$
(B) $A$
(C)

## TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1007 | Geometric patterniny is presented in this problem. |
|  |  | ANSWER: |
| 2 | 1050 | Listing all the sums of 5 , including those with "commuted addends," makes this a computational puzzle. In the small-group session, list all the families for several numbers other than 4 and 5. You might even ask for them to notice a pattern to the number of family members (one more than the number itself). |
|  |  | ANSWER: $3+2,2+3,4+1,1+4,0+5,5+0$ (in any order) |
| 3 | 1125 | Students are asked to measure the length of a pencil, using a non-standard unit. Do similar problems using other non-standard units in the small-group session, ensuring that students always start at one end of the object being measured, and get the closest possible whole number of unit lengths. |
|  |  | ANSWER: 5 |
| 4 | 1007 | This problam involves a numerical pattern. |
|  |  | ANSWER: |
| 5 | 1007 | Numerical patterning is also in this problem, but in a more difficult form since the numbers "bridge decade." |
|  |  | ANSWER: 30, 29, 28, 27 |
| 6 | 1170 | Practice in reading a digital display is provided in this problem. |
|  |  | AMSWER: 134 |

Students are asked to read and interpret a pictograph In this problem. In the sma!l-group session, get more mileage from the problem by asking other questions, such as:

Who ate the least?
How many more did the squirrel eat than the monkey? If Suzie fed those 3 animals from a bag of 20 peanuts, how many would she have left?

ANSWER: Squirrel

81036
This problem provides practice in estimating measurement. The student needs to estimate the area of this sheet of paper using a non-standard element. You may let the students trace the card to help them get the idea of area and measuring, or take out an actual deck of cards and lay them down on the paper to get the concept of "covering."

ANSWER: 8, 9, or 10 cards would be acceptable.

TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1147 | Students make a pictograph using "smiling faces." In the small-group session, you might have them make another type of pictograph, given similar directions. You might also extend the lesson by asking questions (after a pictograph is made) like "who has the most?," "How many more .......," etc. |
|  |  | ANSMER: $\square$ |
| 2 | 1110 | "Traceability" of networks is introduced in this problem from topology. The network on the left is "traceable" if you start where the "roof" meets the "wall." The other network is not traceable. |
|  |  | In the small-group session, have students consider similar (simple) networks, trying simply by tracing to see if they are traceable or not. Later they'1\% learn another method. <br> ANSWER: a. |
|  |  |  |
| 3 | 1126 | The concept of area is reinforced in this problem. This is the first place students will use a standard unit (square centimeter) to find the area. |
|  |  | In the small-group session, have students find the area of similar shapes, and report the area in square centimeters. |
|  |  | ANSHER: 8 (centimeters) |

In the small-group session, have students do this experiment as a group, recording the information on the chalkboard. This problem lays the foundation for an important probability skill--collecting and recording data--so be sure the students roll the die "fairly," and discuss what would happen over time if a large sample of data were collected.

ANSWER: Count to be sure there are 20 tally marks altogether.

An important part of this problem is for the student to draw a sketch to match the verbal situation. The drawing should show 3 students, with 6 new shoes, und one having a belt--stick figures or other brief sketches are preferred, but the correct number of people, shoes, and belts is necessary. The students can then count and find the answer.

ANSWER: 7 (Note: An answer of 4 should al so be accepted--the student was likely counting a pair of shoes as "one thing." Give them credit!)

Some students will find the answer to this problem by counting, but they' 11 have to count things that aren't visible. Or they might reason along the lines of "four tires on each car, and $4+4=8$, so he will need eight tires."

In the small-group session, give similar problems using bikes, big wheels, skates, etc.

ANSWER: 8 (or 10, counting the spares)

| Problem | Skill of <br> Excellence |
| :---: | :---: |
| 1 | 1006 |

Comment
Students will probably have a hard time deciding visually which of the 2 larger figurcs do not fit in the box. They can decide by tracing each one, and manipulating the tracing overlaid on the box.

ANSWER: The figure closest to the box will not fit.

This problem simply provides practice in writing a coin collection using "dollars and cents" notation. Similar problems can be considered in the smail-group session.

ANSWER: \$1.15

There are two aspects to this problem that will likely give students trouble. First, they are used to "doing something" with problems like "9+6" and "20-5," and not comparing them as expressions. The equal sign, in particular, is frequently interpreted as an action-item because that's what children do when their only exposure is in exercises like "7+4=."

Secondly, the symbols > and < are difficult for students to learn and distinguish. A hint like "It's the same symbol, but can be turned always so the large opening is next to the larger number" might help. Practice with similar problems in the small-group session should benefit the students measurably.

ANSWER: =

The purpose of this problem is to help distinguish which students have developed an awareness of the cost of familiar items. The only part students might confuse is "a computer" with a calculator. In the small-group session, be sure the students understand the difference.

ANSWERS: A toy car.
A coloring book.
A small teddy bear.

Students should be encouraged to look for triangles sion, go over similar problems, using overlapping rectangles and squares.

ANSWER: 3

In the small-group session, have some nennies and have each child actually divide up a group, saying "one for you, and one for me, etc." Then they label their collection as "even" or "odd."

ANSWERS: even odd
odd even

71036
Students should use the R-foot length of the car (bumper to bumper) in arriving at a reasonable answer as to its height. The height is either about the same as the length, or obviously greater or less than the length. In the small-group session, take some common objects and do similar problems.

ANSWER: B

TEACHER COMMENTARY

| Problem | Skili of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1003 | There are two different problems in this exercise: the first one involves the union of two sets (boys and girls- $-9+\epsilon=$ ?) and the second is "comparison of sets"--(9-6 =?). |
|  |  | The second part of the problem is more difficult than the first part, because "comparison of sets" is frequently not covered in elementary textbooks until a child sees them in a word problem, such as this one. If children are having trouble with this problem, have them draw a diagram, as shown to the right, and do a "one-to-one" matching of boys and girls, counting the "extra boys." |
|  |  | ANSWERS: 15, 3 |
| 2 | 1006 | This problem is ususally solved via counting, but it does involve visual discrimination to some degree. The fourth question intuitively uses "more than," a sub-skill for skills that involve > and <. <br> ANSWERS: 10, 4, 6, girls, 5, 5, girls |
| 3 | 1168 | Use of a calculator is the skill reinforced in this problem. |
|  |  | ANSWER: 15 |
| 4 | 1072 | Numeration skills are reinforced in this problem. The unusual part of the situation is that the tens and ones are not "lined up" from left-to-right as in most textbook situations. The student has to re-order the values shown, before writing the number. In your small-group session, give similar problems, but with real manipulative objects. |
|  |  | ANSWER: 86; 34; 75 |

"Estimating costs" is covered in this problem. "Less than" is also introduced, with money.

ANSWERS: The watch has a red ring around it. Everything else, except the turtle, has a blue ring.

## TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1007 | This problem invol ves a numeric pattern--counting by tens, but starting at a starting point other than zero. In the small-group session, have students practice counting forward (and perhaps even backward) orally, in similar problems. |
|  |  | ANSWER: 16, $26,36,46,56,66,76,86$ |
| 2 | $\begin{aligned} & 1005 \\ & 1050 \end{aligned}$ | This is a puzzle that requires the student to demonstrate understanding of, and ingenuity with, computational principles. The student must work backwards to determine some answers. |
|  |  | $\text { ANSMERS: } 10$ |
|  |  | 624 |
|  |  | 4 1 3 |
| 3 | 1107 | This problem is simple recognition of triangular shapes. |
|  |  | ANSWER: Hat, nose, arms and legs |
| 4 | 1019 | This problem requires the child to determine the change he will receive from an amount of money after making a purchase. You might suggest that the child try to use the "count-back" method of determining change, in a small-group session, with similar prob1 ems. |
|  |  | $\begin{array}{lr} \text { ANSWERS: } & 2 \downarrow \\ & 5 \ell \\ & 10 \ell \end{array}$ |
| 5 | 1167 | Have students do a problem similar to this one in the small-group session, but with a different code. |
|  |  | ANSWER: 24 in last square. |

TEACHER COMMENTARY
Skill of

1 Excellence 1002

2
1073

1074

41145
1149

Comment
This problem is similar to problems presented on worksheets II and III, but here the student is not given the chart to fill in. In the small-group session, help start such a chart for those who need a refresher.

ANSWER: 6

Students have a problem similar to a previous problem on worksheet XXI. Perhaps those who had trouble with it before will have internalized now the difference between "even" and "odd."

AMSWERS: odd odd
even

Have a number of similar problems on the board, with square pieces of paper taped over the number students are to find. After they try, they can check by removing the paper. For those having trouble, have them make up some subtraction problems in horizontal form like this, cover the second number with paper, and give it to another student to solve.

ANSHER: 7

The student is to interpret the information on tise graph to the effect that the puppy's weight is increasing about 5 kg ./month. Then the student predicts that the weight in May will be about 25 kg ., and completes the bar graph. You may wish to discuss the kind of puppies which would have this increase in weight.

ANSWER: The bar over May should go up to about 25 on the vertical axis.

The student should reason that the answer is acceptable, since $5+7=12$. Some students might think the answer is wrong since they don't see 12.00 on the display. In the small-group session, show with several calculators how the display usually doesn't show zeros to the right of the decimal point, unless there are al so non-zero digits there too.

ANSWER: C
$6 \quad 1005$
This problem is similar to a previous problem on worksheet XIII. Students who were unsuccessful therefore have another chance to succeed.

ANSWER:


TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1001 | In your small-group session, simply ask the children if they forgot to count the "mama" dog and cat. |
|  |  | ANSWER: 7 |
| 2 | 1146 |  |
|  |  | In your small-group session, have a couple of additional pictures cut out and place them on the grid so students can find their locations. Tell them that they should always tell how far right to go first, since people have agreed down through the ages to do that. |
|  |  | For those having trouble, have them "walk" with their fingers. |
|  |  | ANSWER: Baseball 1,3 |
|  |  | Raccoon 4,3 |
|  |  | Fish 2,1 |
|  |  |  |
| 3 | -- |  |
|  |  | the notion of probability. You should actually bring |
|  |  | in a sack of collipops (or balloons) and go through the experiment. (Be sure the objects that go in the |
|  |  | sack are identical, except for color.) If you introduce numbers into the problem, have them read $9 / 14$ |
|  |  | as "nine out of fourteen" instead of as "nine fourteenths." |
|  |  | ANSWER: Cherry |

ANSWER: 7 days


In class, ask similar questions to those on the worksheet. (Since students can't yet multiply, they can determine the number of games won by each team via "counting by two's.")

ANSWERS: 2
4
2

# TEACHER COMMENTARY 

FOR

## GRADE 2 WORKSHEETS

## TEACHER COMNENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1073 | Several times in the Grade 1 worksheets, students considered "odd vs. even" by deciding if they could divide a collection exactly with a friend, with none left over. You might remind them of this method in your small-group session. Take an even number of pennies and go through the stacking method, and then an odd number. |
|  |  | ANSWER:14 even  <br> 15 odd  <br> 16 even  <br>  17 odd <br> 22 even  <br>  25 odd |
| 2 | 1006 | You might suggest that turning a picture will sometimes reveal hidden figures. |
|  |  | ANSWER: The lady's face is under the man's outstretched (right) arm. |
| 3 | $\begin{aligned} & 1001 \\ & 1003 \end{aligned}$ | Some students might need to draw a sketch of the 4 animals, and count to find the answer. (In your small-group session, suggest this is always a good way to start a problem you don't understand.) Others might try to count the legs on the pictured frog twice, and insect twice - if so, they might have trouble with the hidden legs on the insect. Still others will add $6+6=12$, and $4+4=8$, and $12+8$ $=20$, to get the answer. |

ANSUER: 20

41168
In your small-group session, have the students just add $1+2+3+4+5$ on their calculators, and then finish the problem at home.

ANSUER: 55

In your small-group session, discuss what the graph means, and ask leading questions to be sure they are interpreting it correctly (e.g.-how much did Janet weigh in January?). Watch for students who aren't familiar with abbreviations of the months, or who have trouble "lining up the top of a bar" with the weight it represents. Then have the group discuss how the graph goes up by 1 pound each month, and have them draw in the bar for june, finishing July and August at home.

ANSWER: The bars for June, July, and August should go to 45, 46, and 47, respectively.

TEACHER COMMENTARY

Skill of
Problem
1

21168
1002
1003

The purpose of this problem is to give students experience using a calculator for computational problems that would be difficult for them otherwise. These are addition and subtraction problems, so the concepts should be familiar to second graders. But the exercises involve several digits, and "carrying" and "borrowing." The last problem might give children trouble since the addition key has to be pressed twice, but only one such sign is shown for the problem. In your small-group session, go over at least one exercise similar to this last one.

ANSWERS: 559, 850, 1272

1110 This problem is from a new, emerging area of geometry called "topology." Your students might be interested in knowing that the fact that any map can be colored in 4 or fewer colors was once one of the 50 famous unsolved problems of mathematics-- it was finally verified in 1976 by a computer program that ran for over an hour!

One solution is shown below--each solution will be different, though, so you can show a solution in the small-group session without worrying about giving the children too much assistance. (Note: this problem can also be solved by coloring around the outside of the map, but most children will not think of trying this.)

ANSWER: To check this on a child's paper, first glance to see if more than 4 colors were used. If not, then proceed to look over the map, starting with the smallest states where it's more difficult, and moving toward the west and south.


Students are given a realistic situation for this problem setting. In your small-group session, take a similar but simpler problem--make one up using the toys shown, but with smaller prices attached, and have Maria get a dime from the fairy. Have the students solve the simpler problem in class, and tell them that the concept is the same if they want to solve the given problem at home.

ANSWER: Fish
$5 \quad 1003$

6
1003
The student is to use the diagram above to solve the given problem.

ANSWER: 7
Students are asked to draw a diagram to represent this "comparison of sets" subtraction situation. The 15 envelopes they draw should have stamps in the upper right hand corner of 8 of them--give credit if the stamps are anywhere on the envelope, however.

ANSWER:
 $\square$ $\square$ $\square$ $\square$ $\square$ $\square$

| Problem | Skill of Excellence | Corment |
| :---: | :---: | :---: |
| 1 | $\begin{aligned} & 1050 \\ & 1004 \\ & 1003 \end{aligned}$ | This is a computational puzzle that requires ingenuity to solve. Students will probably solve it by logical deduction, combined either with "guess-checkrevise" or "working backwards," to get the individual digits. |
|  |  | ANSWER: 3,5 |
| 2,3,4 | $\begin{aligned} & 1144 \\ & 1154 \end{aligned}$ | These problems all involve getting information from a pictograph. Problem 2 is simply reading the pictograph correctly, but Problem 3 involves the concept of "comparison of sets," a fundamental interpretation of subtraction (al though students will probably solve it without subtraction). Problem 4 introduces the underlying concept of the average, although this terminology is not used. Many students will solve this simply by visualizing the softballs being "moved around" on the chart--you might show this to children who have t.-ouble seeing it, on a similar problem. <br> ANSWER: 4, Pirates, 3 |
| 5 | 1001 | Division, with a remainder, is introduced in this word problem. The student will probably solve it by counting 9's, till he or she gets to 25. They yill then be on their 3rd group of markers. Go over a similar problem in the small-group session. <br> ANSWER: 3 |
| 6 | $\begin{aligned} & 1006 \\ & 1128 \end{aligned}$ | Studenis should apply visual skills in seeing that the scale is balanced, which means the total weight on the 2 ends is the same. Then they should know intuitively that, if 3 circles weigh the same as 2 squares, then a has to be heavier chan a . If they have trouble with this, relate the situation to a "see-saw" with three 1st graders balancing two 3rd graders. |
|  |  | ANSWER: |

1018 Students have to add the amounts given, to find the total sale price, and then find the amount of tax from the chart. Notice that they are not asked to add the two together. This problem concentrates on the tax itself. To emphasize this, you might discuss briefly with the students what sorts of things our tax money does for us (building roads, schools, etc.).

ANSWER: \$.04 should be circled
$8 \quad 1002$
Hopefully students will solve this problem by "making a list." The otiner numbers are: 91, 82, 28, 73, 37, 46, 64, and 55.

ANSWER: 8

This problem involves extraneous inf:rmation and will later be solved by several computational steps-multiplication and division. At this point, since students 'iave not yet met multiplication or division, they can solve it either concretely or by drawing pictures of the candy, and dividing it up in the manner "one piece for $m$, one for you, etc..."

ANSWER: 12
$10 \quad 10{ }^{7}$
This problem involves a visual pattern, moving from left-to-right.

ANSWER: A square that's divided into 16 smaller squares.

## Comment

This problem lays the foundation for a multi-step word problem, in that students find the answer to two "sub-problems," and then combine these answers to answer the third part.

One difficulty might be in counting the legs of the animals, if the legs aren't visible. Another interesting point will come up in that some children will say that chickens have ears, and some will that chickens don't have ears. (It all depends on the way you define "ears"--chickens don't have external ears, but they do have internal ears, else they couldn't hear themselves.) So the answers to the last two parts will vary, depending on the child's viewpoint.

ANSWERS: 18 legs
8 (or 10) ears
10 (or 8) more legs than ears

The student should be encouraged to think of 55 d as "a little more than 50\&." Since five $50 \%$ pieces would be $\$ 2.50$, five times 55 would be a little more than $\$ 2.50$. Therefore, five school lunches would be closer to $\$ 3$ than to any other choice.

ANSWER: \$3

31002
The student should solve this problem by "making a list." They then count to find the answer to the problem. (Last year they had similar problems, but without street names, so they probably sol ved them by tracing all the paths.) Go over a similar problem in the small-group session.

ANSWER: 6 ways (Monroe, Green)
(Monroe, Milton)
(Monroe, High)
(Adams, Green)
(Adams, Milton)
(Adams, High)

This is a computational puzzle that requires some ingenuity. Most students will initially start it by "guess-check-revise," and gradually refine their guesses. Several answers are possible, so look for commonalities among the students that are successful in the small-group session ( dm of the corner points, e.g.).

ANSWER: (one answer)


This problem reinforces the term "triangle" and it also involves visual discrimination. Students can be encouraged to solve such problems in the following manner:

Look for the smallest triangles and count them first. Find the next largest triangle, and see how many of them you can find.
Go to the next largest, and do the same.
Continue this until you've gotten to the largest you can find.

In this case, there are 9 small triangles like: A There are 3 of the next largest, like:
Finally, there is 1 of the largest possible size, like:


ANSWER: 13

This problem reinforces the skill of reading a time schedule, in a real world situation.

ANSWER: Tuesday and Thursday for PE 3 hours doing math Thursday from 1:00 till 2:00 (movie)

TEACHER COMMENTARY

Skill of
Problem

1

2
1001
1019

Comment
This p.oblem is a sequential geometric pattern. The student should notice that each shape gives two large figures and a small one--and two capital letters and a small letter.

ANSWER: (the first shape on the left)

This is a multi-step word problem that involves getting change after a purchase. The student will probably add 19f and 20\&, and subtract that total from 49\& to get the change. Note that a real concrete way to solve the problem would be to mark out a dime, nickel, and four pennies for the cupcake, and two more dimes for the ice cream. Then look at what's left in the pile.

ANSWER: $\quad 04$

Students might solve this by "guess-check-revise" by guessing pairs of numbers with sum 28, and checking to see if the difference is 6 , and revising the guess each time. Or the student might be encouraged to actually make a list of the numbers that sum to 28--0 \& 28; 1\&27; $2 \& 26$; etc.--till they find a pair that has a difference of 16 . Go over similar problems in the small-group session.

ANSWER: 17, 11 (in either order)

1007 This problem offers another experience in solving a geometric patterning problem. The student would notice that the outside figure "adds a side" each time, the inner arrow rotates counterclockwise, and the small, central figure "subtracts a side" each time.

ANSWER:


Students will be exposed to an underlying theme of probability in this exnerience with the pigs, that of the ratio of a subset, to the set itself.

```
ANSWER: }2\mathrm{ out of 5 have spots
    3 out of 5 have curly tails
```

Students have a chance to consider intuitively the concept of constructing a perpendicular to a line, at a given point on the line, in this problem. Students must understand that, in folding the sheet of paper, they have to be sure that one side of the line segment "falls on top of" the other side of the line segment.

In your small-group session, have them do this process using other lines made on other sheets of paper. You might intuitively introduce "perpendicular lines" at this time.

ANSWER:


Students have a chance to show that they can subtract mentally in this problem. In teaching them how to do this, notice that the problems selected for practice are ones where the minuend is very close to a number that is easy to subtract--students should be encouraged to "adjust" the given problem by adding the same number to the top that they add to the bottom to get this easy number, and then subtract mentally. In your small-group session, go over similar problems for practice. When they turn in their paper, give them this problem, and check to be sure that they do it mentally:

345
$-199$
Note: At a later time (a few weeks) you might review this briefly, and eventually show them how to do a similar thing with addition. However, with addition, they'll have to adjust the two addends in opposite directions to compensate. So be careful when you do this--students who are successful with it will have developed a real "feel for numbers."

ANSWER: 146

TEACHER COMMENTARY

Skill of
Problem
1

## Excellence

1164

## Comment

The Cartesian Coordinate system is introduced in this problem setting. It's important for the students to realize that you go to the right first, and then up, to ? ocate points. This is simply convention.

For students having trouble, have them trace the path with their finger. Have them locate points other than the boat, church, pool, and bridge, in the small-group session.

ANSWER: 5, 2 (The church can be distinguished because of the cross on the top.)

$$
\begin{aligned}
& 2,1 \\
& 3,4
\end{aligned}
$$

1109
1006
The student has to know what "triangle" means in this setting, and also know that there are "overlapping" triangles in the drawing. The problem therefore reenforces visual discrimination also.

ANSWER: 28


31004
1005
This problem might be solved by "guess-check-revise." If so, the student will simply guess digits for each box, till they get ones that "work." Or, the student might "work backwards" by turning the subtraction situation into an addition one. If so, they' ll search for the missing digits in this fashion: box $+2=5,4+2=$ box, etc. In the small-group session, have students make up a similar subtraction problem and cover some of the digits with squares of paper, and give the problem to another student to solve.

ANSWER: 365
$-43$
322

This problem allows students to show that they ca follow a mathematical flowchart that has a branch in it. The difficult part will be for students to realize that they must take different paths at the decision, depending on the answer to the decision. In a small-group session, have students take numbers other than 8 and 15, and trace their paths.

ANSUER: 11 when input number is 8 [bottom box] 12 when input number is 15 [top box]

The purpose of this problem is to have students measure the length of something that's not in a straight line. They can take a real piece of string and lay it down to match, and then measure the string, or do something similar to this. In the small-group session, just asking how they have already done it will help students who have no idea how to begin.

ANSHER: Accept an answer between 27 and 29 cm

Skill of
Problem

1
1017 1046

## Comment

This problem involves both recognizing the value of collectios. of coins and bills and the concepts of greater than and less than for real world situations. Students who are having trouble with this problem might take out real coins, and try to match the coin to the picture first. If they can do this correctly, it's just a matter of counting. Note that the bank with the most coins, is actually worth less than the other two.

ANSWER: The bank in the right should be circled. The center bank should be "X'd."

Students will probably solve this by finding the value in each bank--\$1.15, \$1.07, and \$1.35--and adding. Some might solve it by counting the coin values of all 3 put together. Students who got an incorrect answer through counting should be encouraged to work from the biggest coin values to the smallest--for those who got the wrong answer through adding, watch for misplaced decimal points as the problem.

ANSWER: \$3.57

Since the number of cookies that MOM had to start with is not involved in solving this problem, the problem involves "extraneous information."

ANSHER: $19(2+6+5+6=19)$

This problem has the student consider the concepts and symbolism for greater than, less than, and equal $\pm 0$ in expressions invoiving whole numbers. But the problem also extends to making a bar graph. If students miss the problem, check to be sure they have: 4 <'s 2 >'s $2=1 s$

In the small-group session, go over a similar set of problems written on the board, and quickly make the graph.

ANSWER:


Muber of symole

This problem gives students the chance to demonstrate that they have developed a "feel for numbers" in estimating. "10 inches" can't be correct, since the pencil is shorter than the width of the paper. Of the remaining choices, the student . 111 probably reason that "4 inches" would be about half the width of the paper, and the pencil is clearly more than half (for those that have a good concept of "half"). So "4 inches" isn't as good an answer as "7 inches." Go over similar problems in the small-group session, using the length of a sheet of paper as 12 inches, with various objects drawn so they can be easily compared lengthwise.

ANSWER: 7 inches

While this problem does not directly address one of the skills of excellence, it should be enjoyable for the students. In the small-group session, select one name (perhaps the principal's last name) and find its value.

ANSWERS: lake $=5+2+5+3=15$

$$
\text { brush }=2+7+8+7+4=28
$$

$$
\text { father }=3+2+8+4+3+7=27
$$

$$
\text { puppy }=7+8+7+7+9=38
$$

$$
\text { chain }=2+4+2+4+6=18
$$

| Problem | Skill of <br> Excellence | Comment |
| :---: | :---: | :--- |
| 1 | 1006 | Students need to begin this search in an organized <br> fashion, perhaps starting with the smallest size tri- <br> angles and moving up to larger ones. In your small- <br> group session, you might start and do a few "layers" <br> for them. |

AMSHER: 13

Students once again meet the concept of "area" in this problem. For the first time, however, they'll confront "half-squares." In the small-group session, have some cut-out unit squares and half-squares available, and make several figures and have students find their areas.

Do not stress "half" in counting, but rather use figures where the halves always fit together to make another whole unit square. In this manner, you can simply count all the whole squares, and then the halfsquares two-at-a-time, to find the total area. (You can avoid having to count by halves.)

ANSWER: 12
A few students will probably realize that you need to take one of the larger numbers, and put it with the smallest numbers to "balance things out." From that point, it's just "guess- iheck-revise."

ANSWER: Move 9 to the first circle.

In a small-group session, go over similar problems like "with two 6's, make a number bigger than 50."

ANSWER: 333
$5 \quad 1170$
Students need to be familiar with the keys on a calculator to solve this problem. They will learn that there are certain mathematical symbols (coma, $\$, \infty, \infty$ ) that do not appear on a calculator.

ANSWER: d

$1036 \quad$| In the small-group session, have some square deci- |
| :--- |
| meters cut out and have students measure several flat |
| surfaces that are not an exact number of unit squares. |
| This wiil force them to estimate the final answer of |
| their area, in square decimeters, using an intuitive |
| notion of rounding off as "closer to." |

ANSUER: 6 $\quad$| Students have the chance to begin dealing with alge- |
| :--- |
| braic notions in these problems. They can probably |
| find the answers by "guess-check-revise." The purpose |
| of this problem is not to practice computation, but |
| rather to get at the algebraic equality notion. Stu- |
| dents who are weak computationally should therefore |
| be encouraged to check their guesses on a calculator. |

TEACHER COMMENTARY

| Problems | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | $\begin{aligned} & 1001 \\ & 1003 \end{aligned}$ | This problem involves 2 steps. The student should add the apples on hand ( $12+8$ ) and subtract that total from 25 needed. Students can solve it by drawing a diagram. |
|  |  | ANSWER: 5 apples |
| 2 | 1003 | Students will almost naturally draw a diagram to solve this non-routine problem. In the small-group session, have students determine the total number for stairs 6 cubes high, or 7. |
|  |  | ANSMER: 15 cubes |
| 3,4 | 1022 | These two problems have students reading and interpreting information from a chart. In the small-group session, use the same chart, but ask different questions. |
|  |  | 3) Thursday <br> 4) Friday |
| 5 | 1050 | This computational puzzle is not difficult if students follow the steps in the order in which they are presented. Have them follow a similar set of directions for this same chart, in the small-group session. Try: |
|  |  | A) Two numbers whose sum is 4 <br> B) Two numbers whose sum is 6 <br> C) Two numbers whose sum is 17 <br> D) Two numbers whose sum is 12 |
|  |  | The answer to this similar problem is 6. ARSUER: 7 |

ANSWER:


71126

8
1050

The student is asked to identify an angle.

The student is asked to find the area of a figure, using a non-standard unit. Have them do similar problems in the small-group session.

ANSWER: 8

The student can solve these computational puzzles, with a little ingenuity. Have several problems like this on large sheets of paper, with the missing digit covered up. As a group, the students can try to guess the missing digits.

ANSWERS: 2; 6] [6; 1] ; 3] 7]
5

245

## TEACHER COMMENTARY



The student is to place the steps in a flowchart in a logical sequence. Have several other such "daily activity" sequences available for consideration.

ANSWER: 4
2
1
3

ANSWER: They are the same size.

81168
This problem gives kids a chance to use their calculators. Be sure to mention that the answer looks like the word "hi," and then mention that other words are frequently spelled out on calculators as "fun things." (Words like shell, Bob, Bells, etc.)

ANSWER: B

TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | $\begin{aligned} & 1009 \\ & 1003 \end{aligned}$ | The number of adults is extraneous information in this problem. Students who understand this, but can't recide what arithmetic to do, can draw a diagram to rind the answer. <br> ANSWER: 15 |
| 2 | $\begin{aligned} & 1018 \\ & 1009 \end{aligned}$ | Extraneous information - the cost of the rope and hat - is included in this word problem. Students also must add the tax to the total. <br> ANSWER: \$2.03 |
| 3 | $\begin{aligned} & 1035 \\ & 1037 \end{aligned}$ | The student must use his personal knowledge of m. . rement to give a reasonable response. Computation or estimation will not help the student derive an answer. <br> ANSWER: liters |
| 4 | 1009 | This problem also involves extraneous information the number of apples in the basket. Many students will assume you need to subtract 4 from 44 to get the answer. <br> ANSWER: 4 |
| 5 | 1078 | The student will have to compute the totals on both sides of the box, and then compare them, to decide on an answer. In the small group session, have students put similar problems on $3 \times 5$ cards for other students, with the correct answer hidden by tape. <br> ANSWER: > |

"Elapsed-time" is the essence of this problem situation. Students who have difficulty can consider similar problems on a clock with moveable hands.

ANSWER: 4:30

71145
"Reading and interpreting a table" is at the heart of this problem. Have students answer similar questions regarding this chari in the small-group session.

ANSWERS: Fran, 5, 5
$8 \quad 1168$
Notice that the $=$ has not been shown in this prob1 em , but it's necessary to push this key to finish the problem. Have some similar problems for the smallgroup sessions, ones whose answers spell common words like oil, shell, Bob, etc.

ANSWER: SELL

31031

## Comment

This problem reinforces the ability to use a table as an organizer for an appropriate problem situation. The student is to find all the ways to make 154 , using combinations of pennies, nickel s, and dimes. In your small-group session, you might take a similar problem, perhaps for 10\&, and show all the ways.

ANSWER: In any order, ihe student could show:

| 10 | 1 | 0 |
| ---: | ---: | ---: |
| 5 | 2 | 0 |
| 5 | 0 | 1 |
| 0 | 3 | 0 |
| 0 | 1 | 1 |

This problem involves reading the information in a chart, and applying it in a real-world situation. It also impinges on the skill of greater than, less than, and equal to. In your small-group session, consider similar questions using the same chart. Allow students to use a calculator if they need to.

ANSWER: B.

Measuring length is the skill being reinforced in this problem, but it also includes the skill of approximation since none of the lines turn out to be exactly a whole number of centimeters long. Students might have trouble with this if they're not lining up the " 0 " on the ruler, with the very end of the line segment, or if their ruler has a lot of "distracting" divisions within the major units of measure.

ANSWER: 2, 4, 7

Right-angles are introduced in this problem, and a practical way to test to see 'f an angle has $90^{\circ}$ is used. Have students do similar problems in your small-group session.

ANSWER: $A, C$, and $D$

This problem combires the concept of "perimeter" with that of measuring length. Have them find the perimeters of other triangles in your small-group session - watch for "lining up the ruler wrong" type mistakes.

ANSWER: 22 or 23 cm

This problem combines an intuitive notion about probability with predicting outcomes, given a trend that continues. If students have trouble understanding what the problem is all about, actually take a thumb tack, and drop it several times, and record the result using the given chart, and the tally system.

ANSWER: 2nd choice listed (more likely down)

The first problem in this set is necessary to lay the foundation for problems 2 and 3. The answer to this particular problem will vary, of course, but can be obtained by finding the value of the student's name from the top line of the page, and comparing it to the answer.

ANSWER: variable

21046

The purpose of this problem is to continue to intuitively introduce the concept of odd vs. even numbers. You might ask them a challenge question in the smallgroup discussion, of the nature "What would the 15th letter be, the 20th , etc." Write the numbers on the board, so they'll get the idea that the odd and even numbers alternate.

ANSWER: odd
even
odd
even
odd
even
odd

The fraction $1 / 2$ is being introduced in a concrete fashion in tris exercise. In the follow-up discussion, be sure to emphasize that "one-half" always refers to things that have been divided equally.

ANSWER: A correct answer for this problem is any line that comes close to dividing the cookie into equal pieces.

This problem introduces the fraction "one-third" in an intuitive fashion. (Some students will miss this problem because they see the word "two" and divide the cookie into 2 pieces, instead of three.)

ANSWER: A correct answer would be any lines that divide the cookie fairly closely into 3 equal pieces.

The student is to follow the logic of the flowchart, and al so use calculator to do the computation in-volved--notice that a calculator would be necessary for most students to do the addition involved here, since the problcm involves "carrying." Some students will have trouble because they aren't told to press the "equals key" on the calculator. Going over similar problems in a small-group session should help.

ANSWER: 63

Students who have trouble with this problem might need to use a "chart format" to organize their wort. You might start them off on the solution in the smallgroup session, by first listing tlie days of the week.

$$
\text { S M T W Th } \underset{25}{f} \text { Sat }
$$

The students would put 25 on a Friday, and then count backwards, $25,24,23,22,21,20, \ldots$.$) . Stop when$ you get to 20, and say "Aha, there's a Sunday that's already passed." Let them finish for homework.

ANSWER: 3

Excellence
1155

ANSUER:


This problem gi des students a chance to extend the problem above, in an interesting way.

ANSWE R: $P$

There are several aspects to this problem that you might look for as difficulties for students. The numbers go up both sides of the thermometer, in alternating fashion. And in the last problem, the temperature is at an unsumbered increment.

In a small-group session, have students make such a problem themselves, and give it to the group to consider.

ANSWERS: 40, 70, 55
"Square" and "rectangle" are basic geometric terms used in this problem. In the small-group session have students take 6 pre-cut squares, and physically make the 2 rectangles. (Be sure and emphasize that these are the only two, since any other rectangles would be the same as these if they were turned.) Then do the same, but with 10 squares. Continue this several more times.

This problem can later be used as an introduction to prime and composite numbers.

ANSWER:


For 5 sq.


Students should answer this, based on their personal knowledge of time periods. They may have to choose some answers (painting a house) by process of elimination, rather than direct knowledge.

ANSWER:


Sequential geometric patterning is at the heart of this problem. Some students will see the same basic shape in each figure, but rotated counterclockwise.

ANSWER:


## TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | $\begin{aligned} & 1001 \\ & 1003 \end{aligned}$ | This multi-step word problem can be solved by computation (7+6 - 3-2), or by "acting it out" or "drawing a diagram" and counting. |
|  |  | ANSUER: 8 |
| 2 | $\begin{aligned} & 1004 \\ & 1005 \end{aligned}$ | This problem can be solved by "guess-check-revise" or "working backward." If students use "guess-checkrevise," they'll simply guess a number to go in the space, check it out, and revise their guess if necessary. They'll continue this process till they get the answer. |
|  |  | If they "work backward," they can ask themselves "what number did I have in the last step, before subtracting 7. It had to be 90 . What number did I have to have in the previous step so that, after adding 6, I got 90. It had to be 84." |
|  |  | Go over several similar problems in your small-group session. |
|  |  | ANSUER: 84 |
| 3 | 1017 | Students should be encouraged to find the total amount by counting, going from the largest to the smallest valued coins. |
|  |  | ANSWER: $67 ¢$ or $\$ .67$ |
| 4,5 | 1051 | Taken together, these twn problems should help children realize that $1 / 2>1,->1 / 4$, a fact they tend to disbelieve unless their knowledge of fractions has a firm foundation in concrete experiences. In the small-group session, go over a similar situation, hut use a pie, cake, or cookie example. |
|  |  | ANSWERS: <br> 4) $1 / 4,1 / 3,1 / 2$ <br> 5) $1 / 2$ is the largest |

Students might need to use a calculator to add $60+60$.

## ANSWER: 120

Students have a chance to make their own pictograph in this problem. In the small-group session, have them notice the key (or legend) at the bottom of the graph. They can consider a related problem to this one, and actually make a graph using play money in the session.

ANSWFR:


KEY:


## TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | $\begin{aligned} & 1002 \\ & 1004 \end{aligned}$ | The student might approach this problenl with "guess-check-revise." They would say something like "Suppose I have 2 of each coin. That'll be $30 \%$, which isn't enough. So I'11 try 3 of each type." Or they might make a list, like 1 dime, 1 nickel $=15$; ; 2 dimes, 2 nickels $=30 f$; etc., till they find the answer. |
|  |  | In your small-group session, go over a similar problem, perhaps with other coins. <br> ANSWER: 3, 3 |
| 2 | 1003 | Students can be encouraged to solve this by "acting it out" or "drawing a sketch." They won't have the computational skill to solve $11 / 2+21 / 2+3$, but they can intuitively and concretely put two halves together to get a whole. Go over a similar problem in the small-group session. <br> ANSWER: 7 |
| 3 | 1145 | The student must read this table carefully. The first problem lays an intuitive notion of "mode." Some students will miss the second question because they won't count Angie herself. |
|  |  | ANSWERS: <br> (A) 3 <br> (B) 1 |
| 4 | 1110 | This figure is a simple closed curve, which is like a circle in that it divides the plane into the curve itself, and the inside, and the outside. Have students take a loop of string and make various simple closed curves (they can't "cross themselves," as in $\infty)$. |
|  |  | AMSWER: $\begin{aligned} & \mathbf{B} \\ & \\ & \\ & \\ & \mathbf{A}\end{aligned}$ |

The students can practice on algebraic equalities similar to these by making some true addition/subtraction statements on $3 \times 5$ cards, covering up one of the numbers and asking another student to find the missing number. If students are having difficulty, you might want to use manipulatives.

ANSWER: 15, 25, 70

Some students will not know the even from odd numbers. You might give them an oral "counting by 2's" exercise, starting with 0 for even numbers and 1 for odd numbers, until they notice the ending digit patterns for both.

ANSWER: 218

Students are introduced to solving addition problems via "mental arithmetic" methods in this problem. These practice problems do not "bridge a decade," except for $F, H$, and I. But these should be easily done also since the student winds up adding multiples of ten mentally.

The importance of this problem can't be overemphasized. You should gradually, over the rest of the school year, extend the difficulty of the problems you ask students to use this method on, to these types:
(a) 2-digits + 2-digits, bridging a decade
(b) 3-digits + 3-digits, not bridging a decade
(c) 3-digits + 1- or 2-digits, not bridging a
decade.
In the 3rd grade, students should also practice this skill, on harder problems.

When the student turns in his/her paper, have then do this problem in their head, and write the answer only after they're through:

$$
63+24
$$

ANSWER: 87
$\qquad$

Skill of Problem

1

## Excellence

1006

1001

1017

1051

Comment
Visual discrimination is involved in solving this problem. For the small-group session, have 3 cut out alphabetical letters for $A, J, D, R, F, O$, and $H$, and have students arrange them accordiny to the patiern.

ANSUER:


The student has to find the value of a given coin collection, and then "round that value off" to either $25 \&$ or 50\&. Go over 2 similar problems in the small group session, a collection that rounds off to $25 \%$, and one which rounds off to 50\&.

ANSHER: The half-dollar.

Students are $t_{-}$determine that $1 / 2>1 / 3$ or $1 / 4$ from looking at these pictures. This problem is similar to a problem from last week's worksheet.

ANSWER: 1/2

Students actually collect data for this problem, and then make a graph with it. In the small-group session, have them grade another paper with a few problems on it, and make a similar graph.

NUMBER RIGHT
ANSWER:


Students are dealing with a ratic in this problem. If 1 pint $=2$ cups, then $1 / 2$ pint $=$ ? cups. In the small-group session, go over a similar problem with quarts and a half-gallon milk container.

ANSWER: 1 cup

TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | $\begin{aligned} & 1004 \\ & 1050 \end{aligned}$ | This puzzle will probably be solved with a modified "guess-check-revise" technique. In the small-group session, be sure that students realize all the possibilities to check (anywhere there're 3 numbers in a row) but that they can eliminate some as too large through mental arithmetic, as on problem 7 of worksheet XVI. They can also use a calculator, if the computation is too difficult. |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  | ANSWER: |
|  |  | $X X$ |
| 2 | 1001 | This multi-step word problem involves addition and subtraction, but you might suggest "drawing a diagram" for students having difficulty. |
|  | 1003 |  |
|  |  | ANSWER: 15 |
| 3 | 1006 | The student who has trouble visualizing the cubes that aren't shown, can make such a figure and count them. |
|  | 1127 |  |
|  |  | ANSWER: 20 |
| 4 | 1146 | In your small-group session, have students take their fingers and trace the steps to get to $M$ and $A$. |
|  |  | ANSWER: Math is FUN. |
| 5 | 1004 | Students will probably use "guess-check-revise" to solve this problem. use of a calculator is encouraged since the computation might be too difficult for some students. |
|  | 1168 |  |
|  |  |  |
|  |  | ANSUER: 14, 15, 16 |

Some students will miss this problem by counting each name as many times as it appears on the chart. In the smali-group session, use the chart given but ask different questions that require students to read and interpret the chart.

ANSWER: 7

71035
Students are expected to have some "real world" knowledge to answer this question correctly. Those who have trouble can perhaps visit a store on the way home from school to gain an approximate answer.

ANSWER: A. 35\$

## TEACHER COMMENTARY

Skill of
Problem
1
1050

1036
2

## Comment

In the small-group session, consider several problems similar to this one, but have the problem written on paper with the number actually torn off.

ANSHER: 4

The student has a chance to estimate the area of a figure, using a non-standard unit of measure. In the small-group session, have them find the area of another shape--perhaps a closed hand--using this thumbprint. They can draw circles that are about the size of the thumbprint, to "cover it."

ANSWER: Accept any answer between 22 and 27

3
1007

1007

1007
In the small-group session, go over a similar problem, perhaps with a string of numbered tickets to a theater.

ANSUER :


This is a simple patterning problem, but the digits are written as they would appear on a calculator display.


Most students will realize that this geometric figure has been turned clockwise through a right angle, moving from left-to-right.

ANSWER:


265

Encourage students to notice the key at the top of the chart. They can determine the answer to part B either by skip counting (5, 10), or by adding $5+5$ $=10$.

ANSWER: A. $\downarrow$

B. 10

Students might solve this problem by "guessing-andchecking," or by deducing that each opposite pair of numbers on a line mist total 5.

Have them do a similar problem in the small-group session (with a number other than 5 in the center).

ANSWER: (Or other versions in which


Students can determine that 4 is the covered digit by process of elimination, or by noticirg the pattern of keys ( $1,2,3, ?, 5,6 \ldots$ ) starting at the bottom of the calculator. They must write 4 in the right-hand side of the display to earn this star, however.

ANSWER:


TEACHER COMMENTARY

Skill of

## Comment

The student is to find the area of this figure by counting unit squares. This is the first worksheet in which half-squares are encountered. In your smallgroup session, have a few similar figures drawn on grid paper, and some square centimeters that can be cut with scissors--have the students cover the drawn figures with whole unit squares, and then cut "halfsquares" to cover the extra pieces. The emphasis should be on an intuitive interpretation that 2 halfsquares can be "put together" to make a whole square.

AMSWER: 19

The student is to have both a diagram, and the correct numerical answer, to get credit for the problem. Emphasize to students that, even though they probably could have answered this problem without a diagram, this is a good way to begin trying to understand problems that they don't know how to answer.

ANSWER: Tine diagram should show all 14 hops.

The purpose of this problem is to have the student learn to use a calculator to solve basic addition and subtraction problems. You might notice that, in the last 2 problems, students would probably not know what to do unless they had a calculator.

AMSWERS: 126
235
52
23

1140

1153

In your small-group session, have some similar figures drawn for students to work on briefly. Be sure they understand that they're looking for a figure that can be compl etely drawn without lifting the pencil, or retracing a path, once started. They should also note that, in some "traceable" figures, you have to start at the right place to do so.

This problem is from an area of geometry called "topology." The figure on the far right is the only one that is "traceable" in the manner described. Notice that it has 4 vertices (points where the paths meet), and they're all "even" since they all have an even number of paths coming from them. The other two networks are not traceable, and notice that each of them has 4 vertices that would be called "odd" by the number of paths coming out from it. Whether a network is traceable or not depends on the number of "odd vertices."

ANSWER: The figure on the far right should be circled.

This problem is designed to reinforce the skill on constructing a bar graph. Students would shape in the graph according to the information given in the problem. A finished graph is shown below:
AISHER:


This experiment gives students the opportunity to collect and record data in a simple probability experiment. In your small-group session, have the entire group do the experiment t.cgether, just to be sure they understand how to make tally marks, determine the "up face," etc. Al so be sure that they understand that they may have to circle more than 1 face.

ANSWER: Check to be sure their tally marks total 25, and that they circled the face(s) with the most marks.

## TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1017 | Most students should get this problem, even those who think of adding on the tax. |
|  |  | ANSWER: paint set |
| 2 | 1035 | The student has to use the visual clues to determine that the pies left are closer to $21 / 2$, than to either 2 or 3. Consider several similar problems in the small-group session, some of which "round off" to 2, some of which "round off" to 3, and some to $21 / 2$. |
|  |  | ANSWER: B. |
| 3 | 1046 | Simple addition and subtraction skills are reinforced prior to asking the student to determine the relationship between 2 numbers. In the small-group session, first review > and <, and then do a couple of similar problems with different outcomes at the final step. |
|  |  | ANSWER: < |
| 4 | 1074 | Students might solve these problems by first putting them in vertical format, and then applying logic to determine the digits one-at-a-time. Or they might "work backwards" by subtracting, adding, and subtracting respectively, to find the missing numbers. Do several similar problems in the small-group session, with correct numbers actually covered up by . piece of paper, to get across the concept. |
|  |  | AMSWER: 43, 31, 45 |
| 5 | 1108 | This activity will lead into an understanding of lines of symmetry in the upper grades. It will also reinforce the concept of $1 / 2$ as a fraction. This is preliminary to skill 1108. |



In this problem the student is asked to convert weeks into days. Extraneous information has been added to the problem as a distractor.

ARSWER: 14 days

This activity reinforces the use of a calculator to make calculations. You may point out that the associative principle applies here - you may add the numbers in any order and still come up with the same answer. You might also have to point out that they have to use + two times, and the $=$ also. Some will also not realize that they have to press - at the right time.

ANSWER: \$31.33

Students are likely to solve this by "guessing and checking" until they get the right answer. Another problean organizer would be to list all the numbers that add to 21, and check the list till you find the pair in which one number is 3 greater than its partner. In your small-group session, do a similar problem like "what two numbers have a sum of 20 , and one is 4 more than the other?"

ALSIER: 9, 12

## TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1001 | This is a multi-step word problem, broken down into the steps. The students can get the answer either by adding whole numbers, or simply by counting. It's also a good problem to solve by drawing a diagram (skill 1003)--the simpler, the better. |
|  |  | ANSWER: 13 females <br> 10 males <br> 23 people on the bus |
|  |  | NOTE: 24 if student counts a bus driver |
| 2 | 1002 | Students are to solve this problem by making a list. In your small-group session, consider a similar problem such as " 2 shirts, 3 pants of different colors. How many outfits?" The students should list all of them. |
|  |  | ANSWER:(red, blue) (blue, blue)$\quad$(yellow, blue) <br> (red, white) <br> (red, green) (blue, white) <br> (yellue, green) (yellow, white) |

The order of the list above isn't important.

31030

4

1021
1009

This problem is a subskill for rounding off money values so you can estimate the solution to a money problem. In the small-group session, have coins taped to a number line (a dime to "10," etc.), and consider similarly priced objects. Students would place the object where it belongs on the number line, and then determine which coin it is closest to.

ANSWERS: balloon: dime
car: half dollar
ball: quarter
bear: half-dollar
ring: dime

The essence of this problem is to know that Howard watches $t . v$. from 11:1! 12:15, and from 12:30-1:30. Students shr 1d realiz. that 1 hour passes from 11:1512:15, with computation, and the same for 12:30-1:30.

ANSWER: 2 hours

Have a similar problem for students to do in class, such as arranging these $3 \times 5$ cards in order to eat a banana:

| Peel banana | Throw away peel | Eat banana | Get banana |
| :---: | :---: | :---: | :---: |
|  |  |  |  |

ANSWER: Get the leash. Get the alliyator. Put the leash on the alligator. Open the door.
Take the alligator outside.
Note: Steps 1 and 2 above might be reversed.

## Problen

1

2

31167
Skill of Excellence

$$
1050
$$

1004
1005

ANSWER: one answer
(Others can be checked by ensuring that "opposite numbers" add to 9.)


In your small-group session, consider similar problems. Ask the students how they can tell that the marks "go up by $2^{\prime \prime}$ instead of 1 (they can start at 40, e.g., and count " $42,44,46,48,50 ;{ }^{\prime \prime}$ landing on 50 at the same time they count it means the marks go up by 2).

ANSWER: 3rd thermometer from left.

The student follows this "coded flowchart" that goes right-to-left.

ANSWERS: 39
80
57
4
1107
"Triangle" is being reinforced in this problem.

## ANSWERS:



273

Students can consider similar problems to this one in a small-group session. Encourage them to "count up" from the cost of the item to $75 \notin$, and record each coin value they use. (Be sure they start with the largest coin possible, ir counting back the change.)

ANSWER:


ANSWER:


Students are to make a bar graphusing
data give in the problem.

Students ca, use a calculator to solve this realworld problem, if they need ${ }^{+} 0$. Consider a similar problem in class, perhaps "\$?.'; per week, saved for a month."

ANSWER: \$5.25

Ir later grades, this nroblem will be solved by diviEion ( $\$ 10-1.75$ ). AL ihis stage, students can solve it by simply adding $\$ 1.75$ to itself continously, till they get over $\$ 10$, and counting the number of addends. Do a similar problem in the small-group session. (This is a good chance to show them the value of the "repeating function" characteristic of most calcula-turs--i.e., $1.75+1.75====$ produces $\$ 10.50$ as the answer.)

ANSWER: 6 weeks
$6 \quad 1125$
Have students discuss how they measured the length of the star's tail. Some will trace the wand, and us's the tracing, some might cut off a length that long and use their "real object," etc.

ANSWERS: 2
$21 / 2$ or 3
$31 / 2$ or 4

## TEACHER COMMENTARY

| Problem | Skill of <br> Excellence | Comment |
| :---: | :---: | :--- |
| 1 | 1003 | In your small-group session, have students do a simi- <br> lar problem about a frog falling in a well. They <br> shoulc actually draw the diagram, as in |

ANSWER: 6 hours


21035

31126
ANSWER: Bicycle $\$ 80$
ANSWER: Bicycle $\$ 80$ Barbie doll $\$ 8$ Balloons Computer $80 \&$ $\$ 800$
Be sure students understand the difference in \$ and 4.

Students met this same sort of problem in worksheet $X X$ of this set. This should give them another chance to show they can count whole unit squares, and put two "half-squares" together in counting.

ANSWER: 13

41050
By now, students should be familiar with such prob- lems. However, the last two problems here involve "carrying" and "dorrowing," for the first time. You might have several such problems written on paper (with "carrying" and "borrowing"), with covered-up digits ior the small-group to solve.

ANSWERS: | 15 | 26 | 53 | 94 |
| ---: | ---: | ---: | ---: |
| +21 |  |  |  |
|  | $=14$ | +28 | -38 |
|  | $\frac{12}{61}$ | 56 |  |

The essence of this problem is to have children re- alize that answers on a calculator aren't always correct. jince Josie's best friend was in the 2 nd gradesame as these students-an answer of " 21 " would not be reasonable.
ANSUER: MO
Students will probably miss this the first time, because they think that 2 pieces would require ? cuts (of 5 minutes each) instead of only 1. Have them act it out, or draw a sketch. This should help then see that only 2 cuts are required, at 10 min. each, to get 3 pieces.
ANSUER: 20 minutes
$7 \quad 1003$
Studerits will likely forget to count themsel ves. Acting this out, or drawing a sketch, helps them find their error. Have them draw a sketch of a similar problem.
ANSWER: 21

# TEACHER COMMENTARY 

## FOR

## GRADE 3 WORKSHEETS

$\qquad$ I

## TEACHER CC MENTARY

| Problem | Skill of <br> Excellence |
| :---: | :---: |
| 1 | 1001 <br> 1003 |
|  |  |

1003 This problem is similar to problems in Grade 1, Workshret XXV and Grade 2, Worksheet XXV. In your smallgroup session, you might start off their drawing for them by making the first couple of 3-foot climbs and l-foot slips. The students can finish the sketch by themselves.

ANSWER: 5

Students will probably solve this problem by addition, but the foundation is there for this to be a multiplication problem. The numbers are easy enough to deal with so that an "intuitive thinker" might solve it by simply counting " $1 / 2$ dollars, 3 dollars, $41 / 2$ dollars, etc."

ANSMER: \$9

41031
In your small-group session, measure only one of the three things listed in the chart--students can measure the other two at home, to earn the stars.

ANSWER: 114
93
73

Graph just one of the foods in your snall-group session (perhaps hamburgers) is a group, on the board. The students complete the graph at home, for all three foods.

ANSWER: see below


Do a similar problem in class, but using two children on a see-saw, with known weights.

ANSWER: b
"Mental arithmetic" is the alternative to the $\mathrm{L}: \mathrm{ual}$ "paper-and-pencil" algorith that is being reinfurced in this problew. Consider a few examples in class similar to those on the worksheet (probiems for which it is easy to mentally "go up to" the next hundred).

To earn their stars, have this problem taped to the table where they turn in their papers--they work it mentally, and whisper their result to you. Give them credit if they give you the correct answer verbally.

ANSWER: Problem taped to desk--
WIN $\$ 1000$, BUY GIFTS TOTALING $\$ 697$, HOW MUCH CHANGE FOR A $\$ 1000$ BILL?

The answer is $\$ 303$.

TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | $\begin{aligned} & 1001 \\ & 1003 \end{aligned}$ | This exercise leads the child to soive a multi-step word problem, through several steps. In (a), the student would probably realize that 2 cows have 8 legs, so the rest of the legs--10--would be for chickens. This would be 5 chickens. |
|  |  | For (b), the situation is reversed--6 chickens would have 12 legs, so the legs left ( $24-12=12$ ) would be for the cows. This would be 3 cows. |
|  |  | The last problem has the child compute (or count) the legs on 5 cows--20--and add that to the number of legs on 3 chickens--6. So the total would be 26 legs. Note that a student might solve these problems either with arithetic, or by drawing a diagram and counting. Go over a similar problem in your small-group session. |
|  |  | ANSWER: <br> (a) 10 <br> (b) 3 <br> (c) 26 |
| 2 | $\begin{aligned} & 1170 \\ & 1004 \end{aligned}$ | These three problems give students the opportunity to interact with a calculator, in an interesting fashion. They would probably sol ve them with a modified "guess-check-revise" technique--guessing how to put the digits together, to give the answer shown on the display. Go over a similar problem in your small-group session. |
|  |  | ANSWER: $48+26=74$, or $28+46=74$ |
|  |  | $48+36=84$, or $38+46=84$ |
|  |  | $14+68=82$, or $64+18=82$ |
| 3 | 1003 | Students can arrive at this answer by drawing a diagram and counting the clothespins, or perhaps by reasoning in an inductive fashion--since 5 pins would hold 4 towels, 14 would hold 14-1 or 13 towels. Simply mention to the students that if thay're unsure, they can make a sketch of the problem. |
|  |  | ANSWER: 13 towels |

Students will probably solve this problem using a modified "guess-check-revise" technique. It's probably easier to start guessing by looking at the "clues on the extremes--the ones that have either high or low costs.: For example, the 2 nd rlue tells you that either a brush or an apple is $10 \mathbb{C}$, and the other is 5t--so you can work from there. Or the last clue, by itself, says that either a ball or a brush is $30 \%$, while the other is 108 .

In your small-group session, ask a successful student how he/she started the problem.

ANSWER: ball: 30\&
apple: $\quad 54$
pencil: 12\&
brush: 104
car: 15\%
$5 \quad 1110$
In your small-group session, be sure students understand what they're asked to do. Take a couple of similar figures to do as a class, on the board.

One like.

can be traced by starting anywhere. But one like can't be traced at al?. Yet $\rightarrow$ can be traced by starting at the upper right or bottom right corners.

ANSWER: The bottom figure can be traced by starting at either of the circled points.


TEACHER COMNEMTARY

$5 \quad 1072$
For students who have trouble, have them first place the numerals in descending order:

60,000; 4,000; 900; 20; 7.
ANSWER: 64,927

This appears to be a difficult computational exercise, but it's actually very easy.

ANSWER: 900000000000000009

Students might find these answers either through addition or multiplication. In your small-group session, s) over only Long's length.

ANSUER: 60
34
45
65

Have students measure a similar figure in the smallg: oup session.

ANSWER: 18-19

Students will likely have no trouble with this problem.

ANSWER:


Provide students with a problem like this, but with blanks for the numbers. Then give them 5 or 6 sets of numbers to $g o$ in the blanks, and have them "round off" the money amounts and find the answer through estimation. Be sure they have some te practice with at home, together with answers.

ANSWER: Cut this problem out, and tape it to che table where you take up the worksheets. Students can read it without a pencil in their hands; when they have an answer, they can whisper it to you and you write it on their paper. (The answer is "yes.")

「Davic received $\$ 3.00$ for mowing the lawn. He wants to 1 , buy some toys at the toystore. He has chosen a kite for $\$ 1.49$, a toy car for $\$ .79$ and a mask for $\$ .39$.
'Can he buy all of these toys?
SSolution: $\$ 1.50+\$ .80+\$ .40=\$ 2.70$
Answer: Yes. (\$2.70 < \$3.0C)

## TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1001 | Students will use addition and subtraction to solve this problem, or perhaps draw a diagram, and count. <br> ANSWER: 23 |
| 2 | $\begin{aligned} & 1004 \\ & 1005 \end{aligned}$ | Have students who were successful on this problem share how they began. It will probably involve either "guess-check-revise"--they' 11 guess the answer, and check it by adding 5 , subtracting 6 , then adding 2. If they don't get 20, they'll revise the guess. <br> Another way is to "work backward" by asking "what did I have to have before adding 2 to get 20." I had 18. They continue reversing the steps to arrive at the starting number. <br> ANSHER: 19 |
| 3 | 1017 | Encourage students to count the larger coin values first, and then add on the smaller values. Or, look for coin values that add up to a dollar in counting. :h for a student who writes $\$ 2.1$ or $\$ 2.10$ instead of $\$ 2.01$ <br> ANSWER: \$2.01 |
| 4,5 | 1051 | These two problems are intended as concrete reinforcement for equality between fractions. Have several similar problems for students in the small-group session. <br> ANSWER: <br> (4) $1 / 4$ <br> $2 / 8$ <br> (5) equal to |
| $\epsilon$ | 1073 | In your small-group session, encourage students to say the even or odd numbers in seqquence orally, to themselves, till they notice a pattern. Elicit that the odd numbers end in $1,3,5,7$, or 9 , and the even numbers in $0,2,4,6$, or 8. <br> ANSWER: odd, even, odd, even, even |

Use the graph, but ask students a different question fyom the one on the worksheet. Some will solve the problem by cal ulating the totals for both cities and subtracting - others will simply count " 50,100, etc..." as many times as necessary to find the difference, depending on the "extra" symbols one city has over the other.

ANSWER: 109
$8 \quad 1122$
$9 \quad 1036$
1107

10
1047

11
1107
1006

Students will probably know that 60 secords $=1$ minute, so they can add 60 and 60 for 2 minutes. Many will intuitively realize that "half of 60 is $30, "$ so $21 / 2$ minutes is $120+30$ seconds.

Do a similar problem in class. Do not become formal with the computation.

ANSWER: 150

Take a similar problem in class - perhaps with a square that's 4 inches on a side. Have the students use string to measure the circumference of the circle.

ANSWER: (B)

This is a challenging computational problem, but gives a nice pattern in the answer.

ANSWER: 40000991111

Be sure students know what a rectangle is. Encourage them to start looking in an organized fashion - smallest first then next largest, etc., till they have counted all the rectangles, including the largest.

ANSWER: 6

## Comment

Students will probably notice that these 3 figures all have a "square base" with a roof on it. The next shape would be a square base with 25 dots, and a "roof" of 10 dots. Observing the "square base" and "roof" in joil small-group session should te sufficient he'p.

ANSMER: 35

Take a similar proslem for the small-group to solve, noting they have to add the tax to the total cost, and then subtract from the amount of money shown [or, "count up" from the total, to the amount].

ANSWER: 7¢

Students might solve this simple algebraic equation either by "guess-check-revise" or by "working backward." If they use "guess-check-revise"-they'11 guess a first number to go in the box, and check it to see if, when added to 96, they get 247. If not, they'11 revise the guess either up or down, and guess again. They might "work backwards" if they mentally turn the addition format into one that requires subtraction, i.e., the missing number can be found by doing "247-96."

ANSWER: 151

Students have a chance to learn what "bisect a line segmerit" means in this problem. The purpose is to approach this construction problem that's typically done with straight-edge and compass, through paperfolding, concentrating on an intuitive understanding of the problem. Even though it's not mentioned in the problem, point out to the students later that the crease they make (if they do it correctly, by match-ing-up the end points) gives them the "perpendicular bisector" of the line segment.

Note: Some students might use a ruler to bisect the segment in half, and then fold the paper. Give them credit, but point out that the ruler isn't necessary.

ANSWER:


Students have a chance to show that they understand temperature measurement in this problem, and how to record it using a thermoneter. The readings were set up to carry a student from a positive reading ( $+10^{\circ}$ ), to zero, to the negative side of the scale $\left(-10^{\circ}\right)$. In your problem-sol ving session, do a similar problem. Also ask students "what season of the year was this in--winter, spring, summer, or fall?" This will reinforce skill 1035 - giving reasonable answers based on personal knowledge, rather than rounding and computing.

ANSWER:


Friday


Saturday


Sunday
$\qquad$ (continued)

The purpose of this problem is to have students compute subtraction problems using a method other than the standard algorithm. This method is sometimes called "add a neat number;" the student looks at a problem, and decides what to add to the lower number to make it a "nice number" to subtract. They then add this same number to the top also, to produce a "slightly different" problem with the same difference as the original problem. Students should be encouraged to continue using this method at times throughout the year.

Students are not asked to do anything with the practice problems to get credit, but you can use these as "slightly different" problems in teaching the system in the small group session:

| 347 | 529 | 873 | 768 | 692 | 454 | 625 | 850 | 850 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| -100 | -100 | -300 | -100 | -200 | -100 | -100 | -200 | -300 |

When they turn in their paper, give them this problem, which is taped to the desk or table. Have students work the problem mentally and write the answer on his/ her paper.

472
$-198$
ANSWER: Given problem Different problem

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1035 | In your small-group session, you might do a similar problem with a different coin. |
|  |  | ANSWER: any number for "guess" 12 for "real answer" |
| 2 | 1051 | Show students a real measuring cup, with $1 / 2$ and $1 / 4$ marked on it. Be sure they understand the essence of this problem - that $1 / 2$ is a greater amount than $1 / 4$, even though 2 is less than 4. |
|  |  | ANSWER: No |
| 3 | 1072 | Students should learn to do problems like this by rearranging the numerals, and not by addition. |
|  |  | ANSWER: 343,020 |
| 4 | 1109 | Review this method of testing angles in class. Have students use it to classify 4 or 5 other angles (at least 1 acute, 1 obtuse, and 1 right). |
|  |  | ANSWER: Upper left, counterclockwise: acute, obtuse, right, acute, obtuse |
| 5 | 1006 | This problem is one that requires visual discrimination. If students will physically turn the paper in different directions, they will not focus so hard on the bull that's so obvious when it's "right side up," and have better luck finding the man. |
|  |  | ANSUER: The man's mouth is right under the horns, slightly to the left of the middle. (The middle is the man's nose.) |

This problem combines several of the skills under Standards of Excellence. Students will probably solve it by either "guess-check-revise" or "working backwards" as problem-solving strategies. For "guess-check-revise, ${ }^{*}$ the student would simply guess a number to go in the box, and check it out by adding 3 and multiplying the result by 2 , to see if they get 14. If not, they'd revise the guess either up or down.

If the student uses "working backward," they'11 ask themselves "what number, multiplied by 2, gives 14?" This would give them 7 as an intermediate step. Then they'd ask "what number would I have to start with, so that after adding 3, I get 7?"

ANSWER: 4

This is a word problem that has a "trick" in it--most students will forget to count themselves. It is intended to demonstrate to students that they can't just use "key words" to solve math problems.

ANSWER: 21

8

This puzzle requires computational ingenuity and perhaps "working backward." The "wor!ing backwards" would enter the picture since the student has to "think in reverse" to solve this addition problem. Have them do a similar problem in the small-group session, one that also involves "carrying" for the missing digits.

ANSIER:


These three problems are meant to be done together, to give students some justification in the real world for $\rangle,<$, and $=$ with fractions. In your small-group session, go over a similar problem with months of the year--school vs. summer--in which 9/12 > 3/12.

ANSWER: (9) $5 / 7$
(10) $2 / 7$
(11) $5 / 7$

In your small-group session, have students measure the perimeter of several polygons similar to this one. The lengths of the sides should come out either in whole centimeters or half centimeters.

ANSWER: $16-17 \mathrm{~cm}$

TEACHER COMMENTARY

Skill of

Problem
1

2
1009

1166

Comment
Students can demc.istrate their understanding of "elapsed time" in this problem. The first clock shows 8:15 AM, and the second shows 10:25 PM. Students can either count the hours from 8:15 till 10:15, and add on the extra 10 minutes, or they might know that there would be 12 hours from 8:15 AM till 8:15 PM, and add on the extra 2 hours and 10 minutes.

ANSWER: 14 hours, 10 minutes

This problem contains both the answer, and a lot of extraneous information. Some students will actually compute the answer: $68+12=80$, and then $80-68=12$.

ANSWER: 12

This is a flowchart for a common, everyday activity. Steps $B$ and $C$ are interchangeable, as are $B$ and $G$. But C must precede $G$.

ANSWER:

$4,5 \quad 1001$

These problems both involve estinating and approximating, and problem 4 incorporates visual discrimination. The student must notice that the gas gauge shows a 1 ittle over $1 / 2$ a tank left after their arrival, which means they used less than $1 / 2$ tank in getting to Grandma's house. So they should be able to get back without adding gas.

The answer to the first part of problem 5 comes directly from reading the odometer and subtracting 35,102 from 35,297 (to get 195). The second part involves knowing the speed limit is 55 MPH, and adding to see that there are about $31 / 255$ 's in 195. An answer of either 3 or 4 hours, or $31 / 2$ hours, should be accepted.

In your small-group session, be sure to point out the 3 important features--the speedometer, the fuel guage, and the odometer.

ANSWER: (4) yes
(5) $195 ; 3,31 / 2$, or 4 hours are acceptable. NOTE: If student considered round trip the above figures would be doubled.

This problem gives students the opportunity to practice $>,<$, and $=$ in an interesting puzzle. The answer is "yes," which comes from seeing the diagonal line formed by $>$ from lower left to upper right.

In your small-group session, do the first twu or three problems to $b \geq$ sure students understand what they're to do.


ANSWER: Yes

## TEACHER COMAENTARY

## Problem

1

21050
1005

Comment
Students will probably find the answer by counting by 7's fifteen times, rather than multiplying. They can find the answer by actually building such a figure, if they are having problems with visual discrimination. Also the teacher may bring out in a discussion setting, that this figure is a well-known optical illusion in that, 2 of the blocks "jump back and forth" if you stare at it.

ANSWER: 105

This is a puzzle that requires the student to demonstrate understanding of, and ingenuity with, computational princip?es. Students may solve this problem by "working backwards" mentally because they find the only sum they can $(3+10+6+15)$, and then another row or colum with 1 number missing $(5+11+10+8)$, and keep "working backwards" till they get all the numbers correct. Give them this hint in your smallgroup session.

ANSWER:

| 16 | 2 | 3 | 13 |
| ---: | ---: | ---: | ---: |
| 5 | 11 | 10 | 8 |
| 9 | 7 | 6 | 12 |
| 4 | 14 | 15 | 1 |

Some students will solve this by "cuess-check-revise" (guessing various 2-digit numbers and checking against problem conditions). Others might make a list of all those with a digit sum of 5 , till they get one with a reversed-digit difference of 9 from original number. In your small-group session, consider a different problem, and solve it both ways.

ANSWER: 32

In your small-group session, consider a similar prob1 em - find 3 rectangles with area 18 . They would find a $1 \times 18$, a $2 \times 9$, and a $3 \times 6$.

You can later extend this concept as an introduction to prime vs. composite numbers. Prime numbers are those for which you can only make 1 rectangle (a l by ?).

ANSWER: The 4 rectangles would be a 1 by 24 , a 2 by 12, a 3 by 8 , and a 4 by 6.

71009
As a hint for this problem, ask the students "does it say the clock was even wound to start with?"

ANSWER: 0

Although it's not mentioned in this problem, this is an intuitive introduction to "averaging." Before students meet this word in a similar problem in a few worksheets (XII), you might want to give them several problems similar to this one and use the word "average." Approximate problems are of this nature:

1.

2



ANSWER: 30

## TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1001 | Students will probably solve this by repeated addition $(42+42+42+42)$ or multiplication $(42 \times 4)$, followed by addition (+5). Solve a similar problem in your small-group session--perhaps 3 buses and 20 extra kids. |
|  |  | ANSHER: 173 |
| 2 | 1003 | Encourage students to draw a diagram to solve this problem. If so, perhaps they'll realize they need an extra post at one end. |
|  |  | ANSWER: 11 |
| 3 | 1022 | In your small-group session, ask questions that will enable you to see if the students are correctly interpreting the chart. |
|  |  | ANSLER: Cartoons |
| 4 | 1032 | Consider a similar problem in your small-group session, but using a more concrete example - money. Have the students add two money values together, and round off to the nearest dime. |
|  |  | ANSWER: 0.8 |
| 5 | $\begin{aligned} & 1050 \\ & 1004 \\ & 1005 \end{aligned}$ | This problem requires the student to solve a puzzle based on computational principles. The student may use the "guess-check-revise" method to solve the problem, or "working backward" if he or she reverses the operation and asks a correlated addition fact. |
|  |  | $\text { ANSWER: } \begin{array}{r} 49003 \\ \\ \\ \hline-17874 \\ \hline 21129 \end{array}$ |

1109

| Refresh student's mind about how to test angles (work- |
| :--- |
| sheet VI, *4), and what to call them (acute, obtuse, |
| or right). Show some similar examples in class. |

ANSWER: The 3rd from the left
1127

1006 | Explain to your students that "volume" is the number |
| :--- |
| of cubes it takes to make a sol id figure - relate it |
| as the 3-dimensional equivalent of "area" in 2-dimen- |
| sions. Some will have difficulty counting the cubes |
| because they can't see them all, and can't visualize |
| them. Have these students make such a figure from |
| common blocks or sugar cubes. |
| ANSWER: 27 |

$\qquad$ $x$

## TEACHER COMMENTARY

## Comment

In your small-group session, you might suggest that students first simply try to determine the answer just by looking, but then trace the given shape, and twist and turn it to see if it can be found in the other shapes.


ANSWER: The first three should be circled.

1050 1004 1005

1006 1007

Students will probably either simply guess digits to go in the blanks, or determine them by adding up what is already present and mentally "working backwards," using logical reasoning. For your small-group session, have a similar addition problem with some covered digits, and students tell how they'd find them. (Be sure "carrying" is involved.)

ANSWER:

| 3 | 4 | 9 | 1 |
| ---: | ---: | ---: | ---: |
| 8 | 5 | 6 | 0 |
| 5 | 4 | 2 | $\frac{3}{2}$ |
| 7 | 8 | 0 | 6 |
| 2 | $\underline{5}$ | 2 | 8 | 0

Some students will notice that a rigid "turn" is occurring in moving from left to right. You might take this opport;nity to introduce the 3 types of rigid motion in geometry: slides, flips, and turns.

ANSWER:


This problem, or a similar one, can be briefly demonstrated in class.

ANSWER: B

| 5 | 1123 | In a similar pioblem in your small-group session, encourage students to find the answer by counting from the beginning point, by hours, to that many minutes past 12. Then they count on as far as they can, calculating the last few minutes and adding them to the hours they counted. <br> ANSWER: 6 hours and 15 minutes |
| :---: | :---: | :---: |
| 6 | 1170 | Be sure students understand what they are to do in this problem. You might take another addition problem with sum of 80814, to demonstrate the answer. <br> ANSWER: <br> (c) both |
| 7 | 1036 | This item is designed to provide reinforcement in estimating the area of a geometric figure. It will help them to draw in the lines from point to point, and count half squares, etc. <br> ANSWER: B. about 8 squares |
| 8 | 1166 | This problem is designed to help a student follow the logic of a flowchart for a daily activity. <br> ANSWER: B. Wait for the toast to pop up. |



ANSWER: \$2.66

The student must use his personal knowledge (of measurement) to give a reasonable response. Computation or estimation will not help the student derive an answer.

ANSWER: grams

41050
1005
Students will probably solve this problem by mentally "working backwards" to find each digit, moving right-to-left. Go over a similar problem - one that involves "borrowing" - in your small-group session.

ANSWER: $\begin{array}{lllll}4 & 9 & 6 & 4 & 3\end{array}$

| -2 | 0 | 3 | 2 | 3 |
| ---: | ---: | ---: | ---: | ---: |
| 2 | 9 | 3 | 1 | 8 |

5
Encourage students'to share all of their ways to find the answer, some of which might be surprising.

ANSWER: 109

Do a similar problem for the students. Many will be confused by the fact that they are to compare expressions, rather than simply numbers.

ANSWER: <

71021 1123
$8 \quad 1145$ 1150

Have students solve a similar problem in school.

ANSWER: Yes

Use the pictograph in your small-group session, but ask other questions.

ANSWERS: (A) Mary, Susan, Tom
(B) 5
(C) 7
$9 \quad 1168$
A calculator must be used to perform this computation. The comma will cause a probiem for some students, as will converting
$2 3 \longdiv { 1 1 7 , 4 6 1 }$ into $117401 \div 23$.
ANSWER: LOIS

## Comment

If students have trouble with this problem, they either don't know a process for finding the average, or they perhaps don't know how to divide. You can help them with the concept of averaging, without explicit referral to division, by having them think in this way:


In your small-group session, have pennies stacked up as shown, and tell them to make all 3 stacks equal to find the average, and report how high each "evened out" stack would be. They can actually do this at home, if they want the stars.

Note: This problem was introduced intuitively in worksheet VIII.

ANSWER: 30\&

This problem is one that requires ingenuity with computation.

ANSWER: 20
(4) 7

Be sure students can find the sales tax by counting 5\& for every dollar spent. Practice orally with amounts like $\$ 9, \$ 11$, etc., having students count 5 , $10,15,20$, etc. Be sure they also know to add the tax back to the amount spent.

ANSHER: \$15.75

Demonstrate a couple of problems like this, using some standard weights and familiar classroom objects.

ANSWER: B

Students should solve this problem by thinking of 89 d as "close to" one dollar, and the same for 93p (do not teach "rules for rounding"). Therefore, the change would be "cl ose to" $\$ 5$, $\$ 2$, or $\$ 3$. Go over a similar problem in your small-group session.

ANSWER: (c) $\$ 3$

The chart is a pictograph, with a key bel ow the graph. Students might find the kid with perfect attendance by computing 180-30 $=6$, and then looking for someone with 6 "happy faces." Or they might just count by 30 for each "happy face," and find the child who has 180 days' worth.

ANSWER: Jo

Students who find the answer to this problem will probably be using "guess-check-revise," in that they'11 make a first guess at the dog or cat's weight, and double or halve that for the other's weight, and check to see if they get 27. If not, they'11 use the knowledge gained in the first guess, to revise the guess. (They might use a "modified" first guess, by realizing that the dog's weight has to be an even number.)

Take a similar problem in your small-group session, and solve it together by "guess-check-revise."

ANSWER: 18, 9

This is one of those "trick questions" the first time you hear it. The natural tendency is to think of cotton as lighter than lead; this is true of the density of the two. A follow-up discussion should clarify this point for students.

ANSWER: They're the same weight.

Students will use "guess-check-revise" to solve this problem also (since they don't know algebra). They'll guess at one of the pages, and then add that page and the next, consecutive page, to see if the total is 53. If not, they' 11 use the knowledge gained. to revise their guess either up or down, and guess again.

In your small-group session, solve a similar problem and check the answer by opening a book to the pages and adding on a calculator.

ANSWER: 26 and 27

TEACHER COMMENTARY
Skill of

Problem
1

2
1010

3

4

1126

1019

1046 1054

Comment
Students have previously been introduced to counting whole and half-squares to find the area of a figure this problem should provide practice in this. The only difficult part might be that in the chimney of the house, students must think of "putting together" 2 hal f-squares that aren't visually the same.

ANSWERS: 35, 15, 5

The student is to read the information in the chart, and make a conclusion about the size of the animal in comparison to the heartbeats per minute. This gives the student the opportunity to form a tentative hypothesis in a problem-solving situation.

ANSWER: slower, less, or an equivalent word that gets across the meaning.

Getting change for a purchase is being reinforced in this problem situation. Notice that the answers are all in terms of the actual coins one might get back in such a situation, rather than using standard "dollar and cents" notation. The problem can therefore be solved by "counting up" rather than computing.

ANSWER: (c)

Recognizing >, <, and $=$, and the use of parentheses, are combined in this problem. Go over several similar problems in class, emphasizing evaluating both sides independently before making a judgement about >, <, or $=$. Also include one or two examples (similar to the last problem) in which children must work within the parenthesis first, to eval uate the expression correct$1 y$.

ANSWERS: $=\rangle,,\rangle,=,\langle$

This problem is not directly related to one of the skills of excellence, but it provides you the chance to extend the problem in a direct fashion to the skill of "working backward." Once students understand the basic idea of a "function machine" such as this one-and you could design any type of function machine (adding 4, doubling and then adding 1, etc.), they enjoy finding the output numbers, given the input numbers. But you should also turn the situation around mentally for them, and give them a few output numbers, and ask for the input numbers. In this particular case of the "squaring machine," you might say "Suppose 100 came out of the machine--what number was dropped into the machine?"

ANSUER: 9
49 64

1029

1047

Rounding off to the nearest hundred is the essence of this problem. Probably the hardest part here is that the student is asked to round off to a "middle digit," rather than the way they're asked to round off in most textbook situations.

In this problem, unlike many in which they are estimating an answer, they should add the two gi ven numbers, and then round off the answer.

ANSWER: 7400

This is a straight computational exercise, but is similar to a flowchart in that the steps are assumed to be followed from left-to-right, in the order given.

ANSWER: 1147

This problem is most likely solved either by "working backward" by reversing each step as you go backward from 24 to the left side, or by "guess-check-revise." For "guess-check-revise," the student would simply guess the number to start off the process, and check it out to see if it's correct. If not, they'd revise their guess either up or down, depending on what they learned from their first guess. They'd continue in this fashion till they "narrowed down" the numbers, and found the one to work.

Show the children how this problem is similar to previous ones they've done - IV, \#2 and VI, \#6.

ANSWER: 7

Grade 3, Worksheet XIII (continued)

These two froblems are thrown in simply as computational challenge problems, for the student who wants to earn sore stars. Notice the patterns, for ease of checking!

ANSWERS: 739777397773977739777
46394639463946394639

## TEACHER COMMENTARY

## Problem

1

1007
(B)


Students will need to use visual discrimination skills to notice the patterning involved in these problems. ANSWERS:
In your small-group session, cover only how to locate the "T" and " $S$ " that are given as hints. However, take a moment to show the usual, ordered pair notation - $(1,5)$ for "T"; $(2,5)$ for " $S^{\prime \prime}$ - because it will soon be used in later worksheets.

ANSWER: HOT DOGS
(A)


In this problem the student is asked to recognize a numerical sequence. Three is added to the number just prior to it in this pattern.
ANSWER: $\begin{array}{lllllllll}1 & 4 & 7 & 10 & 13 & 16 & 19 & 22\end{array}$

Use the thermometers shown in your small-group session, asking different questions from the ones on the worksheet. Be sure students know that the unnumbered marks represent $5^{\circ}$ increments. Al so be sure to ask a questicn that requires them to go "below zero" on the scale.

The last question requires that they use personal knowledge of Celsius temperature to answer "real world" questions. It would be helpful if you would permanently post a large picture of a thermometer in the classroom, with some "benchmark temperature" readings they can interpret intuitively. A modified version of this scale could be used:

Try to remember these as "check puin is" for estimating the temperature, of other things in the Celsius scale.

ANSWERS:
(A) Fall
(B) $30^{\circ} \mathrm{C}$
(C) No
$6 \quad 1007 \quad$ Both of these patterns may be easier to recognize if the student looks at the pattern from right to left.
ANSWERS: (A)

(B)

In your small-group session, go over this estimating process several times with different numbers. Give them a prortice page with 10 such problems, and the solutions, for then to use at home.
When they turn in their papers, have this problem taped to the desk. Students can't use a pencil; they whisper the answer to the person taking up the papers. If the student says "800," they earn the stars - if not, they don't.
Problem: 213
478
$+122$

Comment
Students have previously been introduced, intuitively, to the concept of finding an average (or "mean") in worksheet XII, \$1. In your small-group session, return to the "stacking of pennies to get the same height" model--show students concretely how this numerical answer could have been arrived at by adding all 3 numbers, and dividing by 3 . Take another example with 4 stacks of pennies - $10 ¢, 8 \ell, 12 \phi$, and 6\&. Show that if they add and divide by 4, they'11 get the right amount for each stack the same size. Actually construct the 4 stacks to show them.

Then talk about this problem - have "1 hour of sunshine ${ }^{\prime \prime}$ written on 40 index curds - make 5 piles, and then say "how could we make the piles all the same height? How could we find the average without making the piles? (Add and divide by 5.) How could we check our calculated answer?" (Make the 5 piles all the same size, and check.)

ANSWER: 8

Students probably did this "4-color map problem" in a 2nd grade worksheet, for the Southeastern United States. But they'll enjoy doing it again. In your small-group session, you might encourage them to use a pencil and R, B, etc. (So they can erase and start over, if necessary.)

You can show a completed map to the class in the small-group session since it's very unlikely that any two solutions would ever be identical. Call their attention to the "4-corner area" checked below, and the fact that "opposite states" can be the same since they only meet in a point.

ANSUER:
This is one solution.

Students are still using a geometric figure in an equation, at this point. They can solve the equation easily by "working backwards" mentally ( $67-28=$ ). In your small-group session, point out the similarity in this problem and problem 5.

ANSWER: 39

4

Have students make simple closed curves and various types of non-simple closed curves with string.

ANSWER: Curves $A, D, E, F$ and $H$ will be colored.
Curves B and G are not closed and curve C has two interiors.

| Problem | Skill of Excellence | Comment |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1030 | This problem is to reinforce the skill of estimating the solution to money problems. Students should be encouraged to round off the given amount to the closest dollar (e.g., $\$ 5.95$ to $\$ 6$ ) before adding to find the estimate. If they compute an exact answer first, and then round off, they have not estimated at all, but merely computed and rounded off. Use the same problem, but with different dollar amounts, in your small-group. |  |  |  |  |  |
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|  |  |  |  |  |  |  |  |
|  |  | ANSWER: Between \$11 and \$16 |  |  |  |  |  |
| 2 | $\begin{aligned} & 1001 \\ & 1030 \end{aligned}$ | Like this problem above, this situation reinforces estimating with money. The first month, the cat will cost about $\$ 15$, and about $\$ 6$ for each of the remaining 11 months of the year. The total estimate would then be given by $\$ 15+\$ 66$, or $\$ 81$. Notice that this problem also reinforces the skill of multi-step word problems. In your problem-solving session, extend the problem you do for 1 above to an entire year. |  |  |  |  |  |
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|  |  |  |  |  |  |  |  |
|  |  | ANSWER: Between \$80 and \$85 |  |  |  |  |  |
| 3 | $\begin{aligned} & 1006 \\ & 1127 \end{aligned}$ | Students find the volume of this shape, by counting unit blocks. It might be difficult for some students since they have to account for blocks that aren't visible. Encourage them to make such a shape, at home, from sugar cubes. |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
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|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  | ANSWER: 21 |  |  |  |  |  |
| 4 | 1002 | This problem is intended to reinforce using a chart as a problem-solving organizer. In your session, do the first 2 problems ( 32 and $26 d$ ) with real coins. |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  | AMSUER: |  |  |  |  |  |
|  |  |  | No. of |  |  |  |  |
|  |  | Amount | coins used | Quarter |  | Nickel |  |
|  |  | Amount |  | Quarter | Dime | Nickel | Penny |
|  |  | 32, | 4 | 1 |  | 1 | 2 |
|  |  | $26 ¢$ | 2 | 1 |  |  | 1 |
|  |  | 453 | 9 |  |  | 9 |  |
|  |  | 152 | 2 |  | 1 | 1 |  |
|  |  | 19 L | 7 |  |  | 3 | 4 |
|  |  | 388 | 5 | 1 | 1 |  | 3 |
|  |  | 204 | 2 |  | 2 |  |  |
|  |  | NOTE: | Answers | may vary. |  |  |  |

A computational puzzle that requires ingenuity is presented in this situation. The student has to study the subtraction problems and figure out how such answers could be arrived at in a consistent fashion. All teachers will immediately recognize that the student is finding the difference of the' "ones digits," rather than borrowing to resolve the impasse.

In your small-group session, encourage those who observed what was wrong explain it to the others.

ANSWER: 42

Students have a chance to demonstrate knowledge of "parallel" and "perpendicular" in this problem. In discussing the problem with them, ask how they can check to see if 2 lines are parallel (measure them at 2 different places, and see if they're the same distance apart at the 2 places). They can check perpendicularity by tearing off the corner of a sheet of paper, and using it as a "right angle tester."

ANSWER: There are several correct answers to this problem.

Students should list all the letters of the alphabet to start this problem-and then put the money values at beside the letters. This helps make the problem more concrete. They add the money values for each letter in the principal's last name, to get the total value. In your session, have them find the value of someone el se's last name.

ANSWER: variable. An example would be:

$$
\text { "Brown"--72ф } \quad(2 \phi+18+15+23+14)
$$

Recognizing odd vs. even numbers is the skill being reinforced in this problem. By the third grade, students should recognize that even numbers always end in $0,2,4,6$, or 8 , and odd numbers in $1,3,5,7$, or 9 . Classify the name you used above, in your small-group session.

ANSWER: variable, depending on the principal's name. The example above would be "even" since $72 \&$ is an even number of cents.

Students can solve this problem if they're familiar with reading time schedules from a chart. This is a "real world" situation--the television schedule given is from a paper.

ANSWER: (a) 8:30
(b) $11 / 2$ hours $(10: 00$ till 11:30)
(c) 2 hours (7:30 till 8:30, and

9:00 till 10:00)

Problem
1
1010 1125

2,3 1004
1167
1168

Comment
Hopefully students will actually take a guess on this problem, as directed to, before finding the actual lengths and comparing them. The surprising thing to most people is that, although the height always looks longer than around the top, the reverse is usually true. This problem, if a student goes through this procedure, is an exercise in making a tentative hypothesis, and then checking it out. (And this is one of the few cases in which the original hypothesis will invariably be false.) This problem also involves comparing two lengths in an unusual way--the student might have to use a string to measure around the top, for example.

In your small-group session, have a glass for the students to consider. Discuss how they could actually measure it at home, to verify or reject their guess.

ANSWER: The acceptable answer would be that it's longer around the top. If a student has a different answer, don't give credit unless the glass is brought in.

These 2 exercises can probably be solved by "guess-check-revise." Since the problem is to be read left-to-right, and the steps done in that order, the situation is similar to following a flowchart, rather than solving a computational statement with parentheses. The use of a calculator to check the results reinforces skills 1167 and 1168.

In your small-group session, check out an example in which the numbers are put in the boxes at random.

ANSWERS: $5+4-7 \times 1 \div 2=1$
$5+4-2 \times 1 \div 7=1$
(There may be others also.)

This prohlem is a multi-step word problem that inGolves very careful reading. Since Bob spent $25 \not$ each afternoon after school, his total savings for the week would be $\$ 2-\$ 1.25$, or $\$ 0.75$. At this rate, students can add $\$ 0.75$ enough times to produce $\$ 8$, and count the number of addends. Solve a similar problem, but with difierent numbers, in class.

ANSWER: 11 weeks

Demonstrate a few steps of the solution to this problem concretely in class, with 2 bowls to represent cages, and cut-outs of the hamsters. Have children see the value of organizing their approach by perhaps first listing all 3 in cage 1, then all 3 in Cage 2, then $A B$ in 1 with $C$ in 2 , etc.

ANSWER: 8 ways $\quad-\quad \frac{\text { Cage } 1}{A B C} \quad$ Cage 2

|  | ABC |
| :---: | :---: |
| $A B$ | $C$ |
| $A C$ | $B$ |
| $B C$ | $A$ |
| $A$ | $B C$ |
| $B$ | $A C$ |
| $C$ | $A B$ |


| 8 | 1109 | In your small-group session, review how students can test for right, obtuse, or acute angles (worksheet VI, (4). Al so be sure they can name an angle using 3 points, with the vertex always listed as the middle point. The symbol" "below is optional. <br>  |
| :---: | :---: | :---: |
| 9 | 1146 | This problem should not be difficult for students, except that "ordered pair" notation is used for the first time (instead of "go East," then "go North"). In your small-group session, cover this notation by picking out various letters on the graph, and having students write their addresses, using ordered pair notation, on scratch paper. Then reverse it - give them a few ordered pairs, and have them tell the letter they find there. |
|  |  | ANSWER: You just won two stars. |

## TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| ? | 1022 | Ask similar questions in your small-group session, to be sure students can correctly read the graph. |
|  |  | ```ANSWER: Music show 75 minutes (or 1 hr, 15 minutes)``` |
| 2 | 1004 | This is a situation that calls for "guess-check-revis? " tur 3rd graders. In your small-group session, star't by saying, "What are we asked to find - the twin's age! So let's guess what their age might be, and check and see if we are right. If not, we'll change our guess to get closer." |
|  |  | Start with a guess of 5. Then write Alice $=5$, Andy $=5$, so Mom $=24+5=29$. Now is it true that Alice + Andy + Mom $=60$ ? Check it out - if so, we're through, because "5" works. $5+5+29=39$. OOPS! Our guess of 5 must not be right. Let's guess again should we guess higher or lower? Continue for one more guess like this. |

ANSWER: 12

Be sure to use the word "volume" in briefly covering this problem in class. Students can build such a design from sugar cubes if they have trouble visualizing it.

ANSWER: 33 blocks

4
1156
Bring a sack to class, and put in several objects that are alike except for color. Ask several probabilitytype questions, using a verbal response like "the chances are 4 out of 5 that ....," and having the students write " $4: 5$ or $4 / 5^{\prime \prime}$ on scratch paper. Be sure to ask one problem of the "complimentary sort," and have students solve it concretely.

ANSWER: 2:3 or 2/3

Students wili probably use either addition or subtraction to solve this, in one of two ways:

$$
\begin{array}{ll}
\text { one way: } & 29-11=18 \mathrm{yrs} . \text { added } \\
& 18+36=54 \mathrm{yrs.} \text { old }
\end{array}
$$

another way: $36-11=25$ yrs. diff. in age
$29+25=54$ yrs. old
Note that some might solve it concretely using a number line, and simply counting.

ANSWER: 54 years old

Students solve this problem by actually listing the license plates used. Many will notice the pattern that allows an organized list to be made.

ANSWER:


You might have to refresh student's memory on ordered pair notation. Take the first few points listed, and find them on the graph, making the connecting line.

ANSUER:


This problem involves determining a reasonable answer when working with familiar objects and their length. Be sure that students have some "benchmark" lengths that they're familiar with, to use in such situations. For example, the width of their finger is about 1 cm , their height is a little over 1 meter ( 100 cm ), etc. From such comparisons with familiar objects, they should be able to eliminate the other three choices as unreasonable.

ANSWER: b

## TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1050 | The only difficult part of this problem is that "borrowing" must be considered in each step. In your small-group session, go over a similar problem. |
|  |  | ANSHER: $\begin{array}{r}96682 \\ \\ -38446 \\ \\ \\ 583\end{array}$ |
| 2 | 1007 | In your small-group session, have students describe what they see about the pattern. Some will just notice the single-digit counting pattern, while others might notice things like Column A being the multiples of 3, etc. Take a few numbers other than 22 and 96, and have students tell how they'd find where they would be. [A number like 22 is small enough to be found by counting; 96 was used to force students to look for another method, too.] <br> ANSWER: a. 8 <br> b. B <br> c. $A$ |
| 3 | $\begin{aligned} & 1006 \\ & 1007 \end{aligned}$ | Have students describe briefly what they noticed about the shapes. In this pattern, the outside shape is the previous figure's center shape, and the circle is a constant. |
|  |  | ANSHER: |
| 4 | 1144 | Call students' attention to the "key" at the bottom of the page, and the "half symbol" used in Mr. Smith's class. |
|  |  | ANSWER: a. 33 <br> b. 87 |



The area of $A$ can be found by completing the rectangle, which has area 2, and taking half of that.

This "making a rectangle," and then taking half the rectangle, is a new concept to these students. But it's a powerful one, and needs to be followed through in regular class work.

ANSWER: 8, 9, 10, 11,or 12 are acceptable answers.

ANSWER:


This problem gives an opportunity to estimate measurements using metrics. Perimeter is a term. the student should be becoming familiar with. (Note: There is an example of a square centimeter on the page. The student may use this to help with the measurement.)

ANSWÉR: a. Acceptable 7 or 8 cm
b. Acceptable 19, 20 , or 21 cm

TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | $\begin{aligned} & 1001 \\ & 1168 \end{aligned}$ | This is a multi-step word problem that encourages the use of a calculator. Note that it's a mathematical problem that has an answer other than a number. One way of solving the problem is to notice that $9 \times 15$ is 135 , which is more than 125 rabbits, so he' 11 need rabbit food. Likewise, $2 \times 29$ is 58 , but 58 is less than 75, so he doesn't need dove food. <br> ANSWER: <br> b. rabbit food only |
| 2 | $\begin{aligned} & 1107 \\ & 1126 \end{aligned}$ | This problem shows that various rectangles can have the same area. In your small group session, take a similar problem (like all those with area 20) and go through the procedure. This problem and a previous one (Worksheet VIII, \%) can be used as intuitive introductions to prime vs. composite numbers; "12" and "24" are composite numbers because you can make more than one rectangle - "ll" is prime, though, because there's only one rectangle you can make. <br> ANSWER: The three rectangles are a 1 by 12 , a 2 by 6 , and a 3 by 4. |
| 3 | 1003 | The purpose of this problem is to reinforce the skill on "drawing a diagram" to solve a verbal problem. Therefore, the diagram is a very important part of the answer. It should be a line drawing, a.d look something like: |

MY DIAGRAM


ANSWER: Airhead ran 540 feet.

This problem allows the student to collect data for an experiment, and fill it in on an appropriate table. There's no way to tell positively that the student actually made all 50 tosses, but assume they did if the table has 50 tally marks in it. In your smallgroup session, start off the experiment with 10 tosses, and record the data using tally marks. They can finish it at hame.

ANSUER: The table correctly filled in is an essential part of the answer--the other part will depend on the results they got, but will almost always be choice (c). If there's an answer other than that, check to see if the answer matches their own data, and if so, give them credit.

In your small-group session, make a similar graph for Easter eggs. Notice that, on the given graph, the numbers will go along the horizontal axis while the categories go along the vertical - this may cause some children difficulty.


325

This problem is not specifically related to one of the Standards of Excellence skills, but is certainly within the grasp of children who have a good understanding of the ratio interpretation of a fraction. The fractions should be interpreted as "3 out of 5" and "2 out of 5," and students can then figure the answer by drawing a diagram of sets, as in:


## TEACHER COMNENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | 1006 | Students will have to use spatial visualization skills to solve this problem. In your small-group session, you might have a Rubik's cube to show the class and have a student take it apart and show others 1 cube of each type. |
|  |  | $\begin{array}{lr} \text { ANSMERS: } & 8 \\ & 12 \\ & 6 \end{array}$ |
| 2 | $\begin{aligned} & 1004 \\ & 1002 \end{aligned}$ | Students will likely use "guess-check-revise" to solve this problem. They might start by guessing 10 of each coin, check it to see that 10 dimes and quarters would total $\$ 3.50$, so revise the guess downward. |
|  |  | Some might approach it by listing: <br> 1 dime: 1 quarter $=35 \$$ <br>  <br> 3 dimes, 3 quarters $=\$ 1.05$ etc., <br> till they find the amount that yie?ds $\$ 2.45$. |
|  |  | In your small group session, take a similar problem (perhaps pennies and nickels tha! total $36 \AA$ ) to solve. |
|  |  | ANSWER: 7 dimes and 7 quarters |

In this problem the student must estimate the solution. Most children will cross out the pies on the worksheet in order to arrive at the answer.

ANSWER: b. $41 / 2$

41046
Remind students that they need to evaluate the two sides of the expression independently before making a comparison. Some will notice that you don't have any computation to do in (c), if they're clever.
ANSWER:
a. >
b. <
c. >


In your small-group session, have some pictures that students can fold to find the line of symmetry, or that there is no such line.

ANSWER:


Students should not need help with this problem, unless they've learned to tell time exclusively on digital watches.

ANSHER:


Be sure you show students, by example, how to work the parentheses first, and then the rest of the expression. Also, be sure that they know which digital numbers are considered to represent which letters of the alphabet - otherwise, a student might have a correct numerical answer, but not be able to translate it into an English word.

ANSWER: 35006 - EDOSE

TEACHER COMMENTARY


## 6,7 1153

1155
1157
"Line of symmetry" is reinforced in this problem. In your small-group session, show students how they might fold the paper to do the tracing, or use another method that involves the line of symmetry.

ANSWER:


In your small-group session, have 2 students flip coins 12 times and make tally marks on the board for the 2 categories listed. Then select the appropriate answer for problem 7, based on the data just collected. ( 12 times was selected because they can intuitively figure out $1 / 4,1 / 2,3 / 4$ of twelve.) Students can then re-do the experiment at home - they should do a larger number of tosses, of course, and you might want to give them numbers of tosses (48, e.g.) that will work out computationally as " 12 " does.

ANSWERS: 6. Check data for 40 tally marks.
7. The answer selected should match the student's data, but if they did the experiment a large number of times, the 2 nd response (half of the time) would be correct.

## TEACHER COMMENTARY

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | $\begin{aligned} & 1005 \\ & 1004 \end{aligned}$ | Students can solve this problem either by "working backwards," or by "guess-check-revise." By this time in the school year, you can just mention these 2 approaches in your problem-solving session, and briefly discuss what each would mean for this problem. |
|  |  | ANSWER: 7 |
| 2 | 1073 | In your small-group session, take 2 similar problems and have students decide whether or not they should be colored. One problem should yield an odd answer, while the other yields an even answer. You might introduce intuitively, language like "in this case, we had an odd number times an odd number, and got an odd answer." |
|  |  | ANSWER: Flowers 1, 2, and 4 are colored. |
| 3 | $\begin{aligned} & 1050 \\ & 1004 \end{aligned}$ | Students can solve this by simply guessing where the line should go, and then adjusting the line to give the right answer. Some students might notice that you can "work backwards" by starting at 0 and adding numbers to get 51 , rather than starting at 51 and subtracting to get 0 . |
|  |  | ANSMER: |
| 4 | 1109 | Students should have no trouble with this problem by this time of the year. |
|  |  | ANSWER: $X$ on angles 2, 4, 6 |

Encourage students to use the "count back" method of sol ving this problem. To do so, you'll have to assume the child gave all $\$ 3.00$ to the clerk (which he would not really do, because it cost less than $\$ 2.00$ ), and the clerk "counted back" his change.

ANSWER: group 3 (\$1.35)

In your small-group session, consider a similar problem. Be sure that students realize that the marks shown stand for $2^{\circ}$ increments, and that the mercury is between 2 marks. They have to be able to read such a temperature before they can even begin the problem.

ANSWER: $32^{\circ} \quad\left(47^{\circ}-15^{\circ}=32^{\circ}\right)$

In your small-group session, ask "how much would you pay for 50 marbles?" Repeat this for 75 marbles. Students will first have to determine how many bags would be needed to heve 150 marbles; they would then have to either use repeated addition or multiplication to a $\rightarrow$ mer the question asked.

ANSWER: \$2.10

In your small-group session, either take a similar puzzle and solve it, or show how to do only one step of this puzzle.

ANSWER: $6 \times 6=36$

$$
\begin{aligned}
& 2 \times 3=6 \\
& == \\
& 3 \times 2=6
\end{aligned}
$$

| Problem | Skill of <br> Excellence |
| :---: | :---: |
|  | 1107 <br> 1108 |

Comment
In your small-group session, do the same problem, but with the digits $0-؟$. Depending on how you make the digits, you might likely have 1 and 4 circled, and 4 checked also.

ANSWER: O'd: AEFHIKLMNTVWXYZ
Ad: EFHILT

21009

31003
1007

41004

1004
1050
Suggest to students that they draw the next two sizes of triangles similar to those shown. The 4th one has 5 circles per side, and the 5 th has 6 .

ANSWER: 15, 21

Some s.tudents will adjust the line that doesn't work, till they get it positioned correctly. Others will simply guess where the line should go, and a few might try some sort of "pairing" of high and low numbers.
ANSWER:


Solve a similar problem in the small-group session, showing how they can either simply "guess-check-re- vise," or modify this approach because of the digits they can see, and their knowl edge of fundamental addition facts. Use this problem:


ANSWER: 9

Have the students in your small-group session first identify when they might use this method (when there is "carrying" involved - otherwise it's inappropriate). Also have them practice several in class using either of the given addends to "add a little to." (In the example shown, Tamike might have added 4 to 46 to start with, instead of 2 to 28.)

Be sure to continue this method of mental arithmetic drill throughout the year.

Have this problem taped to the table when children turn in their papers--they can whisper the answer to you for their stars.

$$
38+47
$$

ANSNER: 85

| Problem | Skill of Excellence | Comment |
| :---: | :---: | :---: |
| 1 | $\begin{aligned} & 1004 \\ & 1050 \\ & 1005 \end{aligned}$ | In your small-group session, have students solve a similar problem using "guess-check-revise." You can have them each make such a problem themselves to give a friend to solve--in so doing, they should work backwards mentally by writing the whole addition problem and answer, and then covering up any place a particular digit appears. |
|  |  | ANSWER: 6 |
| 2 | $\begin{aligned} & 1107 \\ & 1108 \end{aligned}$ | Review "parallel" for the students, and perhaps check several letters till you find one that is both circled and checked. |
|  |  | ANSWER: E,F,H,I,M,N,Z are checked. <br> Note: "U" doesn't qualify - the bottom is a curve. "W" also, because the lines are almost, but not quite, parallel. |
| 3 | 1006 | This problem is an extension of a problem introduced earlier in the year. You might have them solve the same problem, but for a similar figure (perhaps [D]) in your small-group session. <br> ANSWER: 15 |
| 4,5 | $\begin{aligned} & 1153 \\ & 1149 \\ & 1157 \end{aligned}$ | Taken together, these problems have the student collect and record data for a probability experiment. The conclusion reached is not one that requires a numerical answer, but in your small-group session you might decide to cover this in addition to the "more likely" notion. You might actually do the problem in your small-group session, only throwing 20 times. Then the students would do it again at home. |
|  |  | ANSWER: 4. Check to be sure the number of tally marks is 40. <br> 5. This answer should match the data in problem 4 above. |

This problem incorporates several skills from standards of excellence, including an intuitive notion of "tax." In your small-group session, it should suffice to point out to students that Charles is thinking of a cone with 2 scoops on it, and he knows about adding tax. Hopefully students will realize that using a calculator doesn't ensure Charles gets a correst answer.

ANSWER: The answer is reasonable.

Students had a similar prohlem in worksheet IV, \#9. Be sure they realize that "JEXUMS" is an imaginary word, but that each side of the square must be "1 JEXUM." NOTE: The circle is about the size of a dime. Mark off the $P$ and roll the dime.

ANSWER: 13 JEXUMS

Ask students what $\$ 14.99$ has to do with the problem itself.

ANSWER: 8


[^0]:    

    * Reproductions supplied by EDRS are the best that can be made * * Erom tho original docunont.
    

[^1]:    This will likely be the student's initial exposure to a mathematical lowchart. They. ed to practice with t. ie types if flowcharts--they will be meeting more .icult ones shortly, in succeeding worksheets.

    ANSHER: 3

